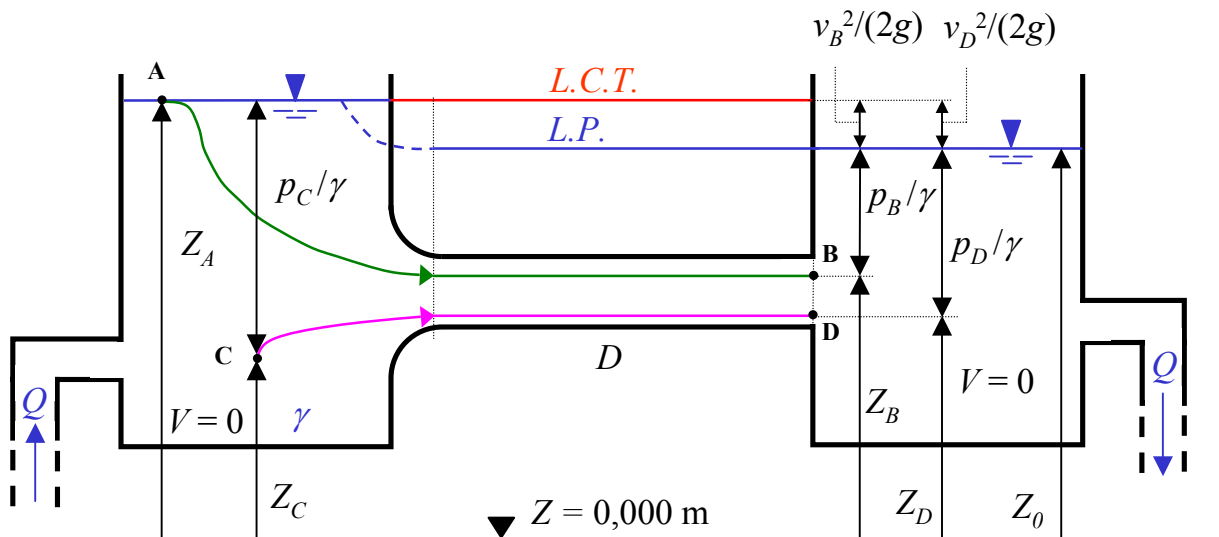
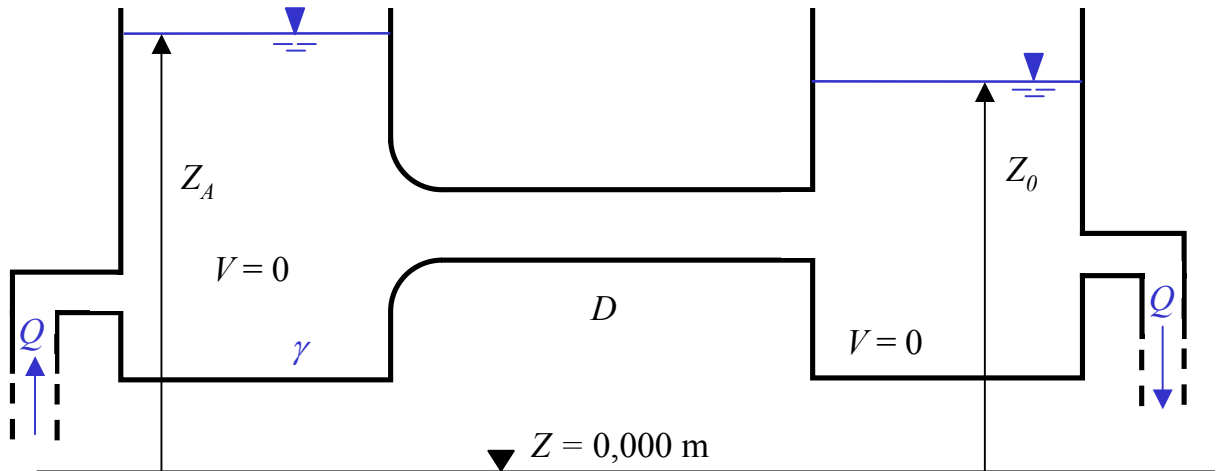


### Esercizio 33

Noti:  $Z_A = 18,000$  m,  $Z_0 = 16,000$  m,  $D = 0,300$  m,  $\gamma = 8825$  N/m<sup>3</sup>,  $g = 9,806$  m/s<sup>2</sup>, fluido ideale.

Determinare la portata circolante  $Q$ . Tracciare la linea dei carichi totali (L.C.T.) e la linea piezometrica (L.P.).

