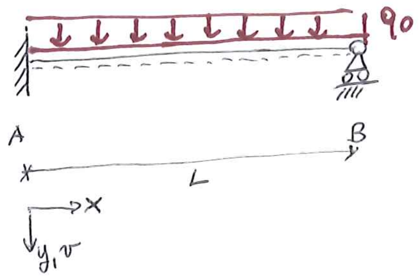
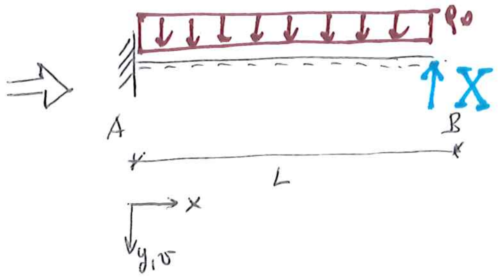
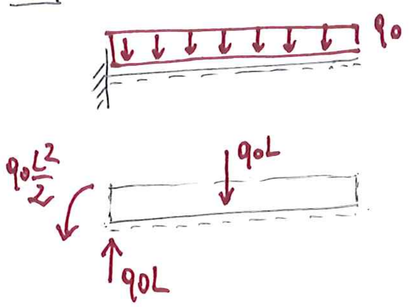
RISOLUZIONE DI STRUTTURA IPERSTATICA E CALCOLO DI COMPONENTE DI SPOSTAMENTO



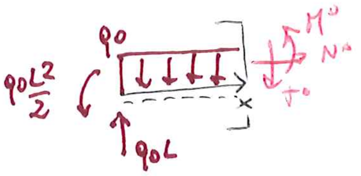


$$\boxed{v_{(B)}(q_0, X) = 0}$$

S0



$H_{0A} = 0; \quad V_{0A} = q_0 L; \quad M_{0A} = q_0 \frac{L^2}{2}$

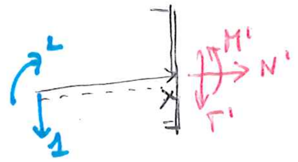


$N_0(x) = 0; \quad T_0(x) = q_0 L - q_0 x = q_0(L - x)$

$M_0(x) = -q_0 \frac{L^2}{2} + q_0 L x - q_0 \frac{x^2}{2} = -\frac{q_0}{2}(L - x)^2$

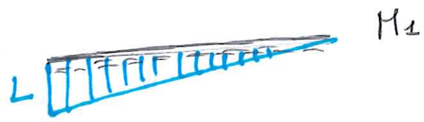
S1

$H_{1A} = 0; \quad V_{1A} = -1; \quad M_{1A} = -L$



$N_1(x) = 0; \quad T_1(x) = -1;$

$M_1(x) = L - x$



$$\varepsilon_x = \frac{1}{EA}\left(N_0(x) + X N_1(x)\right) = 0$$

$$\gamma_x = \frac{1}{GA_T}\left(T_0(x) + X T_1(x)\right) = \frac{q_0(L-x) + X(-1)}{GA_T}$$

$$\chi_x = \frac{1}{EJ_x}\left(M_0(x) + X M_1(x)\right) = \frac{-\frac{q_0}{2}(L-x)^2 + X(L-x)}{EJ_x}$$

$\delta L_e = \delta L_i \qquad \delta L_e = 1 \cdot v_B = 1 \cdot 0 = 0 \qquad \delta L_i = 0$

$$\delta L_i = \int_0^L \cancel{N_1(x)\, \varepsilon_x\, dx} + \int_0^L T_1(x)\, \gamma_x\, dx + \int_0^L M_1(x)\, \chi_x\, dx =$$

$$= \int_0^L T_1(x) \frac{T_0(x) + X T_1(x)}{GA_T} dx + \int_0^L M_1(x) \frac{M_0(x) + X M_1(x)}{EJ} dx =$$

$$= \int_0^L -1 \left(\frac{q_0(L-x) + X(-1)}{GA_T}\right) dx + \int_0^L (L-x)\left(\frac{-\frac{q_0}{2}(L-x)^2 + X(L-x)}{EJ_x}\right) dx =$$

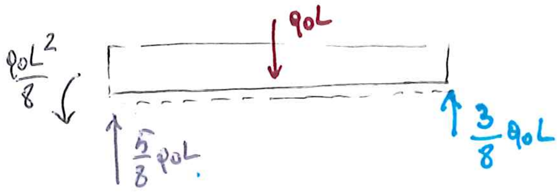
$$= \int_0^L \left(\frac{-q_0(L-x)}{GA_T} + \frac{X}{GA_T} \right) dx + \int_0^L \left(\frac{-q_0/2\,(L-x)^3}{EJ_x} + \frac{X(L-x)^2}{EJ_x} \right) dx =$$

$$= \int_0^L \frac{-q_0(L-x)}{GA_T} dx + \int_0^L \frac{-q_0(L-x)^3}{2EJ_x} dx + X \left[\int_0^L \frac{1}{GA_T} dx + \int_0^L \frac{(L-x)^2}{EJ_x} dx \right] = 0$$

$$\frac{1}{GA_T} \int_0^L q_0(L-x)\,dx + \frac{1}{2EJ_x} \int_0^L q_0(L-x)^3 dx = X \left[\frac{1}{GA_T} \int_0^L dx + \frac{1}{EJ_x} \int_0^L (L-x)^2 dx \right]$$

$$\frac{q_0 L^2}{2GA_T} + \frac{q_0 L^4}{8EJ_x} = X \left(\frac{L}{GA_T} + \frac{L^3}{3EJ_x} \right) \rightarrow X = \frac{q_0 \left(\frac{L^2}{2GA_T} + \frac{L^4}{8EJ_x} \right)}{\frac{L}{GA_T} + \frac{L^3}{3EJ_x}}$$

