

## Economia regionale e dell'innovazione, Scienze Economiche Lezione 2

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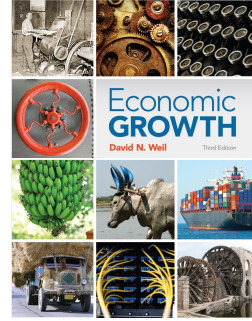
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## PHYSICAL CAPITAL



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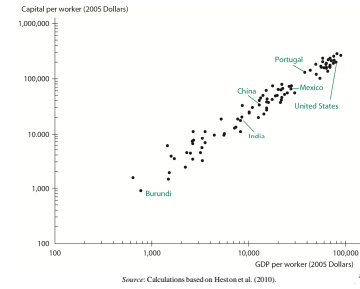
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## An interesting stylised fact: GDP and Capital per Worker, 2009



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### Nature of capital

- Capital is productive
- But it is has been produced itself...through investments. In other words capital is accumulated. Distinction between flows and stocks
- Capital depreciates
- Capital stock is made of machinery, tools, buildings, roads....
- It can be private or public (mainly infrastructures)

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### Early models of economic growth

- Harrod-Domar model
- Solow model

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### Capital's role in production

- Production function:

- $Y=F(K,L)$
- $Y/L=F(K/L, 1)$
- $y= f(k)$

NOTE: in a competitive environment alpha is the capital factor share. In a Cobb-Douglas model this is constant

#### SOLOW model: Cobb-Douglas PF

- $Y=F(K,L) = AK^\alpha L^\beta$
- Usually  $\alpha+\beta=1$  (assumption of no economies of scale), in this case we can rewrite the function above as follows:
- $Y=F(K,L) = AK^\alpha L^{1-\alpha}$ , which is also in per capita terms
- $y = A k^\alpha$

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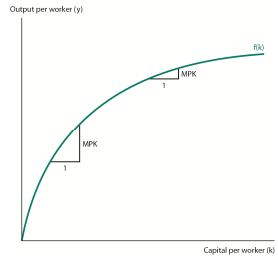
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**Solow model:** A Production Function with Diminishing Marginal Product of Capital




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Capital's role in production

In a competitive environment, where factors are paid according to marginal productivity, alpha is the capital factor share, and in a Cobb-Douglas model this is constant:

$$MPK = \alpha AK^{\alpha-1} L^{1-\alpha}$$

– Quota of income to capital:

$$-(MPK * K) / Y = (\alpha AK^{\alpha-1} L^{1-\alpha} * K) / AK^{\alpha} L^{1-\alpha} = \alpha$$

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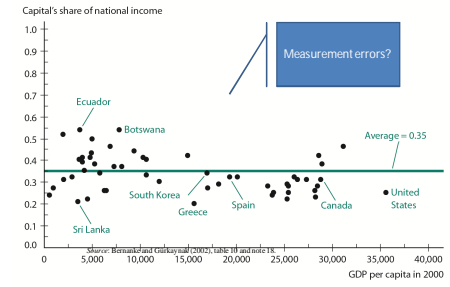
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Capital's Share of Income (which is equal to  $\alpha$ ) in a Cross-Section of Countries




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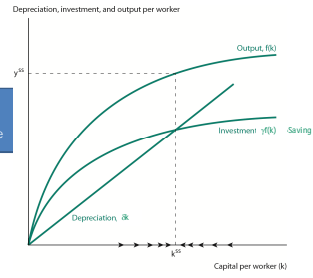
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### The Steady State of the Solow Model (with no population dynamics)

$\gamma$  = saving rate  
 $\delta$  = depreciation rate



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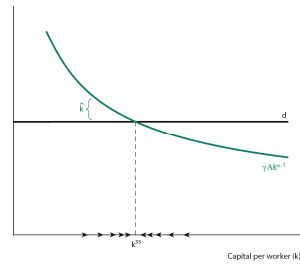
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### Speed of Convergence to the Steady State



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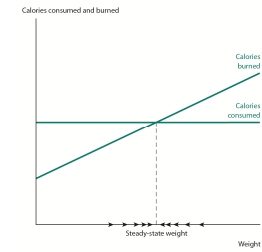
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### A non economic example: Determination of Steady-State Weight

Think also  
about  
changes in  
the position  
of the two  
lines



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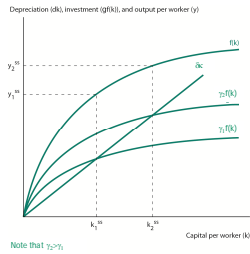
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### Effect of Increasing the Investment Rate on the Steady State




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### Solow model calibration

Using  $y = A k^\alpha$

- $\Delta k = \gamma A k^\alpha - \delta k$

In steady state  $\Delta k$  is equal to zero, that is

- $0 = \gamma A k_{ss}^\alpha - \delta k_{ss}$

Which implies that

- $\gamma A k_{ss}^\alpha = \delta k_{ss} \Rightarrow \gamma A k_{ss}^\alpha / k_{ss} \delta = 1 \Rightarrow \gamma A / \delta k_{ss}^{\alpha-1} = 1$

- $k_{ss} = (\gamma A / \delta)^{1/(1-\alpha)}$

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### Solow model calibration

- $y_{ss} = A k_{ss}^\alpha = A^{1/(1-\alpha)} (\gamma/\delta)^{\alpha/(1-\alpha)}$

- If we take the value of  $y$  of steady state for country  $i$  and country  $j$ , we can compare them in the following way

- $y_{ss}^i / y_{ss}^j = (\gamma^i / \gamma^j)^{\alpha/(1-\alpha)}$

- Now let us assume that country  $i$  has an investment rate of 20% and country  $j$  of 5%

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## Solow model calibration

- With alpha equal to 0.3 the previous formula gives a value of 2....
- ... do you remember the example of Sylvania and Freedonia?

