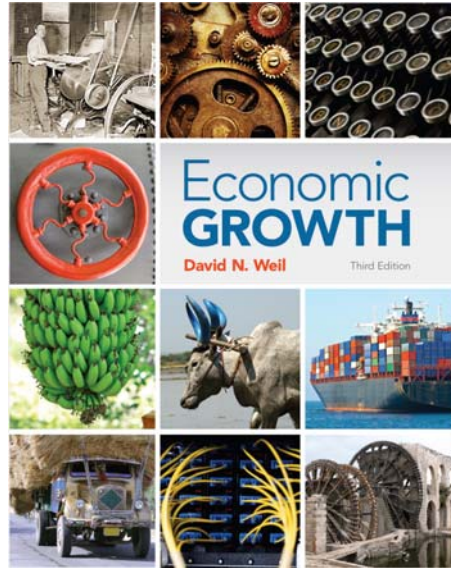


Chapter 4

POPULATION AND ECONOMIC GROWTH



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Groups for presentations

1. ...
2. ...
3. ...
4. ...
5. ...

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The European Semester

The European Semester provides a framework for the coordination of economic policies across the European Union. It allows EU countries to discuss their economic and budget plans and monitor progress at specific times throughout the year.

The framework

The European Semester: why and how
Macroeconomic imbalance procedure
Stability and Growth Pact

European Semester timeline

Setting the priorities
The analysis phase
National Reform Programmes and
Stability/Convergence Programmes
EU country-specific recommendations
Putting recommendations into practice

Thematic factsheets

Business environment
Financial stability
Green economy
Public administration
Labour markets and skills
Social protection and cohesion
Fiscal stability

The European Semester in your country

Austria

Themes for presentations

1. ...
2. ...
3. ...
4. ...
5. ...

Calendar

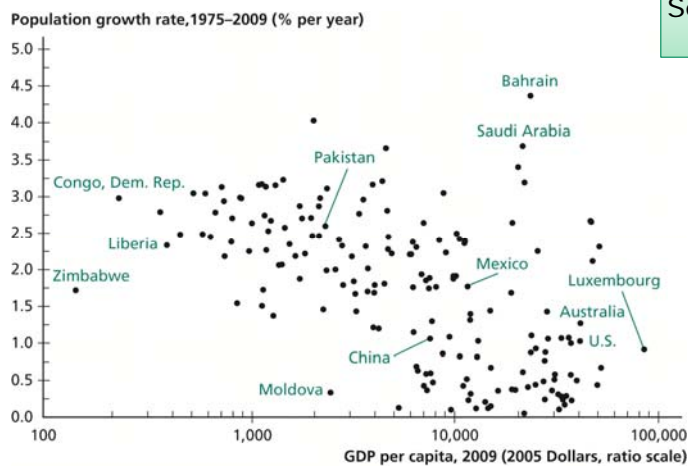
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Relationship Between Income per Capita and Population Growth



See Gapminder

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Population growth

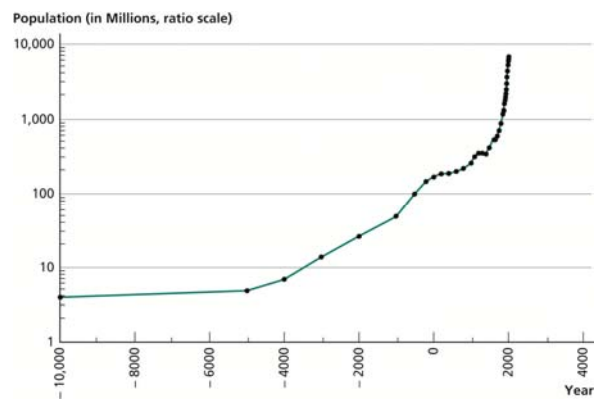
- High population growth → low income?
 -
- High income → low population growth?
 - ...
- Omitted variables that affect both income and population growth?

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World Population, from 10,000 B.C. to A.D. 2010



Source: Kremer (1993).

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World Population : 10,000 BC to 2010 AD

High population growth only in recent decades.

Growth rates over time:

- 10,000 BC-0: 0.04%
- 0-1800: 0.09%
- 1800-1900: 0.6%
- 1900-1950: 0.9%
- 1950-2000: 1.8%

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14th
Oct
2018

Current World Population

7,656,635,743

[view all people on 1 page >](#)

TODAY	THIS YEAR
Births today 269,524	Births this year 110,605,151
Deaths today 111,635	Deaths this year 45,811,803
Population Growth today 157,889	Population Growth this year 64,793,348

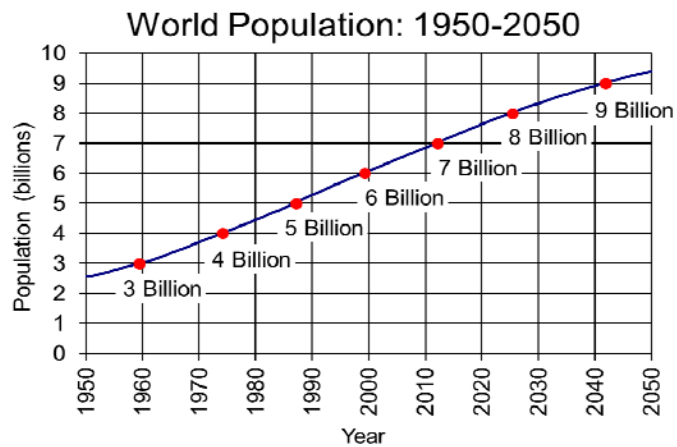
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World Population : 1950 to 2050

Increase from 3 billion in 1959 to 6 billion by 1999. Projections: From 6 in 1999 to 9 by 2042, a 50% increase that is expected to require 43 years.



Source: U.S. Census Bureau, International Data Base, July 2015 Update.

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Malthus' theory

Thomas Malthus (1766-1834):

Essay on the Principle of Population (1798).

The first economist to propose a systematic theory of population.

Central idea: Population growth is determined by the economic environment.

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Malthus' theory

- Assumptions:
 1. Large population → Low income per capita.
 - Because of finite quantity of resources (land, food).
 2. Low income per capita → low fertility /high mortality
 - population size ↓
 - Feedback loop from 2. to 1.
- Population limited by
 - famine and disease → Malthusian catastrophe (positive check)
 - deliberate reduction in fertility to prevent poverty (preventive check).
 - No role for improvement in living standards.

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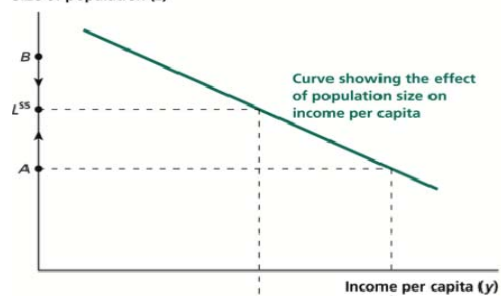
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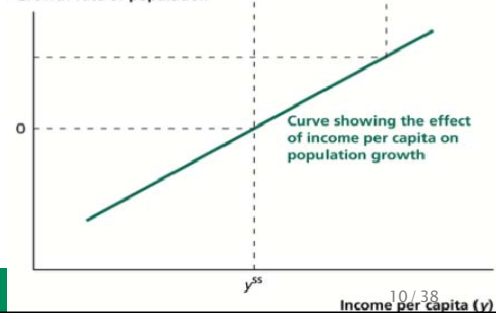
Malthus' theory

$y > y^{ss} \rightarrow$ population growth $\rightarrow y \downarrow$.
 $y < y^{ss} \rightarrow$ population falls $\rightarrow y \uparrow$.