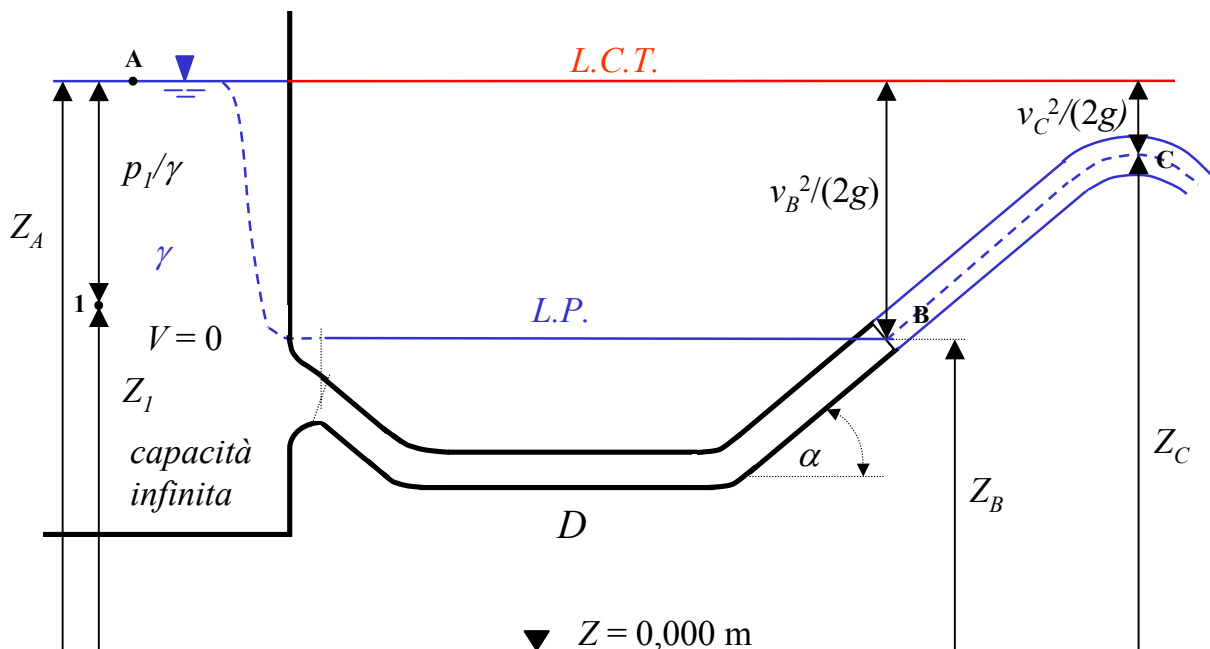
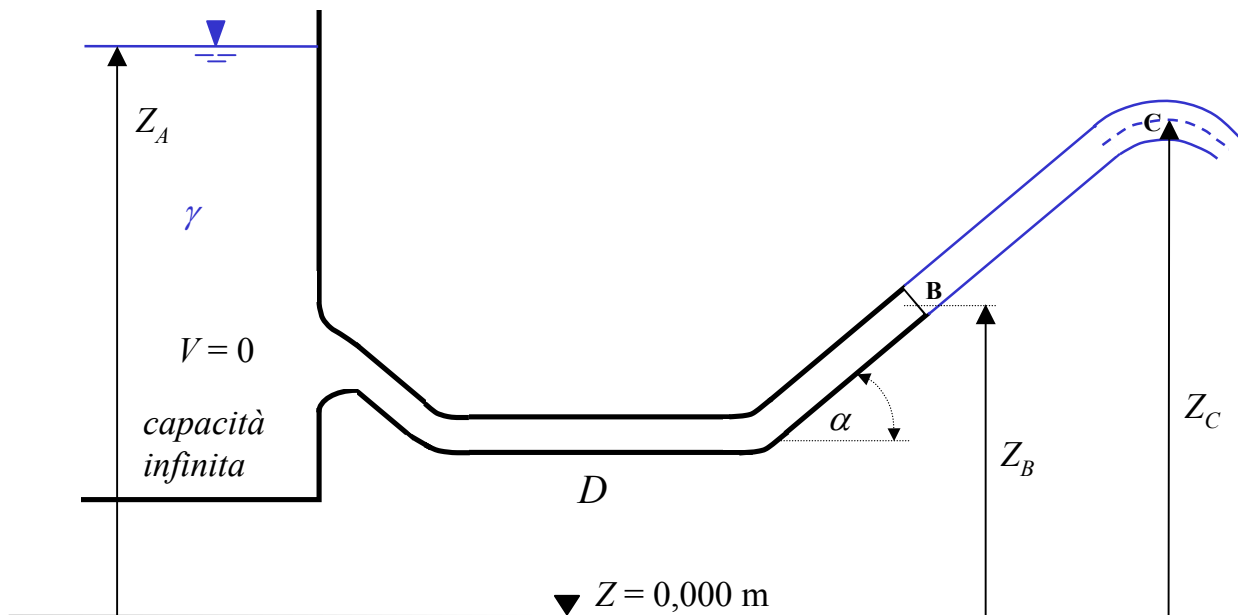


$$(Q = \pi D^2/4 [2 g (Z_A - Z_0)]^{1/2} = 0,443 \text{ m}^3/\text{s})$$

### Esercizio 34

**Noti:**  $Z_A = 50,000$  m,  $Z_B = 45,000$  m,  $D = 0,600$  m,  $\gamma = 7752$  N/m<sup>3</sup>,  $\alpha = 45^\circ$ ,  $g = 9,806$  m/s<sup>2</sup>, *fluido ideale*.

**Determinare** la portata  $Q$  transigente, la quota  $Z_C$  raggiungibile dal getto in atmosfera e la massima quota  $Z_C$  al variare dell'angolo  $\alpha$ . **Tracciare** la *linea dei carichi totali (L.C.T.)* e la *linea piezometrica (L.P.)*.