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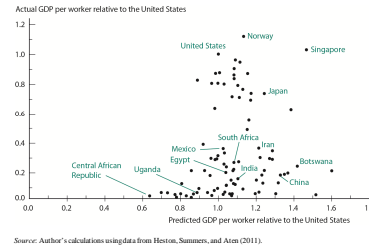
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## Predicted versus Actual GDP per Worker



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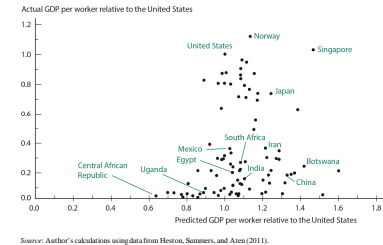
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## Predicted versus Actual GDP per Worker based a calibration of the Solow model



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### The Solow model as a theory of relative growth rates (difference btwn s.r. and I.r.)

The Solow model does not provide a complete explanation of growth rates since once a country reaches its steady state there is no longer growth!

*Despite this failing we may still ask whether the model has something to say about relative growth rates - that is why some countries grow faster than others...*

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### The Solow model as a theory of relative growth rates (difference btwn s.r. and I.r.)

#### The key is to think about countries which are not in s.s.

- *If two countries have the same rate of investment but different levels of income, the country with lower income will have higher growth*
- *If two countries have the same level of income but different rates of investment, then the country with a higher rate of investment will have higher growth*
- *A country that raises its level of investment will experience an increase in its rate of income growth*

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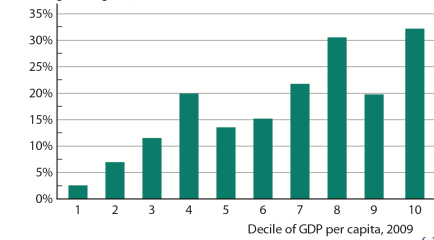
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### Saving rate: is it really exogenous? Saving by Decile of Income per Capita

Average saving rate, 2009



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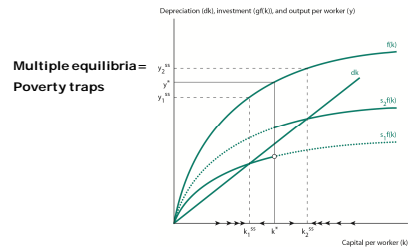
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### Solow Model with Saving Dependent on Income Level



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### The rise and fall of capital revisited

- The belief that capital accumulation is the key ingredient for economic growth reached its peak after WWII (see Arthur Lewis and Soviet Union's success)
- Policies were designed accordingly
- Now economist have discarded the idea that development depends mainly on capital accumulation

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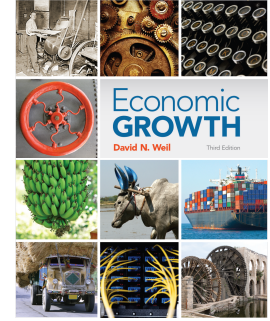
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### Chapter 4

## POPULATION AND ECONOMIC GROWTH



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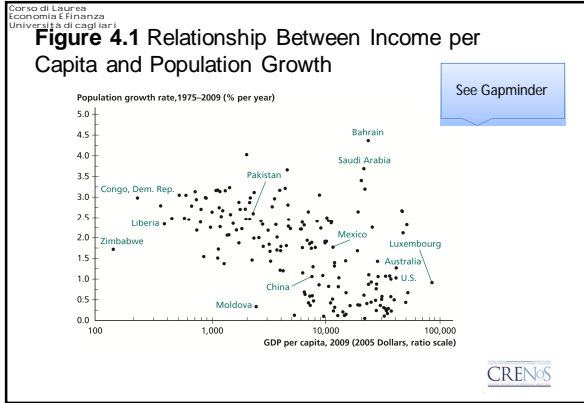
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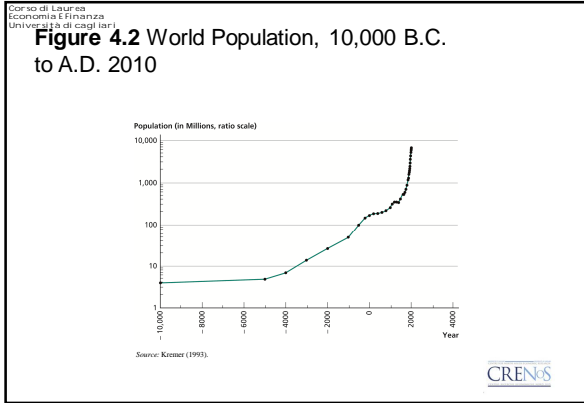
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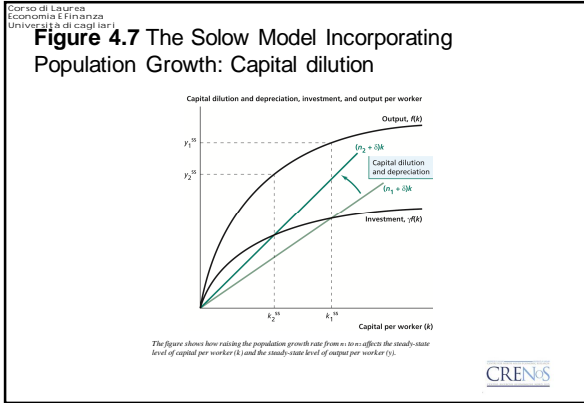
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## Population growth and capital dilution