(a) Relationship Between Income per Capita and Population Size
 Size of population (L)



(b) Relationship Between Income per Capita and Population Growth
 Growth rate of population



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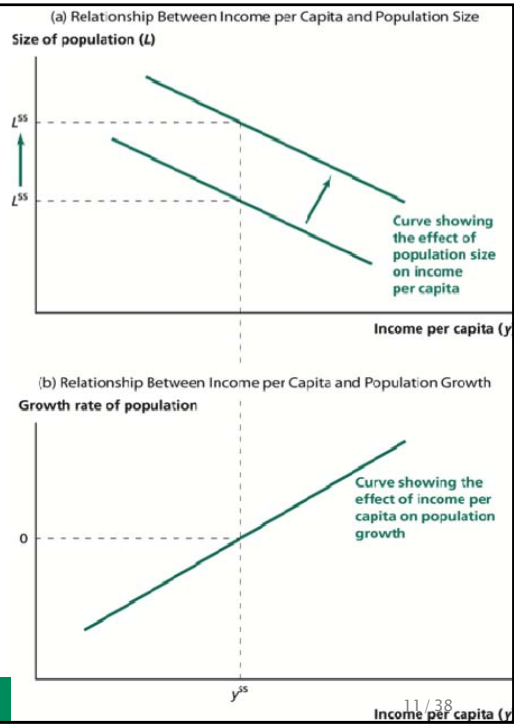
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 Income per capita (y)

Productivity improvement

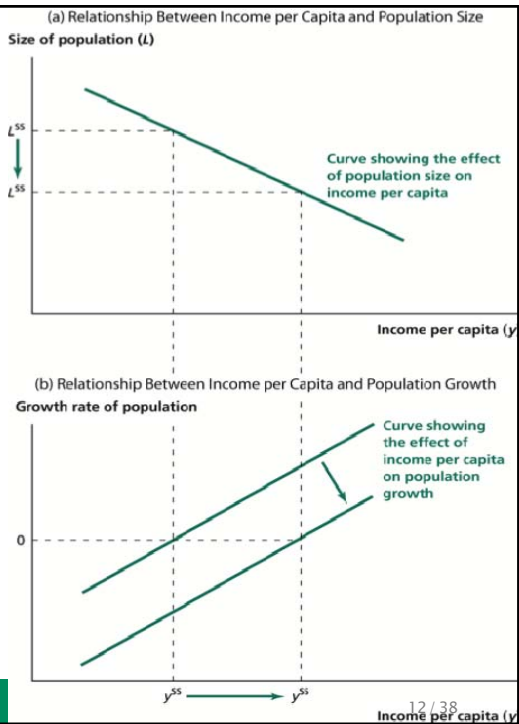
More resources \rightarrow higher $y \rightarrow$
 Population growth $\rightarrow y \downarrow$.
 Hence no improvement in living standards, only population growth.

Consistent with the data until early 1800s.



Moral restraint

Only lower fertility will increase GDP/capita.



Last two centuries

Predictions from theory:

GDP/capita constant in the long run.

More food, land etc available (productivity growth) → population growth.

Data:

Enormous productivity improvements, followed by

- Low population growth in rich countries
- Increase in living standards.

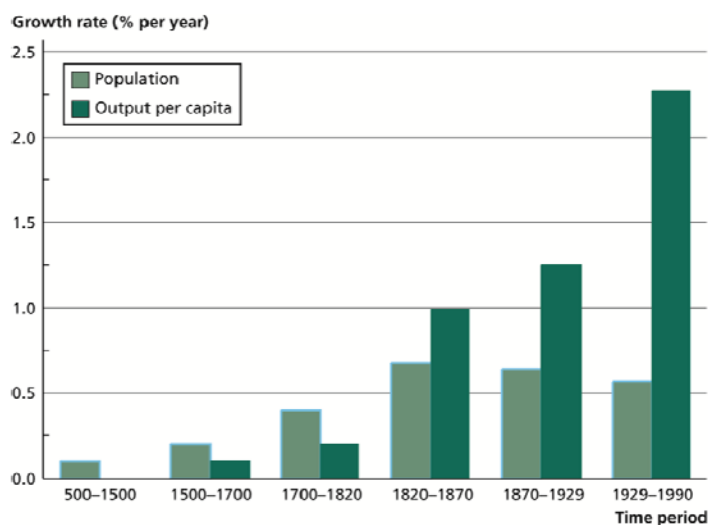
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Breakdown of the Malthusian model

Malthus predicts high population growth when output ↑.
No longer valid today, population growth negative in many rich countries.



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What's wrong with Malthus' model?

Resources (capital, land, crops etc) are fixed.

- ◆ Resource limitations such as land less important today.
- ◆ Human capital and ideas can be shared irrespective of population size.

Assumptions about population growth.

Does population size not matter for living standards anymore?

Fixed factors still exist:

- ◆ Food.
- ◆ Environment (e.g., global warming).
- ◆ More?

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The Solow model revisited

- Let's introduce population growth n in the Solow model.
- Is high n bad for growth (per capita)?
- Yes.
 - Intuition: High n means that the capital/worker ratio \downarrow .
 - This dampens the steady state growth rate.

Define

$$\frac{\partial L}{\partial t} = \dot{L} \quad n = \frac{\dot{L}}{L}$$

Change in the capital stock: $\dot{K} = \gamma Y - \delta K$.

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Change in capital stock

Let's rewrite \dot{K} in intensive form:

$$\begin{aligned}\dot{k} &= \frac{\partial(K/L)}{\partial t} = \frac{\dot{K}L - K\dot{L}}{L^2} \\ &= \frac{\dot{K}}{L} - \frac{K\dot{L}}{L^2} \\ &= \frac{\gamma Y - \delta K}{L} - kn \\ &= \gamma f(k) - (\delta + n)k.\end{aligned}$$

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Steady state

Steady state defined by $\dot{k} = 0$:

$$\gamma f(k) - (\delta + n)k = 0$$

$$\gamma f(k) = (\delta + n)k.$$

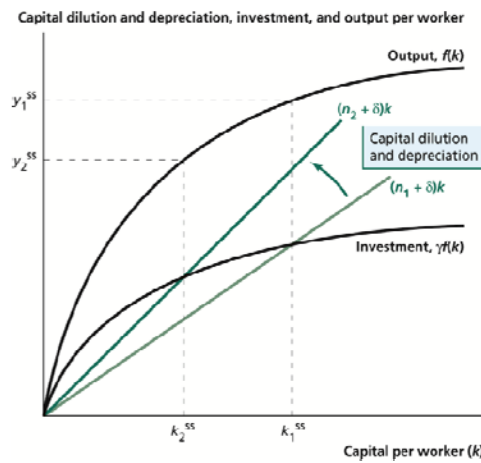
Investment per worker (LHS) = depreciation + dilution of capital per worker (RHS).

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Steady state



Higher $n \rightarrow$ Steeper slope of $(n + \delta)k \rightarrow$ SS $k \downarrow$ and $y \downarrow$.
 Intuition: Less capital/worker \rightarrow lower productivity.
 Growth in y or Y ? In Y but not y .