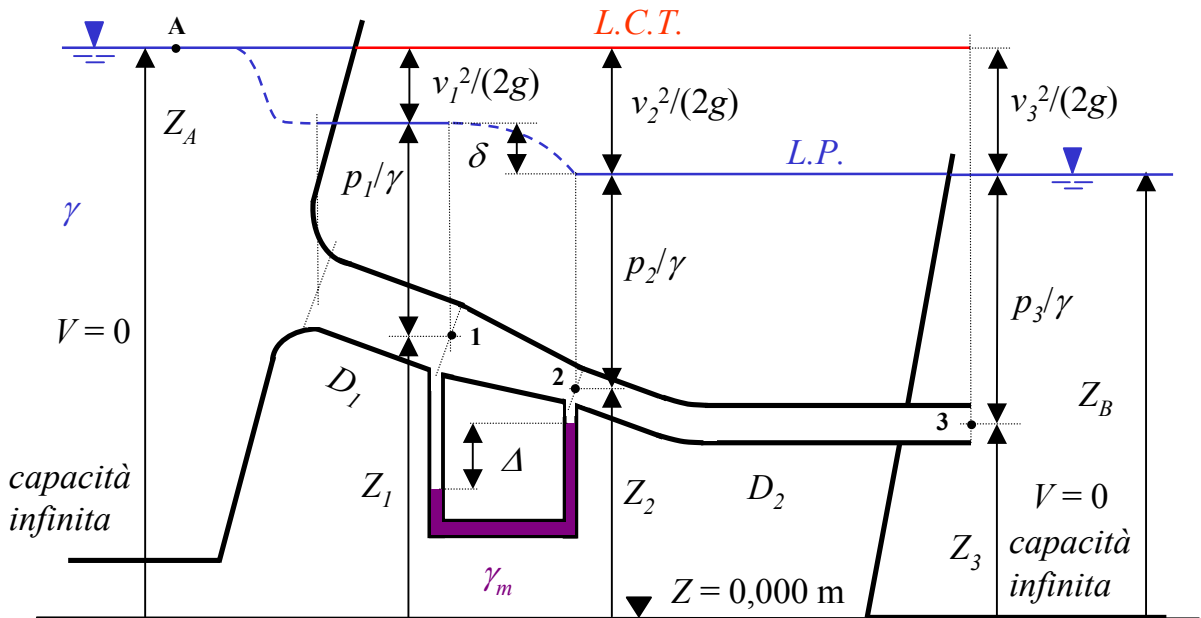
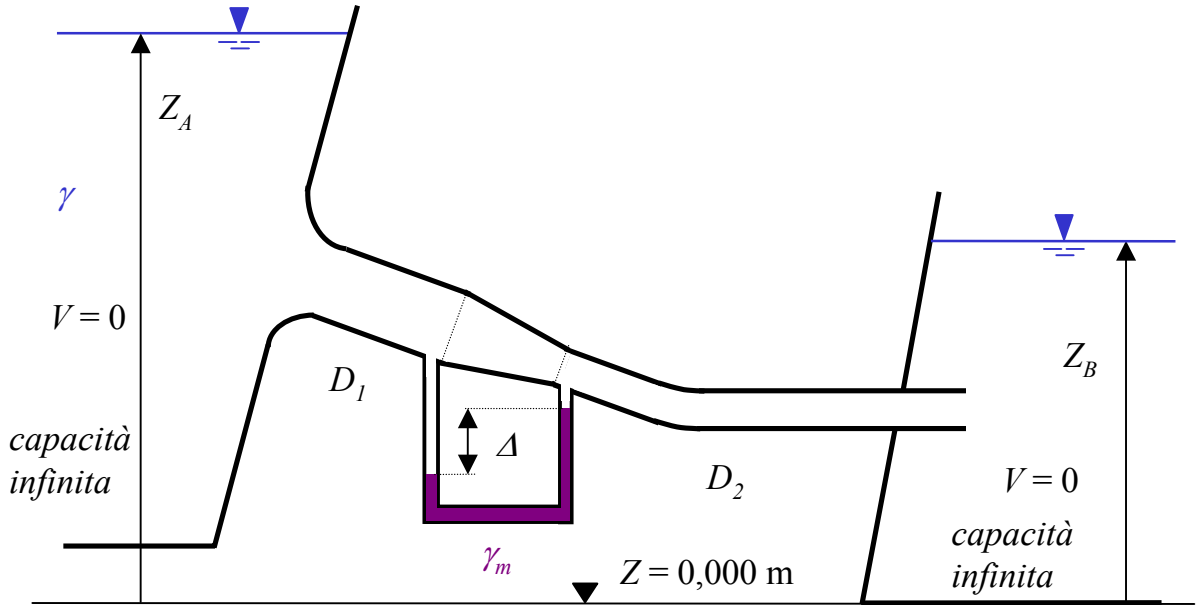


$$\left[ \begin{array}{l} Q = \pi D^2/4 [2g(Z_A - Z_B)]^{1/2} = 2,800 \text{ m}^3/\text{s} \\ Z_C(\alpha = 90^\circ) = Z_{C,MAX} = Z_A = 50,000 \text{ m} \end{array} \quad Z_C(\alpha) = Z_A - [v_B^2/(2g)] \cdot [\cos\alpha]^2 = 47,500 \text{ m} \right]$$

### Esercizio 35

**Noti:**  $Z_A = 12,000$  m,  $D_1 = 0,200$  m,  $D_2 = 0,100$  m,  $\Delta = 0,150$  m,  $\gamma = 9806$  N/m<sup>3</sup>,  $\gamma_m = 133362$  N/m<sup>3</sup>,  $g = 9,806$  m/s<sup>2</sup>, *fluido ideale*.

**Determinare** la portata  $Q$  transitante ed il livello  $Z_B$  del serbatoio di valle. **Tracciare** la *linea dei carichi totali* (L.C.T.) e la *linea piezometrica* (L.P.).



$$Q = [A_1 A_2] / [A_1^2 - A_2^2]^{1/2} [2 g \Delta (\gamma_m - \gamma) / \gamma]^{1/2} = 0,049 \text{ m}^3/\text{s}$$