- The solow model extended to incorporate population growth explains how higher population growth can lower income per capita through the channel of capital dilution
- The solow model can therefore partially account for the negative correlation between income per capita and population growth

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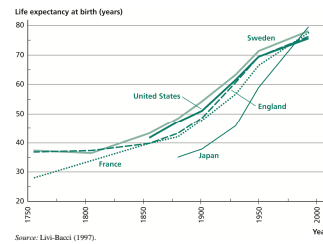
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### Figure 4.8 Life Expectancy in Developed Countries



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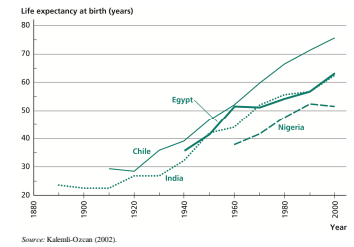
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### Figure 4.9 Life Expectancy in Developing Countries



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## Demographic transition: a tale of two traps...

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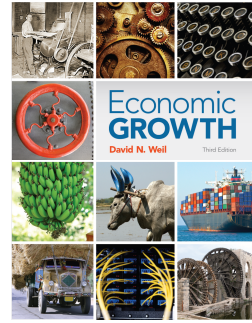
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## Chapter 6

### HUMAN CAPITAL



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## Human capital as an input

- We focus on qualities of people who are productive
- We concentrate on qualities which are produced, as with physical capital also human capital is itself produced
- Human capital earns returns (even though workers have to work to get it whilst capital owners can relax on a beach)

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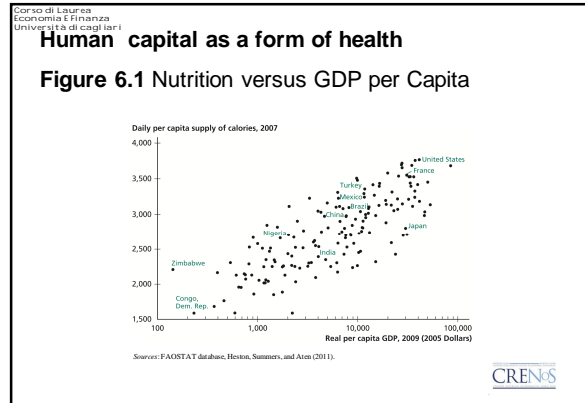
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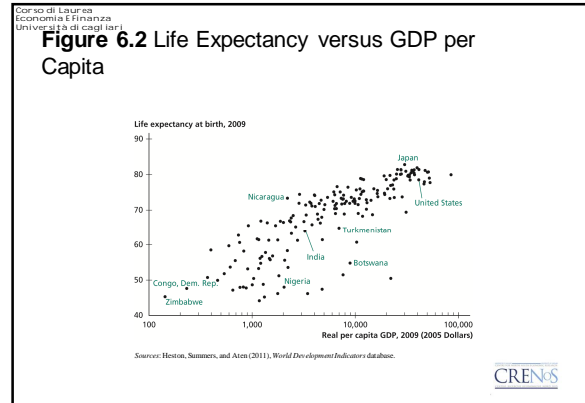
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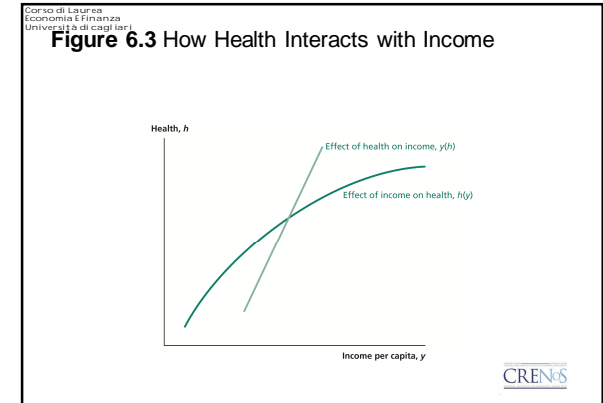
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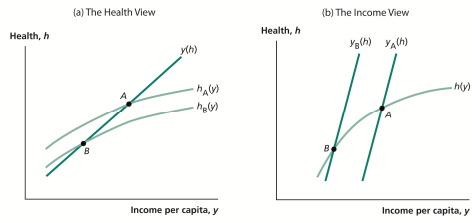
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**Figure 6.4 Health and Income per Capita:  
Two Views**




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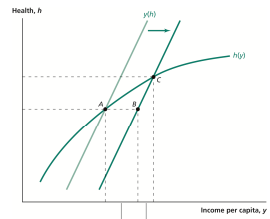
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**Figure 6.5 Effect of an Exogenous Shift in  
Income**



Increase in income due to exogenous shift

Increase in income due to health multiplier

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**Human capital in the form of education  
Table 6.1 Changes in the Level of  
Education, 1975-2010**

		Percentage of the Adult Population with				
		Average Years of Schooling	No Schooling	Complete Primary Education	Complete Secondary Education	Complete Higher Education
Developing Countries	1975	3.2	47.4	32.9	8.1	1.6
	2010	6.7	20.8	68.8	31.5	5.3
Advanced Countries	1975	8.0	6.2	78.8	34.9	8.0
	2010	11.0	2.5	94.0	63.9	16.6
United States	1975	11.4	1.3	94.1	71.1	16.1
	2010	12.4	0.4	98.8	85.4	20.0

Source: Barro and Lee (2010). Data for population > 25.