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The Cobb Douglas case

Let $f(k) = Ak^\alpha$. Then the SS equation becomes

$$\gamma Ak^\alpha = (n + \delta)k$$

$$k^{\alpha-1} = \frac{n + \delta}{\gamma A}$$

$$k^{SS} = \left(\frac{\gamma A}{n + \delta} \right)^{1/(1-\alpha)}$$

Insert k^{SS} into the production function:

$$y^{SS} = Ak^\alpha = A^{1/(1-\alpha)} \left(\frac{\gamma}{n + \delta} \right)^{\alpha/(1-\alpha)}$$

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The Cobb Douglas case

Assume two countries i and j , with same A 's and γ 's but $n_i > n_j$. Then

$$\frac{y_i^{ss}}{y_j^{ss}} = \left(\frac{n_i + \delta}{n_j + \delta} \right)^{\alpha/(1-\alpha)} < 1.$$

E.g. if $\alpha = 1/3$, $\delta = 0.05$, $n_i = 0.04$ and $n_j = 0$. Then

$$\frac{y_i^{ss}}{y_j^{ss}} = 0.75.$$

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Malthus vs Solow

Both models can explain negative correlation between population growth & income. But mechanism differs:

Population vs land (Malthus) vs Population vs capital (Solow) Endogenous population (Malthus) vs exogenous population (Solow).

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Explaining population growth

Models suggest that population growth matters for living standards. But what determines population growth?

Level of development.

◆ **The demographic transition:** Development/growth leads to a transformation of demographic characteristics.

In particular:

- ◆ Mortality transition.
- ◆ Fertility transition.

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Life Expectancy

Define life expectancy at time of birth

$$\sum_{i=0}^T \pi(i),$$

where $\pi(i)$ is the probability that a person will be alive at age i . Small/no change in life expectancy before the 1700s.

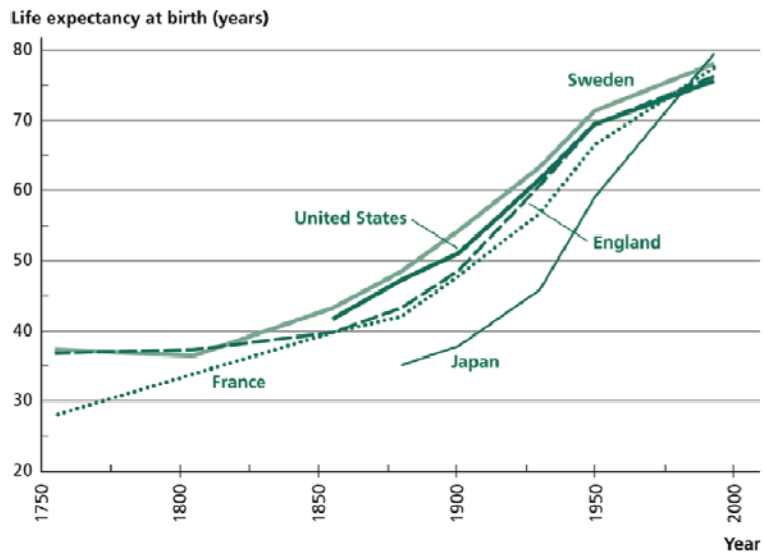
Dramatic increase the last 200 years.

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Life Expectancy

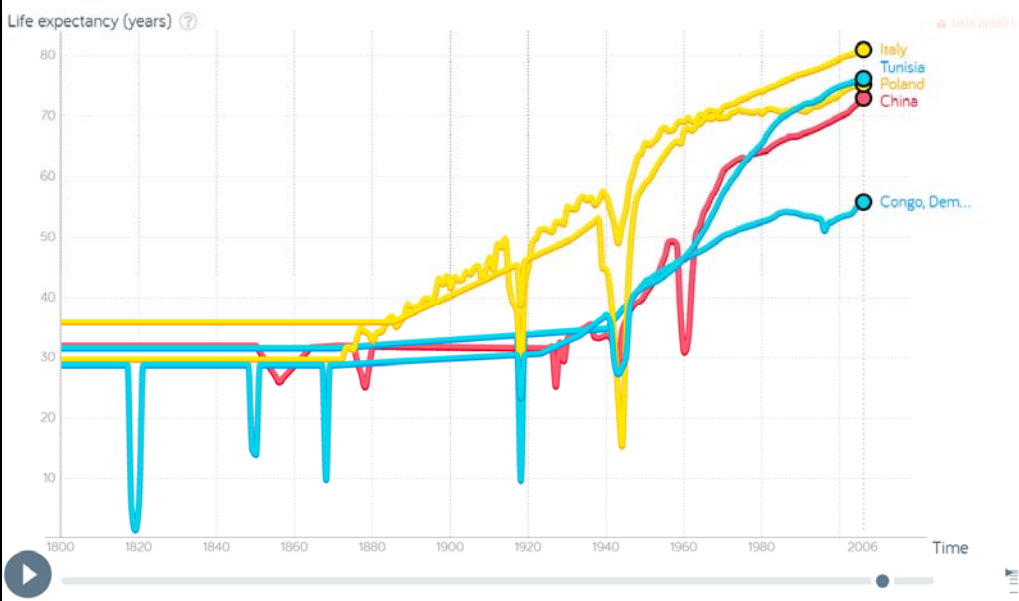


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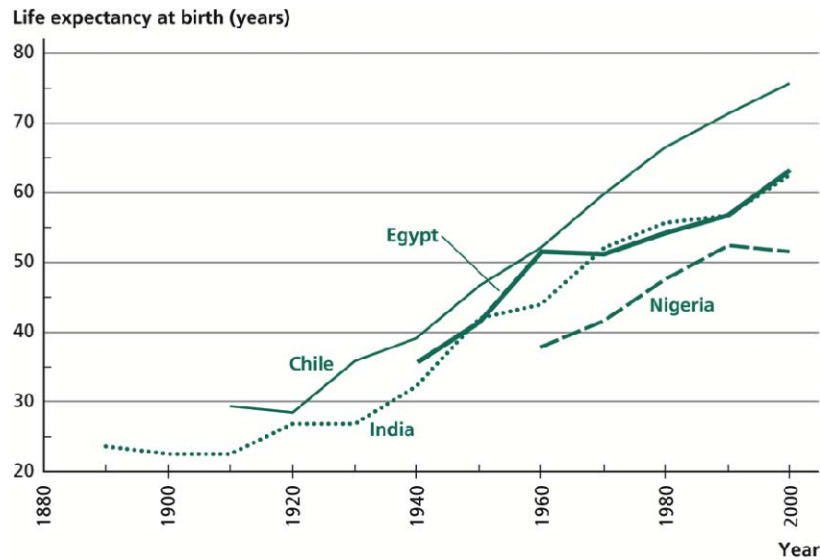
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Life Expectancy : Italy & c



Mortality : Developing countries



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Explaining mortality transition

- Better living conditions (nutrition, housing).
- Public health (water and sewage).
- Medical treatments.

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Explaining mortality transition

Better living conditions (nutrition, housing).

Public health (water and sewage).

Medical treatments.

Infant mortality.

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Fertility

Define total fertility rate (TFR) as expected number of children that a woman would have if she lived through all of her childbearing years:

$$TFR = \sum_{i=0}^T F(i)$$

where $F(i)$ is the age-specific fertility rate (average no of children for woman of age i).