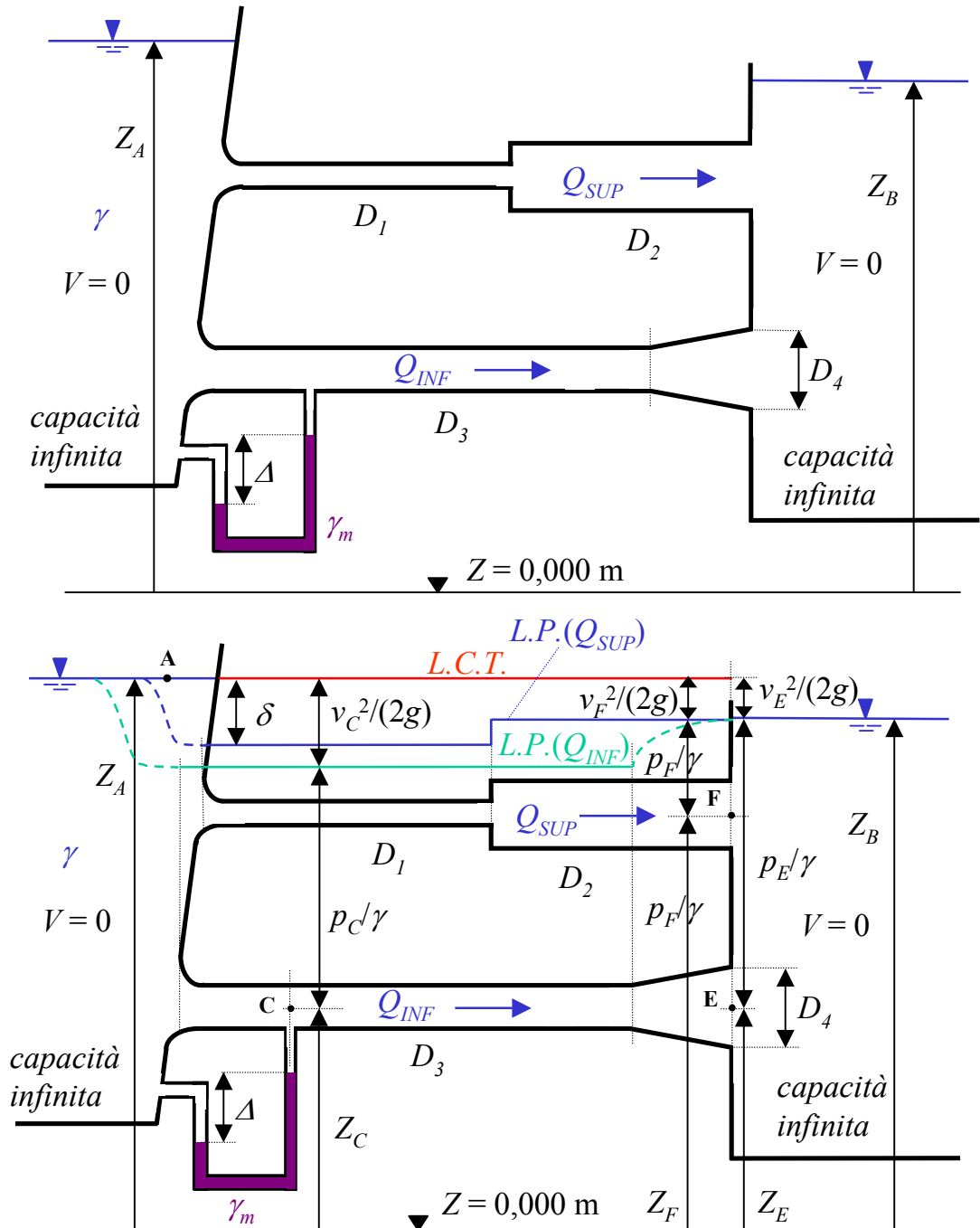
$$Z_B = Z_A - Q^2 / (2 g A_2^2) = 9,984 \text{ m}$$



### Esercizio 37

Noti:  $Z_A = 21,000$  m,  $\Delta = 0,050$  m,  $D_2 = 0,250$  m,  $D_3 = 0,200$  m,  $D_4 = 0,300$  m,  $\gamma = 7800$  N/m<sup>3</sup>,  $\gamma_m = 133362$  N/m<sup>3</sup>,  $g = 9,806$  m/s<sup>2</sup>, fluido ideale.

Determinare le portate transittanti,  $Q_{INF}$  e  $Q_{SUP}$ , ed il livello  $Z_B$  del serbatoio di valle. Tracciare la linea dei carichi totali (L.C.T.) e la linea piezometrica (L.P.).