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## Education as an investment

- It is costly (6% of GDP in US, 4.5% in Italy)
- Not only in terms of money but especially in terms of opportunity costs (this is true mostly for developing countries)
- The return to education is wage...a wage premium

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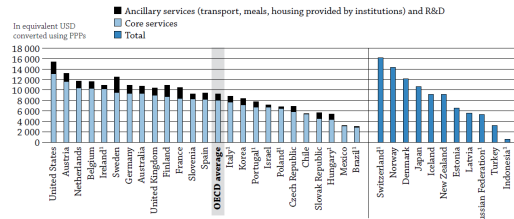
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**Chart B1.1. Annual expenditure per student by educational institutions, by type of service (2011)**  
In equivalent USD converted using PPPs, based on full-time equivalents, for primary through tertiary education



1. Public institutions only.  
Countries are ranked in descending order of expenditure per student by educational institutions for core services.

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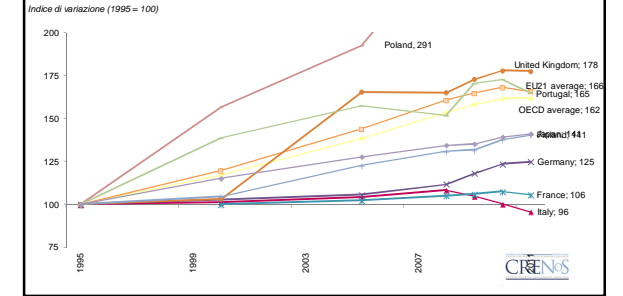
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## Change in per student expenditure total, constant prices(1995 = 100)

Table B1.5a




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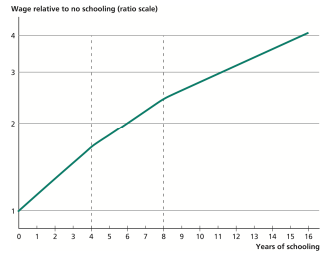
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**Figure 6.6** Effect of Education on Wages



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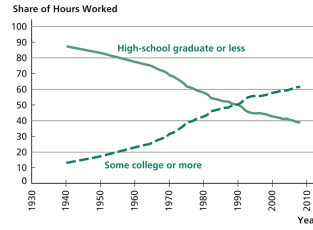
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**Figure 6.7** Share of Hours Worked by Education Level, 1940–2008



Sources: Autor, Katz, and Krueger (1998), Autor, Katz, and Kearney (2008), Acemoglu and Autor (forthcoming).

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**Figure 6.8** Ratio of College Wages to High-School Wages



Sources: Autor, Katz, and Krueger (1998), Autor, Katz, and Kearney (2008), Acemoglu and Autor (2010).

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**Table 6.2** Breakdown of the Population by  
Schooling and Wages

Highest Level of Education	Years of schooling	Wage Relative to No Schooling	Percentage of the Population	
			Developing Countries	Advanced Countries
No Schooling	0	1.00	20.8	2.5
Incomplete Primary	4	1.89	10.4	3.4
Complete Primary	8	2.43	18.0	12.3
Incomplete Secondary	10	2.77	19.3	17.8
Complete Secondary	12	3.16	23.2	37.4
Incomplete Higher	14	3.61	2.9	9.9
Complete Higher	16	4.11	5.3	16.8

Source: Barro and Lee (2010).

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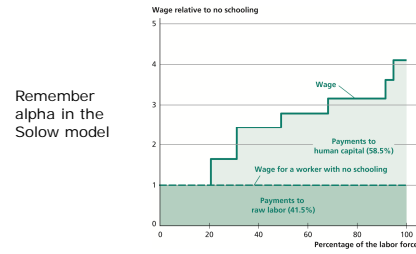
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**Figure 6.9** Share of Human Capital in Wages  
in Developing Countries



Remember  
alpha in the  
Solow model

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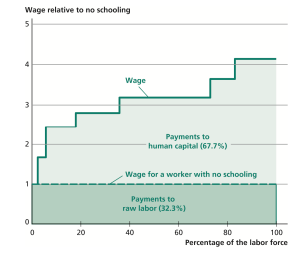
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**Figure 6.10** Share of Human Capital in Wages  
in Advanced Countries




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## Important factors to explain figure 6.12

- Quality of schooling
- Externalities

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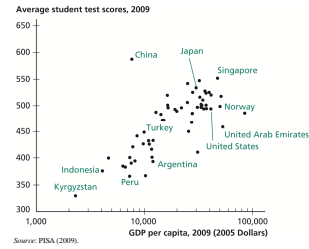
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### Figure 6.13 Student Test Scores versus GDP per Capita



Source: PISA (2009).