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US Fertility, 1860-2008

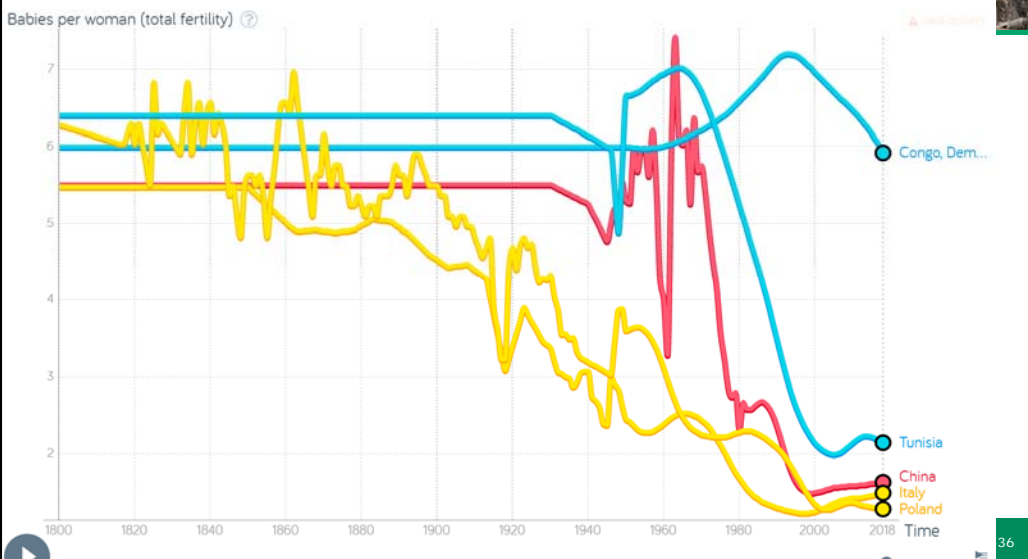


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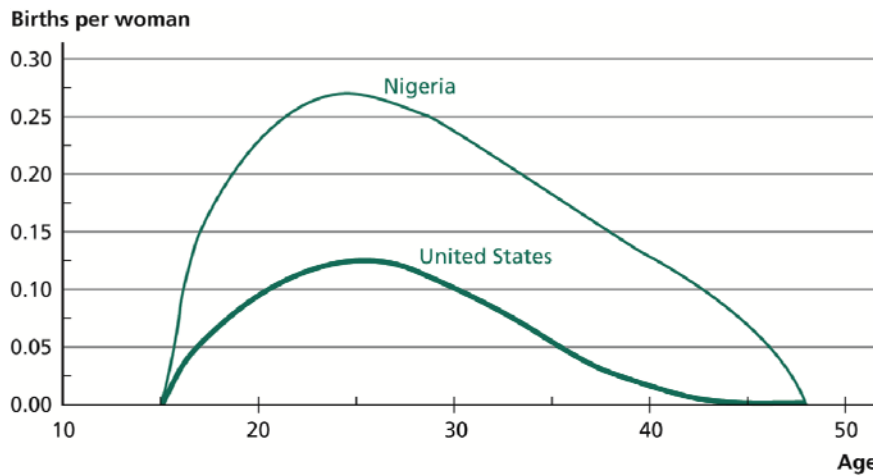
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Some countries' fertility, 1860-2008



Age-specific fertility, 1999



TFR = area under the curve, 2.1 for U.S., 6.0 for Nigeria.

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Explaining fertility transition

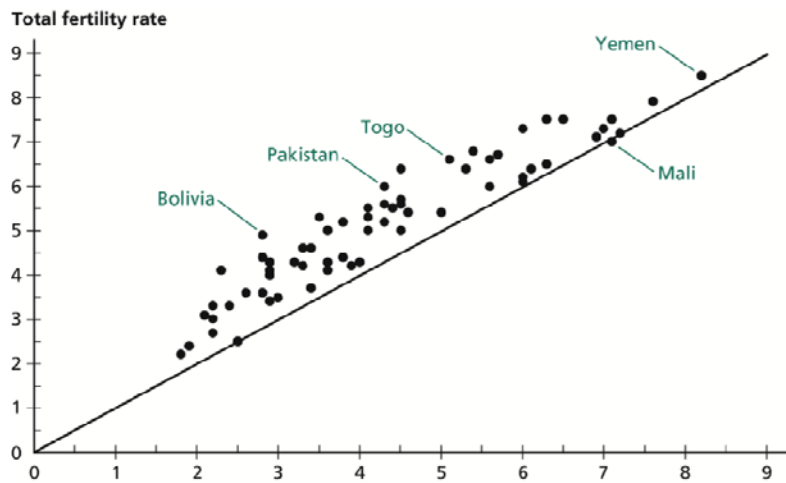
- Improved technology (contraception).
 - Contraceptive pill (1960-)
 - Quality condoms (1840s-).
- Family planning attitudes & programs.
 - One-child policies.

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Desired and actual fertility, 70s and 80s



Contraception explain 10-40% of decline in fertility (Keyfitz, 1989). Attitudes more important.

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Explaining fertility transition

Development. U.N. (1974): "Development is the best contraceptive".

Mortality reduction → lower fertility bc # *surviving* children matters. Income and substitution effects.

- Income effect: Get more children.
- Substitution effect: Get less children because the *opportunity cost* is higher.
- Opportunity cost even higher if women become more educated and earn more.

Resource flows between parents and children.

- Decline of child labor
- Social Security.
- Quality-quantity trade-offs.
- More investment in quality of child vs quantity.
- Because of higher life expectancy?

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Fertility-mortality interaction

Define net rate of reproduction (NRR) as the number of daughters that each girl who is born can be expected to give birth to.

Assuming fertility and mortality rate of current population:

$$NRR = \beta \sum_{i=0}^T \pi(i) F(i)$$

where β is the share of female newborns.

Zero population growth if $NRR = 1$.

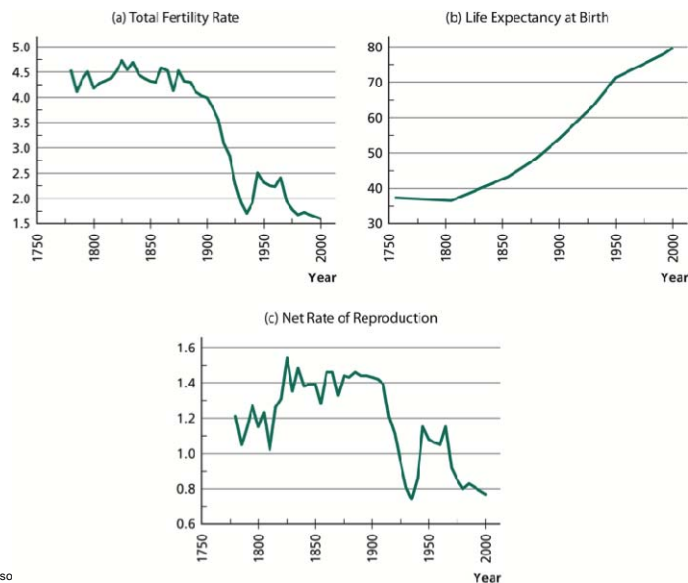
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Example: Sweden

Demographic transition complete: Both fertility and mortality down, currently $NRR < 1$.



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Example: Nigeria

Period	Total Fertility Rate	Life Expectancy at Birth	Net Rate of Reproduction
1955–1960	6.90	38.2	1.97
1965–1970	6.90	42.0	2.12
1975–1980	6.90	46.1	2.28
1985–1990	6.70	50.2	2.38
1995–2000	5.92	52.5	2.20
2000–2005	5.61	50.3	2.00

Source: United Nations Population Division (2010).

End of demographic transition?

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Example: India

Period	Total Fertility Rate	Life Expectancy at Birth	Net Rate of Reproduction
1955–1960	5.92	42.8	1.75
1965–1970	5.66	48.0	1.87
1975–1980	4.83	52.9	1.73
1985–1990	4.15	57.4	1.81
1995–2000	3.45	62.1	1.43
2000–2005	2.73	64.2	1.17

Source: United Nations Population Division (2010).