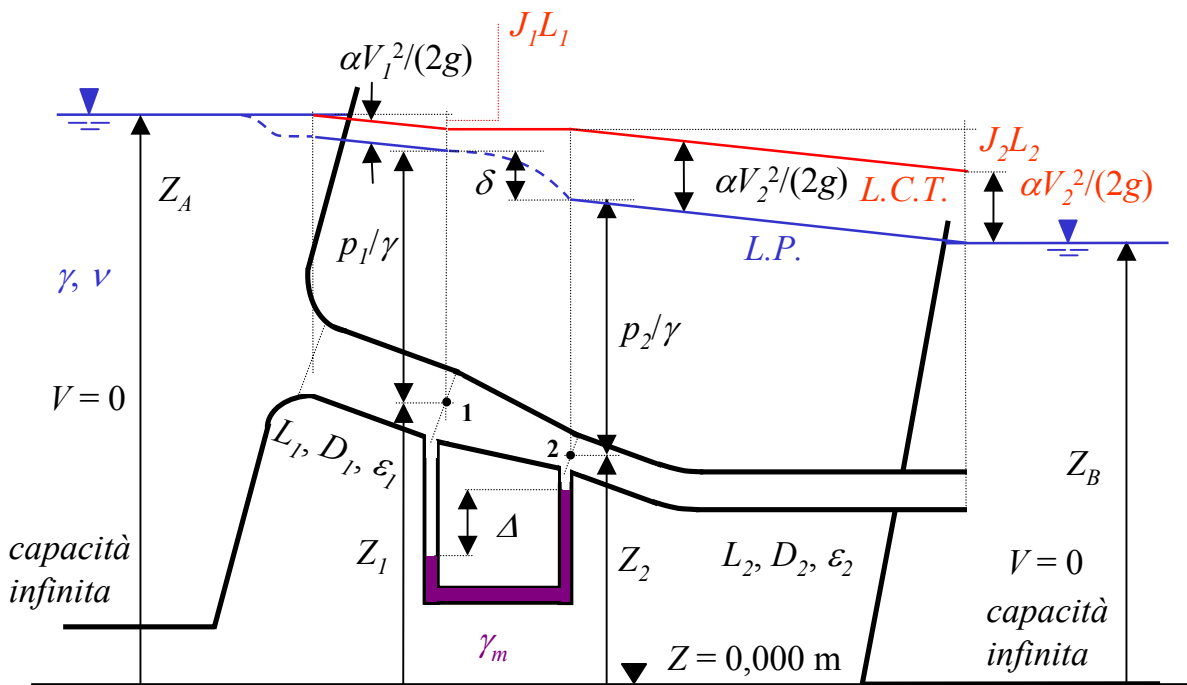
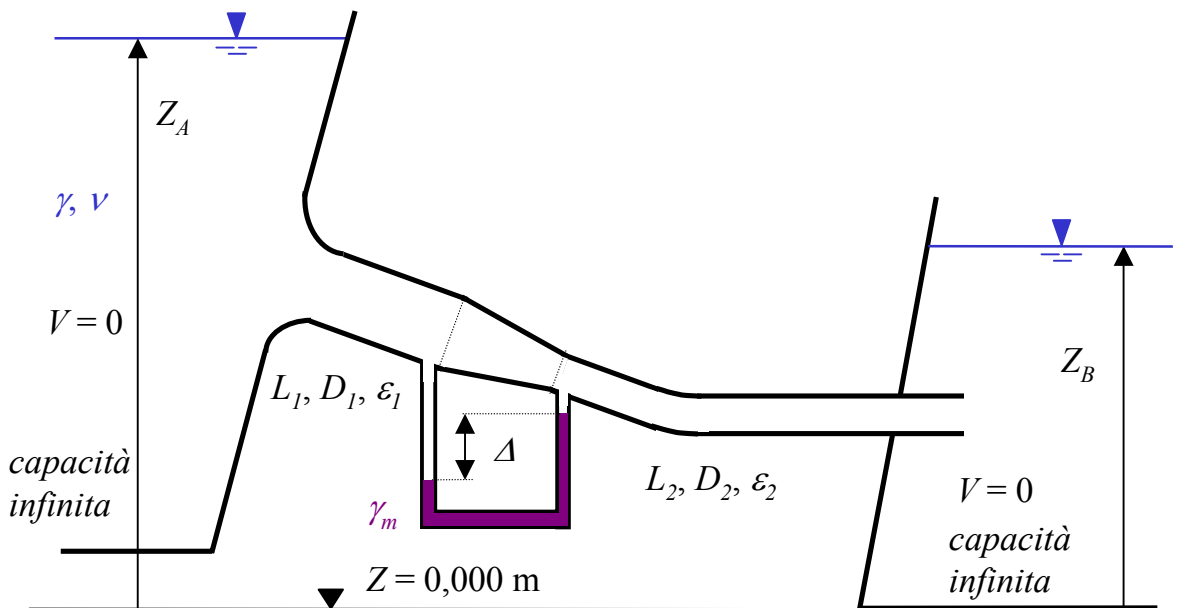


$$\left[ \begin{array}{l} Q_{INF} = A_3 [2 g \Delta (\gamma_m - \gamma) / \gamma]^{1/2} = 0,125 \text{ m}^3/\text{s} \quad Z_B = Z_A - Q_{INF}^2 / (2 g A_4^2) = 20,841 \text{ m} \\ Q_{SUP} = A_2 [2 g (Z_A - Z_B)]^{1/2} = 0,087 \text{ m}^3/\text{s} \end{array} \right]$$

### Esercizio 38

Noti:  $Z_A = 12,000$  m,  $D_1 = 0,200$  m,  $D_2 = 0,100$  m,  $\Delta = 0,150$  m,  $\gamma = 9806$  N/m<sup>3</sup>,  $\gamma_m = 133362$  N/m<sup>3</sup>,  $g = 9,806$  m/s<sup>2</sup>,  $\nu = 2,3 \cdot 10^{-6}$  m<sup>2</sup>/s,  $L_1 = 6,000$  m,  $L_2 = 8,000$  m,  $\varepsilon_1 = 0,0005$  m,  $\varepsilon_2 = 0,000$  m (liscio),  $\alpha = 1$ .

Determinare la portata  $Q$  transitante ed il livello  $Z_B$  del serbatoio di valle. Tracciare la L.C.T. e la L.P..