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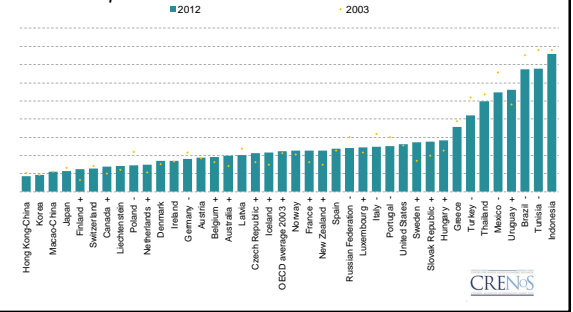
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## Percentage of low performers in Maths, PISA 2003-2012



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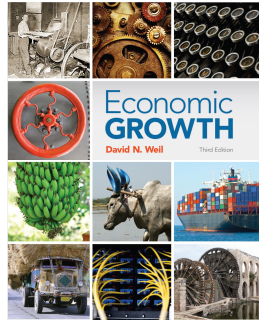
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# Chapter 7

## MEASURING PRODUCTIVITY



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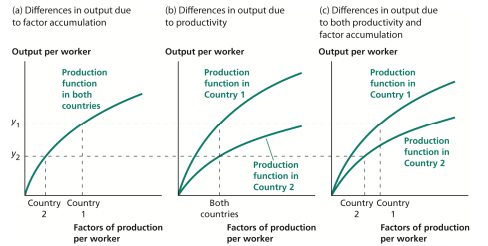
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### Figure 7.1 Possible Sources of Differences in Output per Worker



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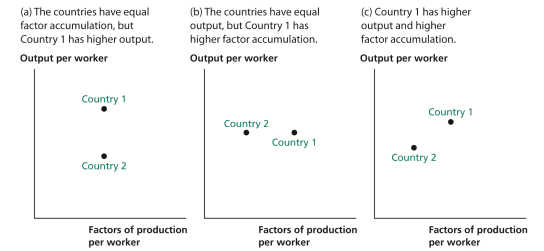
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### Figure 7.2 Inferring Productivity from Data on Output and Factor Accumulation



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## productivity accounting

- Ratio of output=
- Ratio of productivity \* Ratio of factors of production
- Ratio of productivity=
- Ratio of income/Ratio of factors of production

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**Table 7.1 Data Used to Analyze Productivity in Country 1 and Country 2**

	Output per Worker, $y$	Physical Capital per Worker, $k$	Human Capital per Worker, $h$
Country 1	24	27	8
Country 2	1	1	1

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**Table 7.2 Development Accounting**

Country	Output per Worker, $y$	Physical Capital per Worker, $k$	Human Capital per Worker, $h$	Factor of Production, $\alpha k^{1-\beta} h^{\beta}$	Productivity, $A$
United States	1.00	1.00	1.00	1.00	1.00
Norway	1.12	1.32	0.98	1.08	1.04
United Kingdom	0.92	0.85	0.87	0.80	1.03
Canada	0.80	0.91	0.96	0.91	0.88
Japan	0.73	1.16	0.98	1.04	0.70
South Korea	0.62	0.92	0.95	0.96	0.64
Turkey	0.37	0.28	0.75	0.55	0.68
Mexico	0.35	0.33	0.84	0.61	0.58
Brazil	0.20	0.19	0.78	0.48	0.42
India	0.10	0.080	0.68	0.34	0.31
Kenya	0.052	0.022	0.73	0.23	0.14
Maliawi	0.018	0.029	0.57	0.21	0.087

Source: Output per worker, Human Capital, and A are 2011 physical capital and human capital per worker. Data are not comparable to Section 7.2 as compared with the 90 countries for which constant data are available for 1975 and 2000.

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## Problems with measuring capital and implications

- Waste of investment
- Quality of investment
  
- There are estimate according to which the actual level of the capital stock is in between 60% to 75% of the official statistics...

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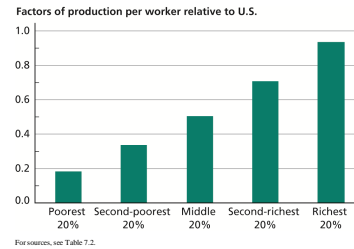
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**Figure 7.3** Role of Factors of Production in Determining Output per Worker, 2009



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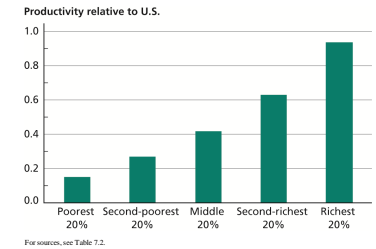
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**Figure 7.4** Role of Productivity in Determining Output per Worker, 2009



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### Growth accounting

Output = productivity \* factors of production

Output growth rate =  
Productivity growth rate + growth rate of factors of production

The growth rate of factors of production has to be weighted with respect to their share on output

Productivity growth rate =  
Output growth rate – growth rate of factors of production




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**Table 7.3** Data for Calculating Productivity Growth in Erewhon

	Output per Worker, $y$	Physical Capital per Worker, $k$	Human Capital per Worker, $h$
Erewhon in 1975	1	20	5
Erewhon in 2010	4	40	10
Annual Growth Rate	4%	2%	2%




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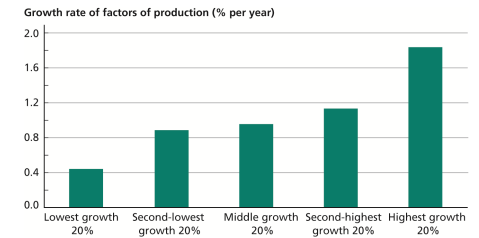
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**Figure 7.5** Role of Factors of Production in Determining Growth, 1975–2009



For sources, see Table 7.2.