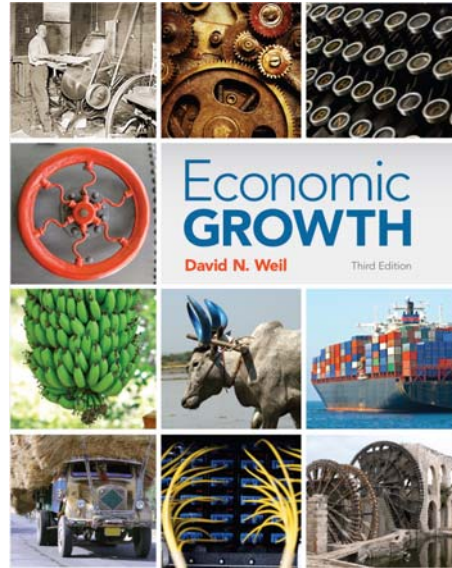
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Chapter 6

HUMAN CAPITAL



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Human capital and income

So far: Workers assumed to be identical over time and across countries.

How can differences in **human capital** explain cross-country income differences?

Human capital: Factors that influence the productivity of the worker, e.g. education & health.

Production function with human capital:

$$Y = F(K, hL),$$

where h is effort/quality per worker.

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Human capital as an input

- We focus on qualities of people who are productive
- We concentrate on qualities which are produced, as with physical capital also human capital is itself produced, contrary to natural resources
- Human capital earns returns, e.g. investment in education increases the wage.
- Cannot be rented, as opposed to physical capital, that is workers have to work to get it whilst capital owners can relax on a beach)
- Human capital depreciates
- Human capital can have two forms: health and education

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Human capital: Health

We'll focus on two determinants of human capital: Health & education.

Better health:

Improves productivity - increase output by working more or improving quality.

Brings more people into the workforce.

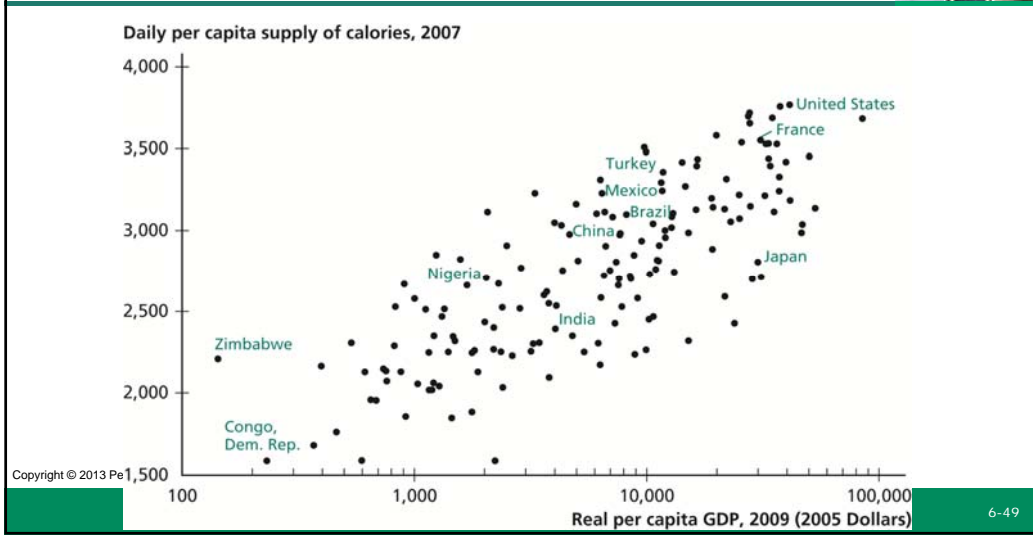
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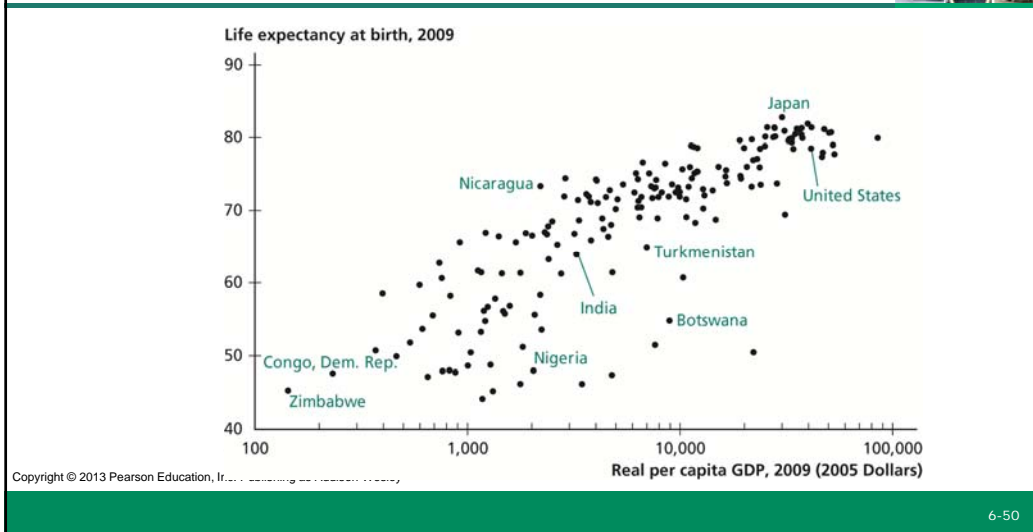
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Human capital as a form of health

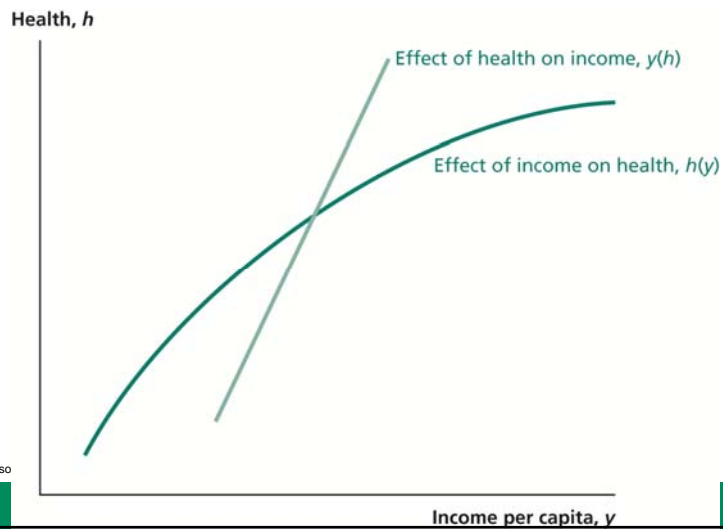
Nutrition versus GDP per Capita



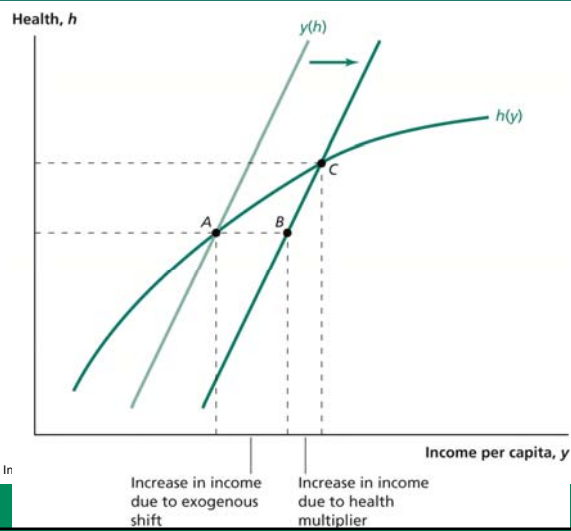
Life Expectancy versus GDP per Capita



How Health Interacts with Income



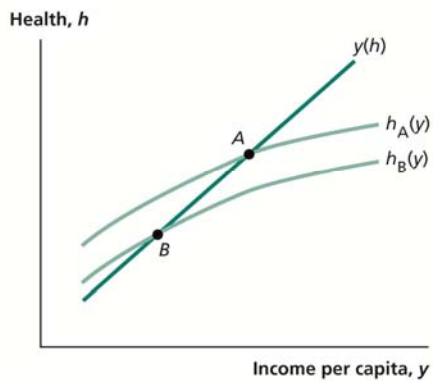
Effect of an Exogenous Shift in Income



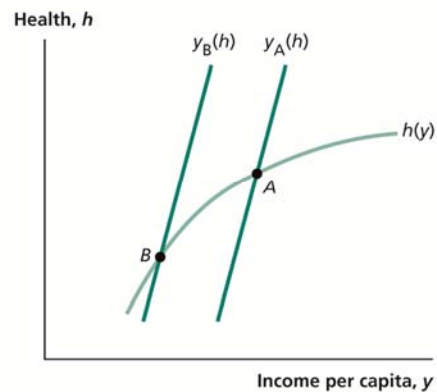
Health and Income per Capita: Two Views



(a) The Health View



(b) The Income View



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HC : Education



Education & skills also human capital.