TRASCURANDO LA DEFORMABILITÀ A TAGLIO: $\boxed{X = \frac{3 q_0 L}{8}}$



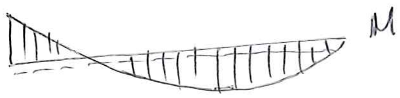
$H_A = H_{0A} + X H_{1A}$ $\quad$ $H_A = 0$

$V_A = V_{0A} + X V_{1A}$ $\quad$ $V_A = q_0 L + \frac{3}{8} q_0 L (-1) = \frac{5}{8} q_0 L$

$M_A = M_{0A} + X M_{1A}$ $\quad$ $M_A = q_0 \frac{L^2}{2} + \frac{3}{8} q_0 L (-L) = \frac{q_0 L^2}{8}$

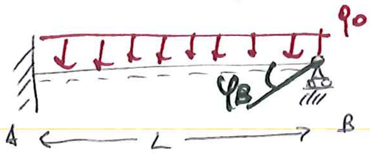
$N(x) = N_0(x) + X N_1(x)$ $\quad$ $N(x) = 0$

$T(x) = T_0(x) + X T_1(x)$ $\quad$ $T(x) = q_0(L-x) + \frac{3}{8} q_0 L$



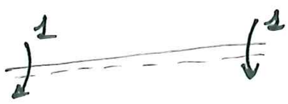
$M(x) = M_0(x) + X M_1(x)$ $\quad$ $M(x) = -\frac{q_0}{2}(L-x)^2 + \frac{3}{8} q_0 L (L-x)$

• CALCOLO DELLA COMPONENTE DI SPOSTAMENTO $\boxed{\varphi_B}$:

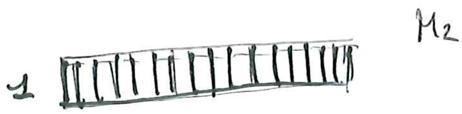


$\boxed{\varphi_B = ?}$

S_2|



$H_A = 0$; $V_A = 0$; $M_A = -1$;



$M_2(x) = 1$

$$\varepsilon_x = \frac{1}{EA}\left(N_0(x) + \overline{X} N_1(x)\right) = \frac{1}{EA}\left(N_0(x) + \frac{3}{8} q_0 L \, N_1(x)\right)$$

$$\gamma_x = \frac{1}{GA_T}\left(T_0(x) + \overline{X} T_1(x)\right) = \frac{1}{GA_T}\left(T_0(x) + \frac{3}{8} q_0 L \, T_1(x)\right)$$

$$\chi_x = \frac{1}{EJ_x}\left(M_0(x) + \overline{X} M_1(x)\right) = \frac{1}{EJ_x}\left(M_0(x) + \frac{3}{8} q_0 L \, M_1(x)\right)$$

$$\delta\mathcal{L}_e = \delta\mathcal{L}_i \qquad \delta\mathcal{L}_e = 1 \cdot \varphi_B = \varphi_B$$

$$\delta\mathcal{L}_i = \cancel{\int_0^L N_2(x)\, \varepsilon_x \, dx} + \cancel{\int_0^L T_2(x)\, \gamma_x \, dx} + \int_0^L M_2(x)\, \chi_x \, dx =$$

$$= \int_0^L M_2(x) \, \frac{M_0(x) + \overline{X} M_1(x)}{EJ_x} \, dx = \int_0^L M_2(x) \, \frac{M_0(x) + \frac{3}{8} q_0 L \, M_1(x)}{EJ_x} \, dx =$$

$$= \int_0^L \left[\frac{M_2(x) M_0(x)}{EJ_x} + \frac{M_2(x) \frac{3}{8} q_0 L \, M_1(x)}{EJ_x}\right] dx =$$

$$= \frac{1}{EJ_x} \int_0^L 1 \left[-\frac{q_0}{2}(L-x)^2\right] dx + \frac{1}{EJ_x} \int_0^L 1 \cdot \frac{3}{8} q_0 L \, (L-x) \, dx =$$

$$= \frac{-q_0}{2EJ_x} \left[\frac{x^3}{3}\right]_0^L + \frac{3 q_0 L}{8EJ_x} \left[Lx - \frac{x^2}{2}\right]_0^L =$$

$$= -\frac{q_0 L^3}{6EJ_x} + \frac{3 q_0 L^3}{8EJ_x} - \frac{3 q_0 L^3}{16EJ_x} = \frac{q_0 L^3}{48EJ_x} \qquad \boxed{\varphi_B = \frac{q_0 L^3}{48 EJ_x}}$$