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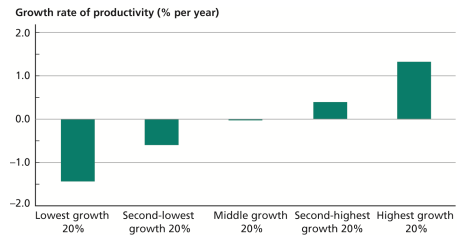
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**Figure 7.6** Role of Productivity in Determining Growth, 1975–2009



For sources, see Table 7.2.




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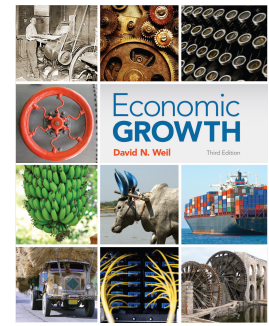
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Chapter 8

**THE ROLE OF TECHNOLOGY IN GROWTH**




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**Table 8.1** Researchers and Research Spending, 2009

And Italy?

Country	Number of Researchers	Researchers as a Percentage of the Labor Force	Research Spending (\$ billions)	Research Spending as a Percentage of GDP
United States	1,412,639	0.89%	398.2	2.8%
Japan	655,530	1.00%	137.9	3.4%
Germany	311,519	0.74%	82.7	2.8%
France	229,130	0.80%	48	2.2%
Korea	236,137	0.96%	43.9	3.3%
OECD Total	4,199,512	0.70%	965.6	2.4%

Source: OECD Main Science and Technology Indicators database.




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## The nature of technological progress

- Technology creation
- Technology transfer or diffusion
  - Non rivalry
  - Non excludability

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## Determinants of R&D spending

- Profit considerations
  - How much advantage with respect to followers
  - Size of the market
  - How long does the advantage last
  - Uncertainty

Concept of creative destruction

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## One country model

- Labour is the only factor
- Which can be used either in production or in the R&D
- $\gamma_A$  is the quota of labour used in R&D...
- Its function is similar to the saving rate in the Solow model

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## Process of productivity growth

- Growth of  $A = L_A/\mu$
- where  $\mu$  represents the price/cost of the new invention
- The growth rate of  $A$  represents the growth rate of  $y$

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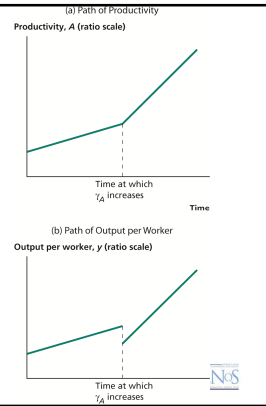
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## Figure 8.1 Effect of Shifting Labor into R&D



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## Two country model

- $\mu$  is now different among countries
- One country invests more in R&D and it is the leader the other one is the follower

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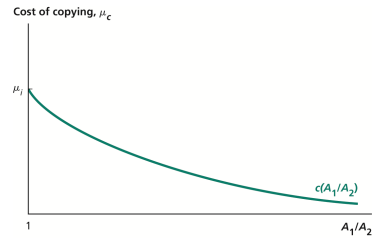
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**Figure 8.2** Cost of Copying for the Follower Country



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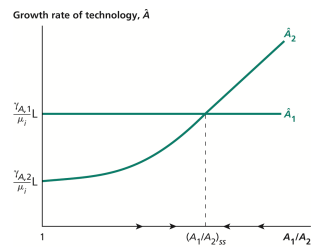
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**Figure 8.3** Steady State in the Two-Country Model



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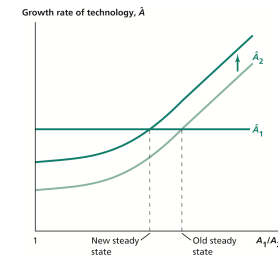
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**Figure 8.4** Effect of an Increase in R&D in the Follower Country on the Steady State



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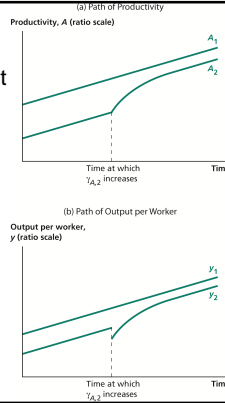
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**Figure 8.5** Effect of an Increase in  $\gamma_{A,2}$  on Productivity and Output



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## Barriers to international technology transfer

- Appropriate technology
- Tacit knowledge
- Patents and other tools to appropriate R&D returns

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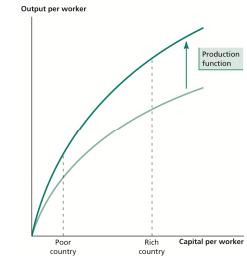
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**Figure 8.6** Neutral Technological Change



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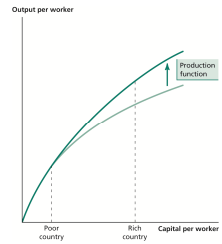
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**Figure 8.7** Capital-Biased Technological Change



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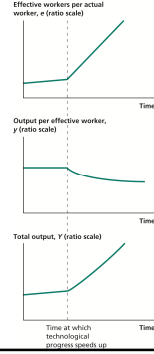
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**Figure 8.8** Effect of an Increase in Technological Progress