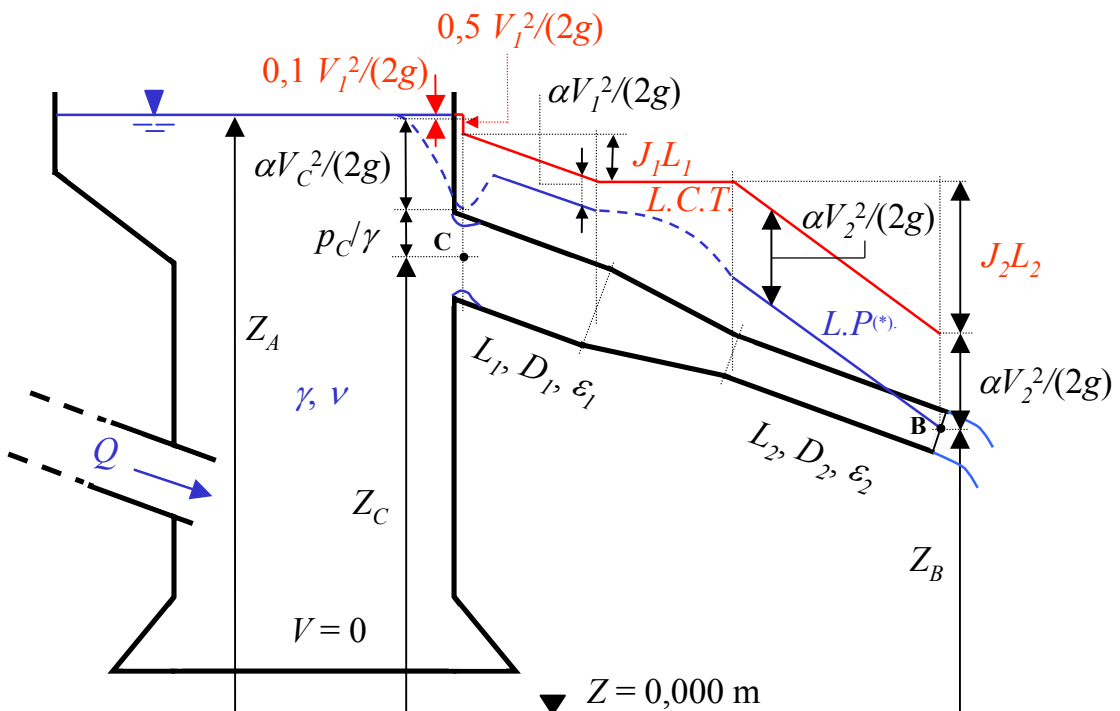
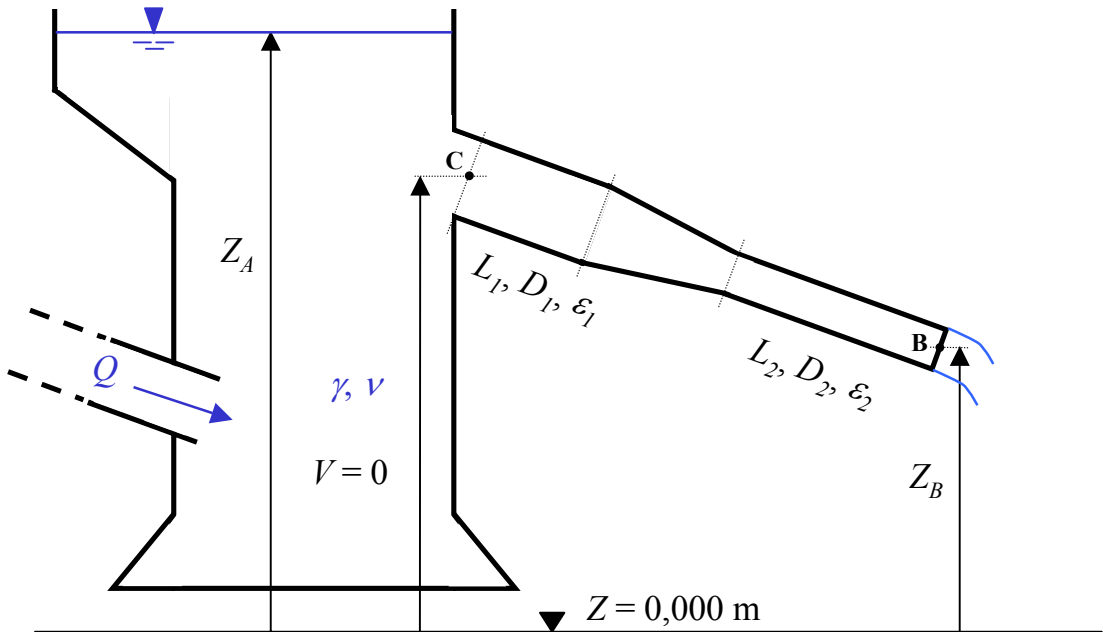
$$Q = [A_1 A_2] / [A_1^2 - A_2^2]^{1/2} [2 g \Delta (\gamma_m - \gamma) / \gamma]^{1/2} = 0,049 \text{ m}^3/\text{s}$$

$$Z_B = Z_A - \lambda_1 / D_1 Q^2 / (2 g A_1^2) L_1 - \lambda_2 / D_2 Q^2 / (2 g A_2^2) L_2 - \alpha Q^2 / (2 g A_2^2) = 7,852 \text{ m}$$

### Esercizio 39

Noti:  $Z_C = 11,000$  m,  $Z_B = 9,000$  m,  $L_1 = 10,000$  m,  $L_2 = 3,000$  m,  $D_1 = 0,200$  m,  $D_2 = 0,150$  m,  $\gamma = 7845$  N/m<sup>3</sup>,  $\nu = 2,3 \cdot 10^{-6}$  m<sup>2</sup>/s,  $Q = 0,100$  m<sup>3</sup>/s,  $C_C = 0,61$ ,  $\varepsilon_1 = \varepsilon_2 = 0,000$  m (primo caso);  $\varepsilon_1 = 8,0 \cdot 10^{-4}$  m,  $\varepsilon_2^{(*)} = 7,0 \cdot 10^{-4}$  m (secondo caso),  $g = 9,806$  m/s<sup>2</sup>,  $\alpha = 1$ .

**Determinare** il livello  $Z_A$  del serbatoio di monte. **Tracciare** la *L.C.T.* e la *L.P.*. **Verificare** il valore della pressione all'imbocco.