- Boost productivity & wages
- Intrinsic value, higher utility.

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Human capital in the form of education

Changes in the Level of Education, 1975-2010



		Percentage of the Adult Population with				
		Average Years of Schooling	No Schooling	Complete Primary Education	Complete Secondary Education	Complete Higher Education
Developing Countries	1975	3.2	47.4	32.9	8.1	1.6
	2010	6.7	20.8	68.8	31.5	5.3
Advanced Countries	1975	8.0	6.2	78.8	34.9	8.0
	2010	11.0	2.5	94.0	63.9	16.6
United States	1975	11.4	1.3	94.1	71.1	16.1
	2010	12.4	0.4	98.8	85.4	20.0

Source: Barro and Lee (2010). Data for population 25+.

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Education as an investment

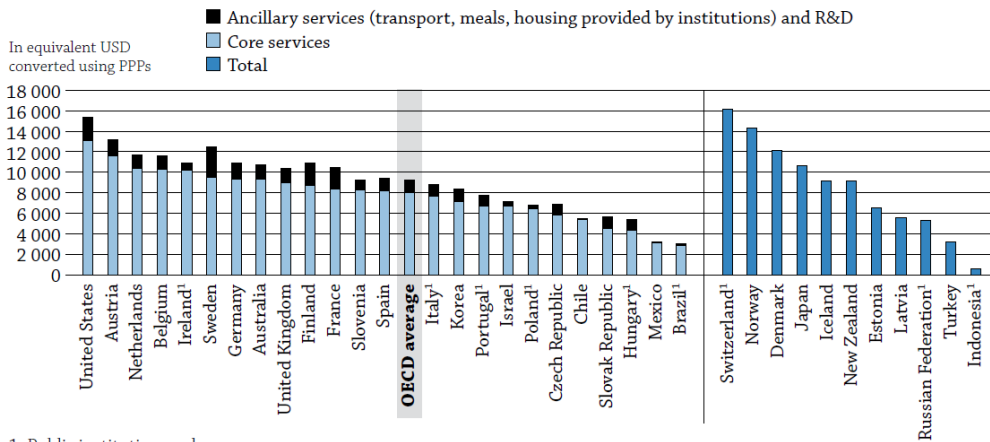


- It is costly (6% of GDP in US, 4.5% in Italy)
- Not only in terms of money but especially in terms of opportunity costs (this is true mostly for developing countries)
- The return to education is wage...a wage premium

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Chart B1.1. Annual expenditure per student by educational institutions, by type of service (2011)
In equivalent USD converted using PPPs, based on full-time equivalents, for primary through tertiary education

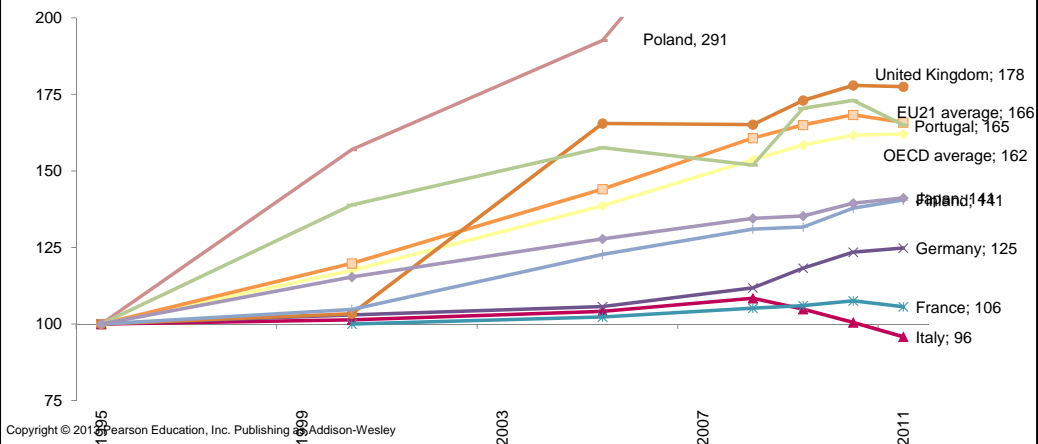


1. Public institutions only.

Countries are ranked in descending order of expenditure per student by educational institutions for core services.

Change in per student expenditure total, constant prices(1995 = 100)

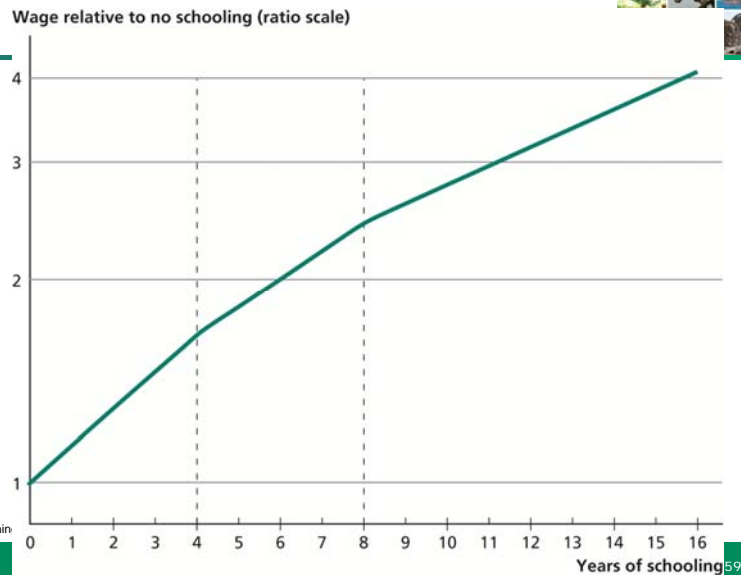
Indice di variazione (1995 = 100)



Effect of Education on Wages



Hall and Jones (1999). 13.4% per year for years 1-4, 10.1% for next 4 years, 6.8% for 8+ year.



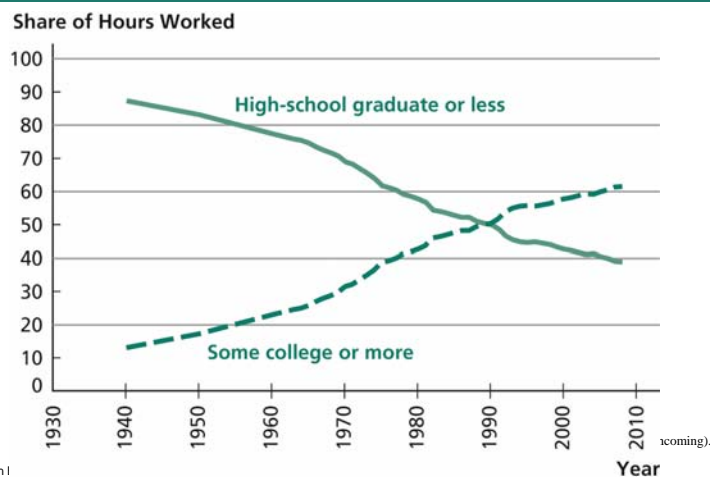
Decomposing wages



We know that capital's share of income is around $1/3$ (the α).