**Incorporating Technological Progress into the Solow Model**



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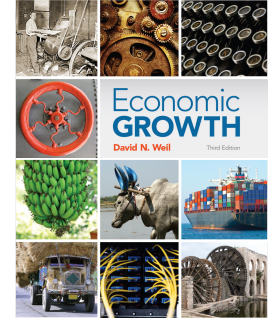
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## Chapter 9

# THE CUTTING EDGE OF TECHNOLOGY



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**Table 9.1** Growth Accounting for Europe, A.D. 500–1700

Period	Annual Growth Rate of come per Capita, $\gamma$	Annual Growth Rate of Population, $\lambda$	Annual Growth Rate of Productivity, $A$
500–1500	0.0%	0.1%	0.033%
1500–1700	0.1%	0.2%	0.166%

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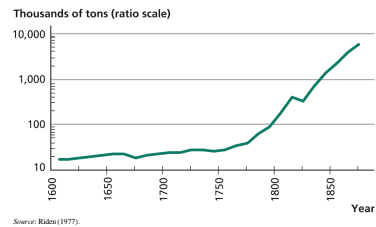
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**Figure 9.1** British Iron Production, 1600–1870




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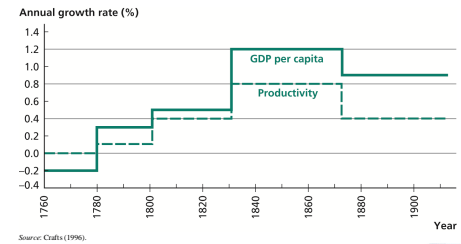
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**Figure 9.2** British Output and Productivity Growth, 1760–1913




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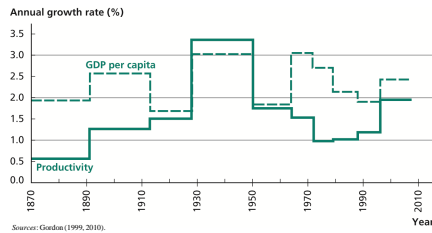
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**Figure 9.3 U.S. Output and Productivity Growth, 1870–2007**



Source: Gordon (1999, 2010).




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**Table 9.2 U.S. Patents and Patents per Million Residents, 2010**

Country	Patents	Patents per Million Residents
France	9,615	418.7
Spain	46,978	368.2
Israel	1,917	267.7
Finland	1,272	214.4
Switzerland	1,889	247.8
Sweden	1,196	174.7
South Korea	42,588	257.1
Germany	13,215	175.9
Canada	2,511	162.0
Hong Kong	719	101.0
Singapore	613	123.2
South Korea	42	82.4
Denmark	766	128.9
Netherlands	1,919	113.4
Italy	25	80.9
Japan	905	110.2
Australia	2,879	99.6
Belgium	869	86.0
France	5,038	77.8
Norway	418	64.8
United Kingdom	5,035	80.5
India	225	56.3
New Zealand	212	24.6
Italy	2,254	97.1

Source: U.S. Patent and Trademark Office, [http://www.uspto.gov/ip/offices/industry/industry\\_jobs.html](http://www.uspto.gov/ip/offices/industry/industry_jobs.html)




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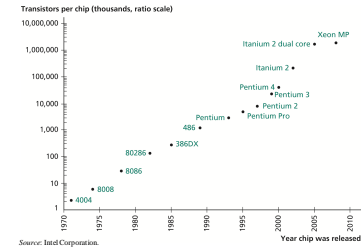
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**Figure 9.4 Moore's Law as Seen in Intel Microprocessors**



Source: Intel Corporation.




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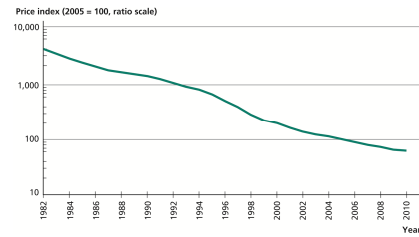
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**Figure 9.5** Price of Computers, 1982–2010



Source: U.S. Department of Commerce, National Income and Product Accounts, Table 1.5.4. Includes both computers and peripherals.



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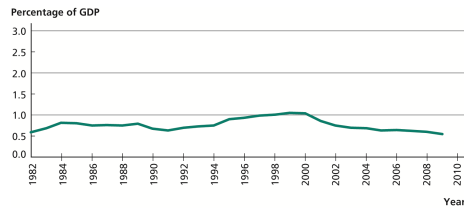
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**Figure 9.6** Investment in Computers as a Percentage of GDP, 1982–2009



Source: U.S. Department of Commerce, National Income and Product Accounts, Table 5.5.5. Includes both computers and peripherals.



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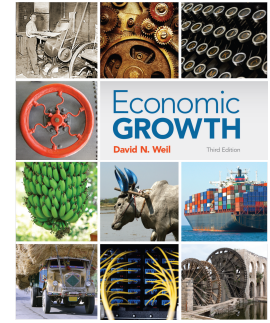
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## Chapter 10

# EFFICIENCY



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**Table 10.1** Decomposition of Productivity Gap Between India and the United States

Years India Lags United States in Technology (G)	Level of Technology in India Relative to United States (T)	Level of Efficiency in India Relative to United States (E)
10	0.95	0.33
20	0.90	0.35
30	0.85	0.36
40	0.81	0.38
50	0.76	0.41
75	0.67	0.46
100	0.58	0.53
125	0.51	0.61

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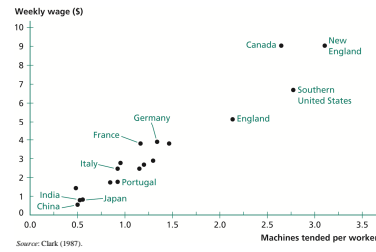
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**Figure 10.1** Wages and Machines in the Textile Industry, 1910



Source: Clark (1987).