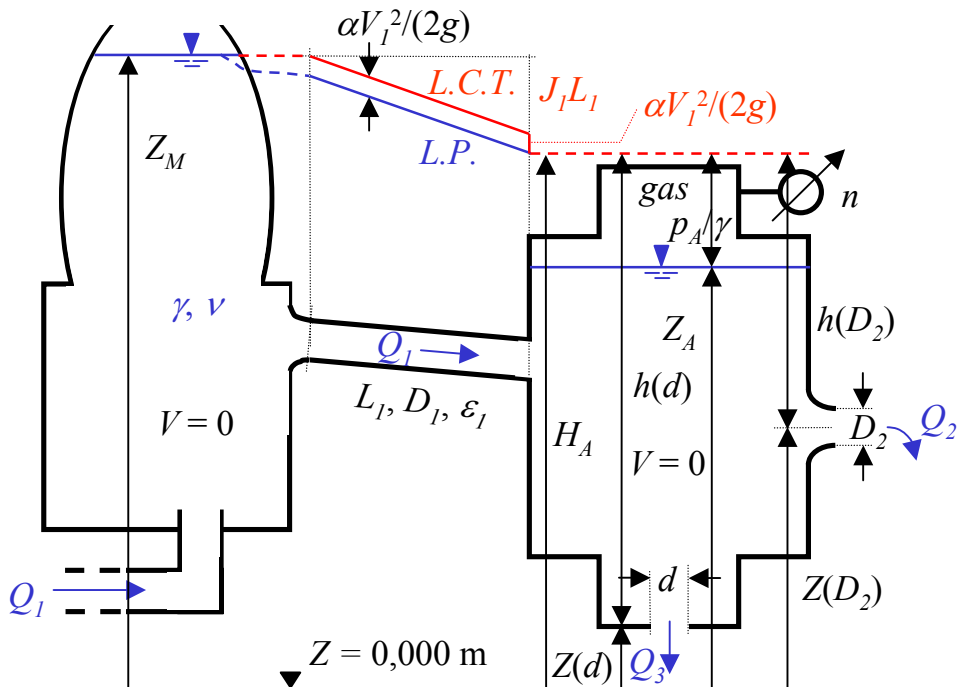
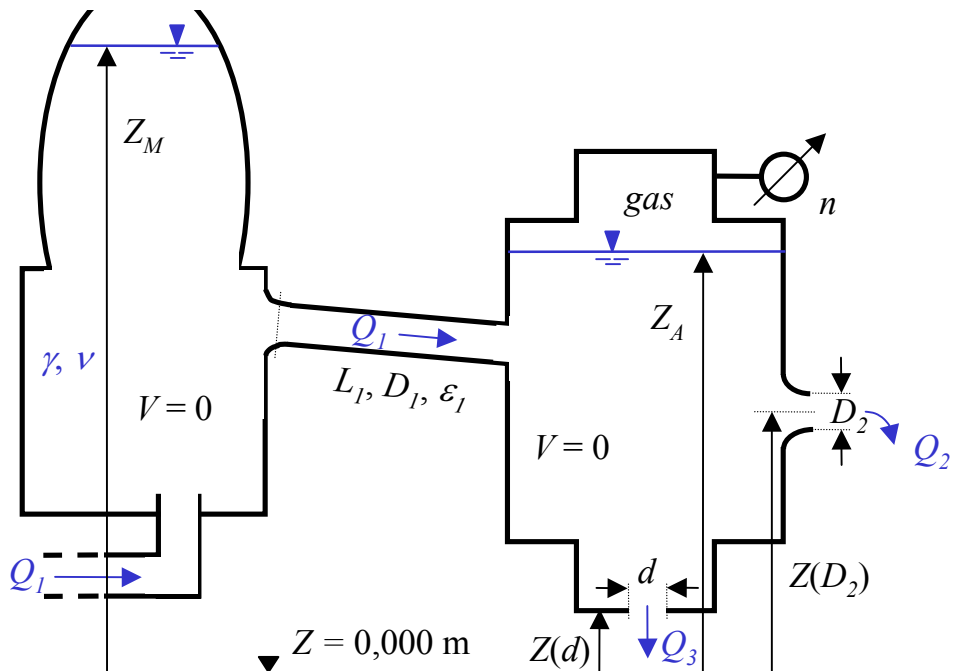


$$\left[ \begin{array}{ll} Z_A = Z_B + \alpha V_2^2/(2g) + 0,5 V_1^2/(2g) + J_1 L_1 + J_2 L_2 = 11,725 \text{ m} & p_C/\gamma = -0,715 \text{ m (tubi lisci)} \\ Z_A = Z_B + \alpha V_2^2/(2g) + 0,5 V_1^2/(2g) + J_1 L_1 + J_2 L_2 = 12,614 \text{ m} & p_C/\gamma = 0,174 \text{ m (tubi scabri)} \end{array} \right]$$

### Esercizio 40

Noti:  $n = 0,25$  bar,  $Z_A = 10,000$  m,  $Z(d) = 3,000$  m,  $Z(D_2) = 5,000$  m,  $L_1 = 100,000$  m,  $D_1 = 0,600$  m,  $\varepsilon_1 = 0,002$  m,  $D_2 = 0,200$  m,  $d = 0,150$  m,  $\gamma = 6668$  N/m<sup>3</sup>,  $\nu = 4,4 \cdot 10^{-7}$  m<sup>2</sup>/s,  $g = 9,806$  m/s<sup>2</sup>,  $\mu(D_2) = 0,98$ ,  $\mu(d) = 0,6$ ,  $\alpha = 1$ .

**Determinare** le portate effluenti,  $Q_2$  e  $Q_3$ , e quella circolante  $Q_1$ ; **determinare** il livello  $Z_M$  del serbatoio di monte. **Tracciare** la L.C.T. e la L.P..