For the remaining $2/3$, how much is due to human capital and how much is "raw labor".

Share of Hours Worked by Education Level, 1940–2008



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Share of HC in wages



Percentage of the Population

Highest Level of Education	Years of schooling	Wage Relative to No Schooling	Developing Countries	Advanced Countries
No Schooling	0	1.00	20.6	2.5
Incomplete Primary	4	1.65	10.4	3.4
Complete Primary	8	2.43	18.0	12.3
Incomplete Secondary	10	2.77	18.3	17.8
Complete Secondary	12	3.19	23.2	37.4
Incomplete Higher	14	3.61	2.9	8.9
Complete Higher	16	4.11	5.3	18.6

Source: Barro and Lee (2010).

Raw labor is 1/4 of wages.

For the economy as a whole, the HC share is larger in advanced countries.

- ◆ Higher wages for more education.
- ◆ Larger share of population with more education.

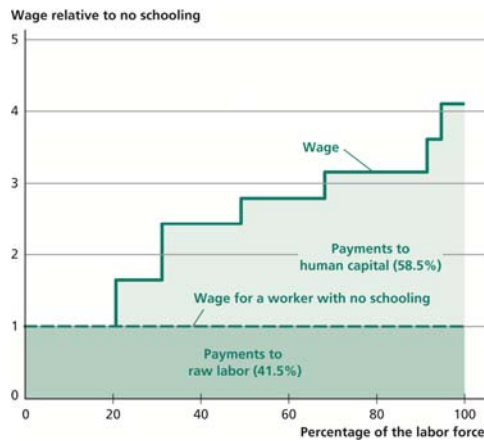
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Share of Human Capital in Wages in Developing Countries



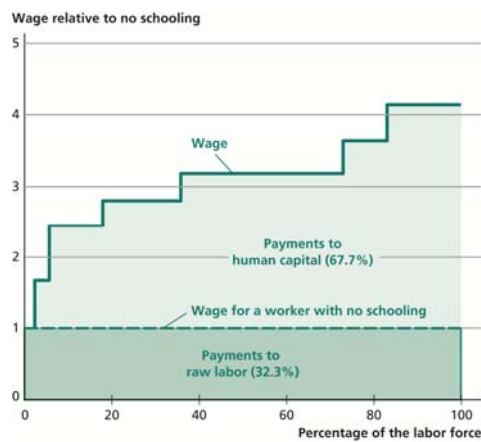
Remember alpha in the Solow model



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Share of Human Capital in Wages in Advanced Countries



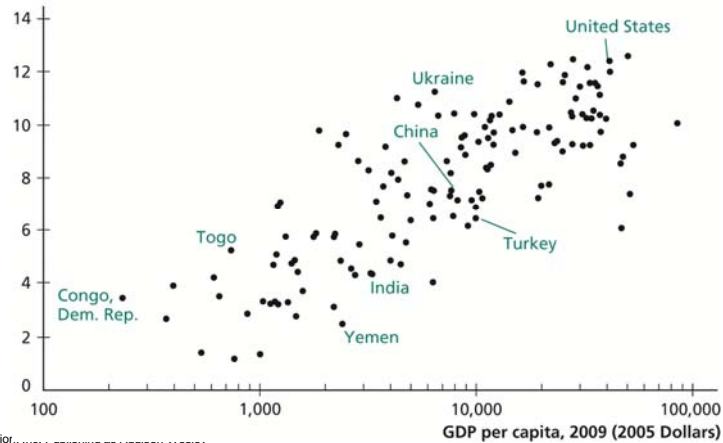
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Education and Income



Average years of schooling, 2010



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Table A7.3a. **Private costs and benefits for a man attaining tertiary education (2010)**

As compared with a man attaining upper secondary or post-secondary non-tertiary education, in equivalent USD converted using PPPs for GDP

	Year	Direct costs	Foregone earnings	Total costs	Gross earnings benefits	Income tax effect	Social contribution effect	Transfers effect	Unemployment effect	Grants effect	Total benefits	Net present value	Internal rate of return	
		(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
OECD	Netherlands	2010	-14 646	-95 834	-110 480	442 661	-197 999	-26 901	0	10 736	13 770	242 267	131 787	7.2%
	New Zealand	2010	-9 384	-43 347	-52 731	193 910	-62 325	-3 875	-86	358	3 039	131 021	78 290	7.3%
	Norway	2010	-1 086	-47 946	-49 032	274 357	-107 528	-23 197	0	23 000	4 690	171 321	122 289	8.2%
	Poland	2010	-7 343	-16 928	-24 270	376 155	-30 873	-75 986	0	38 492	2 228	310 015	285 745	24.6%
	Portugal	2010	-4 627	-16 181	-20 808	324 887	-89 461	-36 243	0	17 564	m	216 746	195 937	18.3%
	Slovak Republic	2010	-6 183	-15 019	-21 202	290 121	-51 866	-40 961	0	38 465	1 226	236 985	215 783	21.4%
	Slovenia	2010	-3 564	-26 242	-29 806	447 946	-110 866	-96 037	0	19 992	259	261 294	231 488	17.1%
	Spain	2010	-8 864	-28 219	-37 083	178 900	-52 903	-14 033	0	41 874	3 791	157 629	120 546	11.2%
	Sweden	2010	-3 560	-50 291	-53 851	209 467	-84 430	-9 281	0	8 454	7 735	131 945	78 094	7.4%
	Switzerland		m	m	m	m	m	m	m	m	m	m	m	m
	Turkey	2005	-1 061	-9 402	-10 463	106 985	-18 682	-16 424	0	2 761	m	74 640	64 177	19.3%
	United Kingdom	2010	-20 162	-47 655	-67 817	413 163	-89 124	-49 107	-4 303	40 284	5 225	316 138	248 322	14.3%
	United States	2010	-61 135	-44 678	-105 813	628 922	-210 898	-55 768	0	100 046	27 162	489 463	383 649	15.4%
	OECD average		-10 563	-40 755	-51 318	347 075	-105 528	-38 085	-777	29 016	6 181	236 602	185 284	13.9%
EU21 average		-6 258	-41 078	-47 335	361 801	-112 936	-45 075	-1 123	31 620	6 135	239 503	192 167	15.1%	
Italy	2008	-7 285	-50 608	-57 893	408 011	-159 562	-41 835	0	3 295	3 330	213 239	155 346	8.1%	
Japan	2007	-37 215	-66 750	-103 965	326 614	-64 523	-36 039	0	20 931	m	246 983	143 018	7.4%	
Korea	2010	-19 211	-34 019	-53 231	379 884	-47 160	-25 602	0	12 407	m	319 528	266 298	12.8%	

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Quantitative analysis of the impact of education differences



- In the simple Solow model: $Y=F(K,L) = AK^\alpha L^{1-\alpha}$

$$y_{ss} = A k_{ss}^\alpha = A^{1/(1-\alpha)} (\gamma/\delta)^{\alpha/(1-\alpha)}$$

let us add human capital and population dynamics...