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**Table 10.2** Productivity in Selected Industries in the Early 1990s

	United States	Japan	Germany
Automobiles	100	127	84
Steel	100	110	100
Food Processing	100	42	84
Telecommunications	100	51	42
Aggregate Productivity	100	67	89

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## Types of inefficiencies

- Unproductive activities
  - Rent seeking phenomena
- Idle resources
- Misallocation of factors among sectors
  - Barriers to mobility
  - Wages not equal to marginal product

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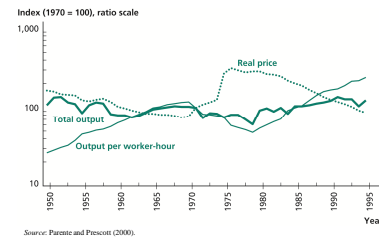
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**Figure 10.2** U.S. Subsurface Coal Mining:  
Output, Price, and Output per Worker-Hour,  
1949–1994



Source: Parrett and Prescott (2000).

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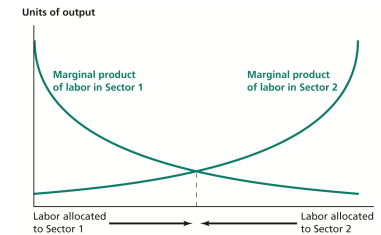
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**Figure 10.3** Efficient Allocation of Labor  
between Sectors



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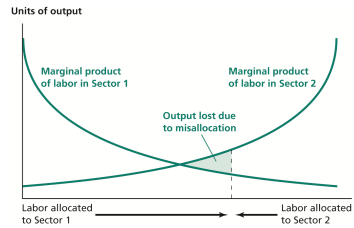
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**Figure 10.4** Overallocation of Labor to Sector 1



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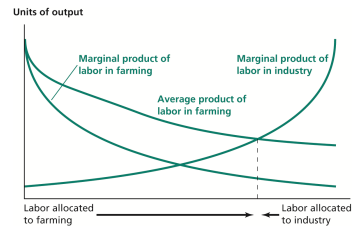
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**Figure 10.5** Overallocation of Labor to Farming When Farmworkers Are Paid Their Average Product



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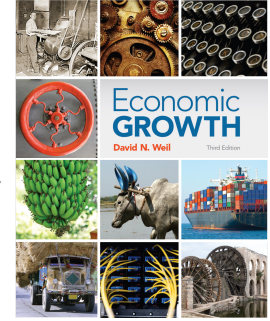
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## Chapter 11

# GROWTH IN THE OPEN ECONOMY



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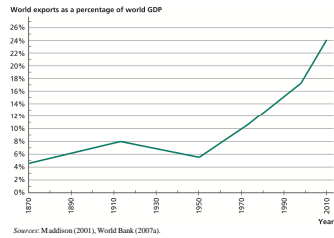
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**Figure 11.1** Growth of World Trade,  
1870–2010



Source: Maddison (2001), World Bank (2007a).



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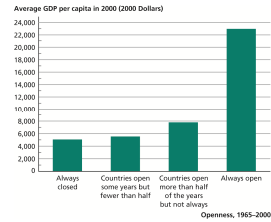
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**Figure 11.2** Relationship between Economic  
Openness and GDP per Capita



Source: Sachs and Warner (1995), Wacziarg and Welch (2008).



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**Figure 11.3** Growth in Closed Economies



Source: Sachs and Warner (1995), Wacziarg and Welch (2008), Heston et al. (2011).



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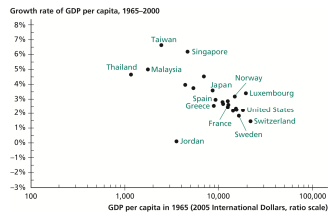
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**Figure 11.4** Growth in Open Economies




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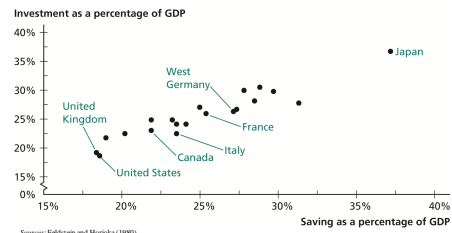
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**Figure 11.5** Saving and Investment Rates of Industrialized Countries, 1960-1974




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**Table 11.1** Prices in Japan before and after Opening to Trade

	Price Before Opening (U.S. cents per pound)	Price After Opening (U.S. cents per pound)
Tea	19.7	28.2
Sugar	22.7	11.2

Source: Huber (1971).

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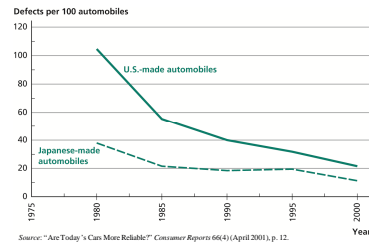
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**Figure 11.6** Quality of U.S.- and Japanese-made Automobiles



Source: "Are Today's Cars More Reliable?" *Consumer Reports* 66(4) (April 2001), p. 12.

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