- $Y=F(K,L,H) = h^{1-\alpha}AK^\alpha L^{1-\alpha}$, where h is effort/quality per worker.
- $y_{ss} = (h^{1-\alpha}A)^{1/(1-\alpha)} (\gamma/n+\delta)^{\alpha/(1-\alpha)}$
- $y_{ss} = h [A^{1/(1-\alpha)} (\gamma/n+\delta)^{\alpha/(1-\alpha)}]$

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Quantitative analysis of the impact of education differences



- In the simple Solow model

$$y_{ss}^i / y_{ss}^j = (\gamma^i/\gamma^j)^{\alpha/(1-\alpha)}$$

- Now with h and n

$$\begin{aligned} y_{ss}^i / y_{ss}^j &= \\ &= h^i [A^{1/(1-\alpha)} (\gamma/n+\delta)^{\alpha/(1-\alpha)}] / h^j [A^{1/(1-\alpha)} (\gamma/n+\delta)^{\alpha/(1-\alpha)}] \\ &= h^i / h^j \end{aligned}$$

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Predictions



Two countries i and j , with h_i and h_j , all else equal.

Then

$$\frac{y_i^{SS}}{y_j^{SS}} = \frac{h_i}{h_j}$$

Income per capita proportional to HC.

E.g. twice as high h in i yields twice as high y .

A numeric example



- 12 years of schooling in i and 2 in j .
- What is human capital h in the two countries?
Recall wage increase per year of additional schooling (13.4% for grades 1-4, etc).
Assume human capital h proportional to wages.

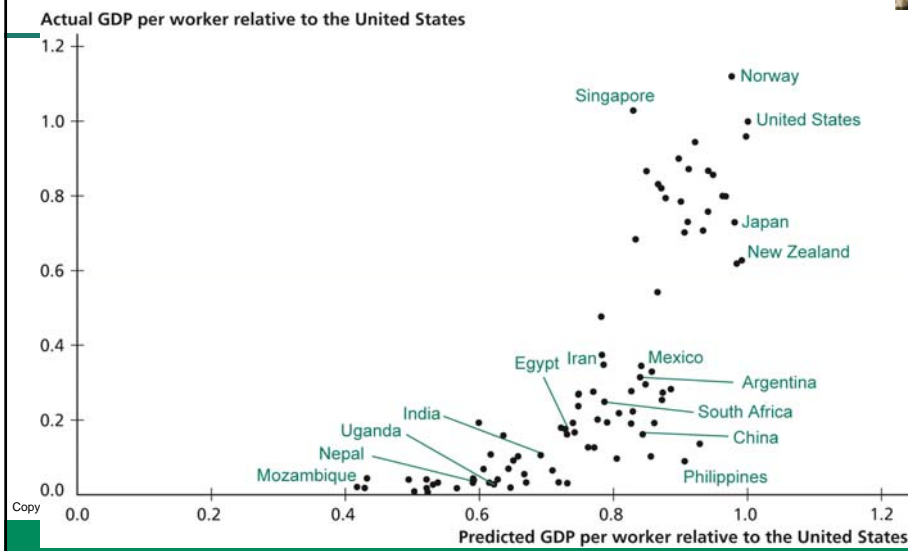
• Then
$$h_i = 1.134^4 \times 1.101^4 \times 1.068^4 \times h_0 = 3.16 \times h_0$$

$$h_j = 1.134^2 \times h_0 = 1.29 \times h_0$$

- And

$$\frac{y_i^{SS}}{y_j^{SS}} = \frac{3.16h_0}{1.29h_0} = 2.47.$$

Predicted versus Actual GDP per Worker



Important factors to explain why predictions are so wrong...

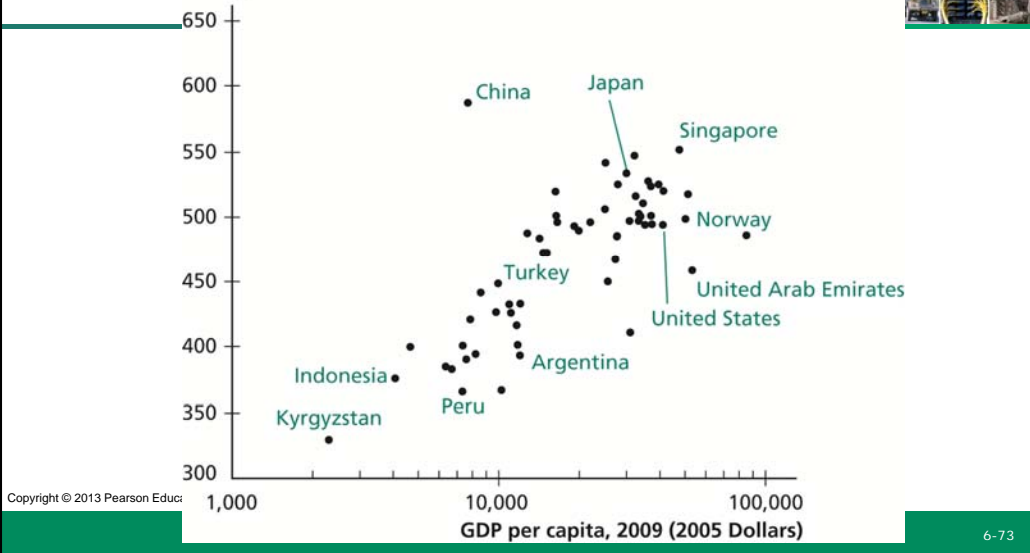


- Quality of schooling
- Externalities

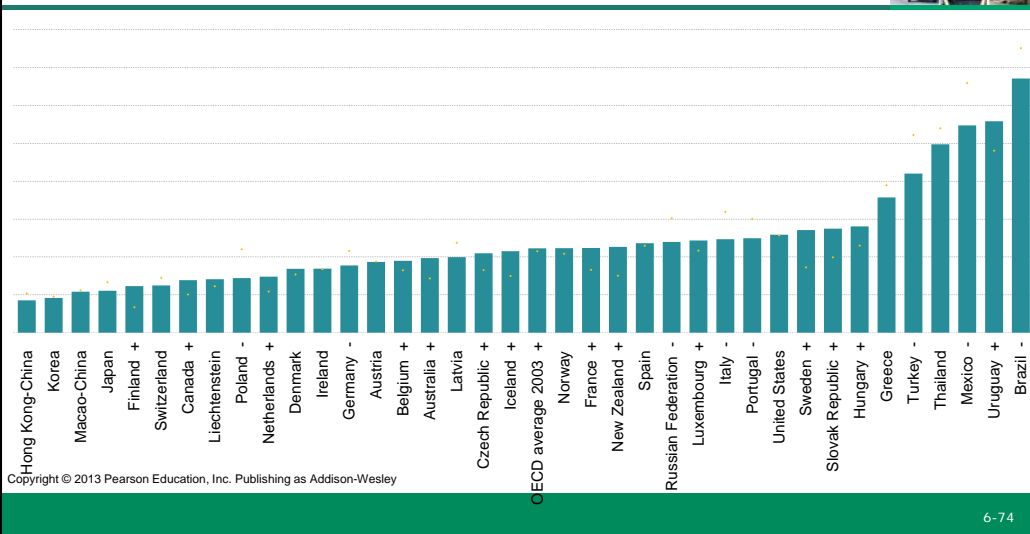
Student Test Scores versus GDP per Capita



Average student test scores, 2009



Percentage of low performers in Maths, PISA 2003-2012



Externalities



Externalities: An incidental effect of economic activity for which no compensation is provided.

The Solow model could not generate sufficient income inequality coming from human capital.

- ◆ One reason could be externalities.

Education: Additional schooling for individual x \rightarrow private return to x but also returns for y .

- ◆ E.g. x adopts new technologies that y also will use.

More on education



- [Education at a glance](#)
- [Alma laurea](#)