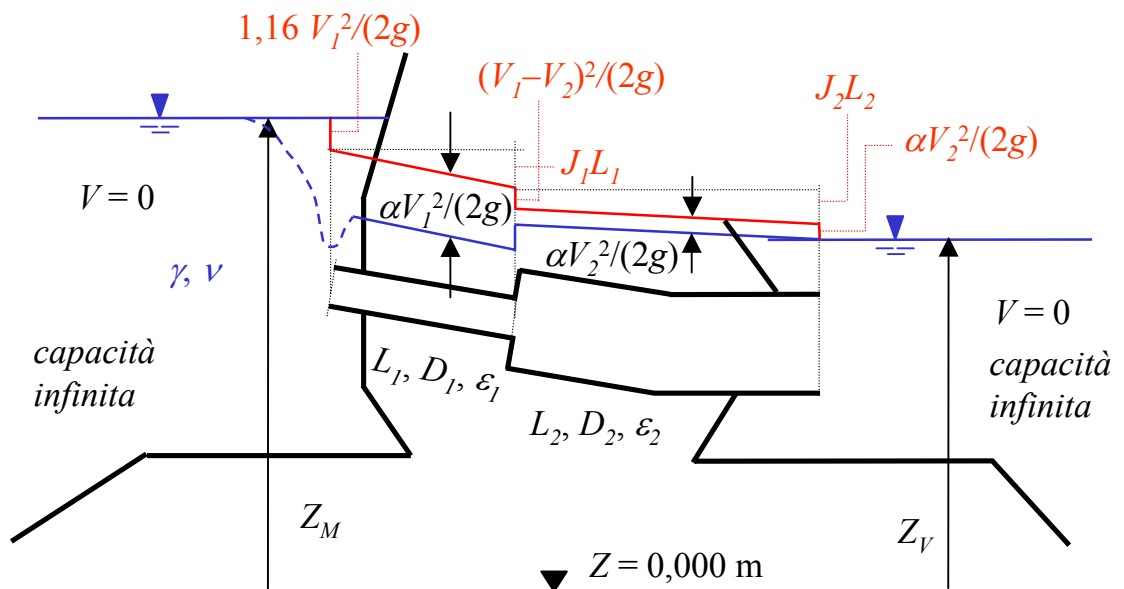
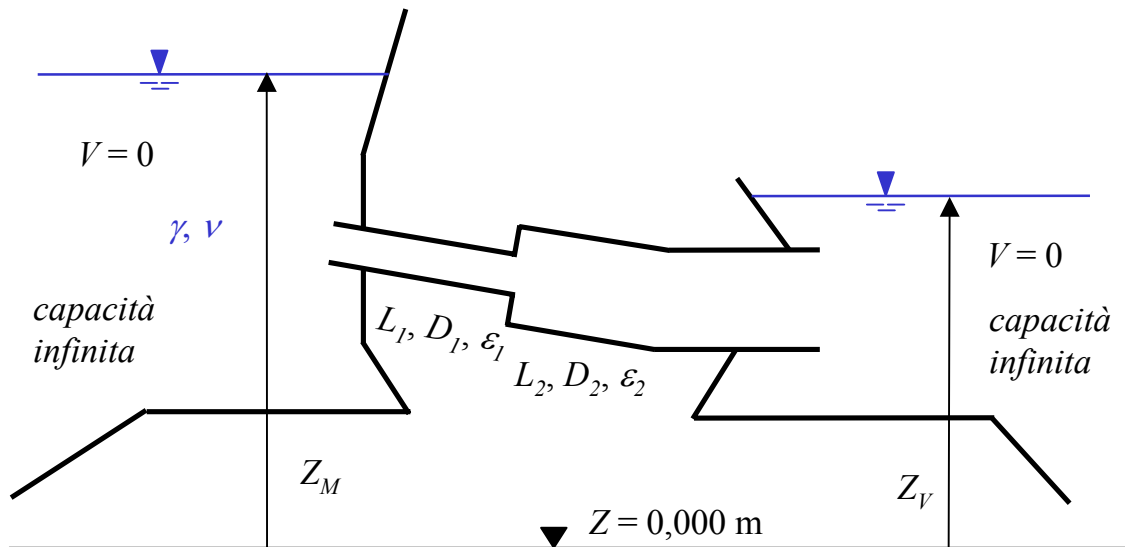
$$\left[ \begin{array}{l} Q_2 = \mu(D_2) A(D_2) [2 g h(D_2)]^{1/2} = 0,403 \text{ m}^3/\text{s} \\ Q_3 = \mu(d) A(d) [2 g h(d)]^{1/2} = 0,154 \text{ m}^3/\text{s} \\ Q_1 = Q_2 + Q_3 = 0,557 \text{ m}^3/\text{s} \\ Z_M = \alpha V_1^2 / (2 g) + J_1 L_1 + H_A = 14,838 \text{ m} \end{array} \right]$$



### Esercizio 41

Noti:  $Z_V = 30,000$  m,  $L_1 = 10,000$  m,  $L_2 = 16,000$  m,  $D_1 = 0,300$  m,  $D_2 = 0,400$  m,  $\gamma = 12366$  N/m<sup>3</sup>,  $\alpha = 1$ ,  $\nu = 6,35 \cdot 10^{-5}$  m<sup>2</sup>/s,  $Q = 0,300$  m<sup>3</sup>/s,  $g = 9,806$  m/s<sup>2</sup>,  $\varepsilon_{1,1} = 0,000$  m (primo caso),  $\varepsilon_{1,2} = 0,005$  m (secondo caso),  $\varepsilon_2 = 0,005$  m.

Determinare il livello  $Z_M$  del serbatoio di monte. Tracciare la L.C.T. e la L.P..

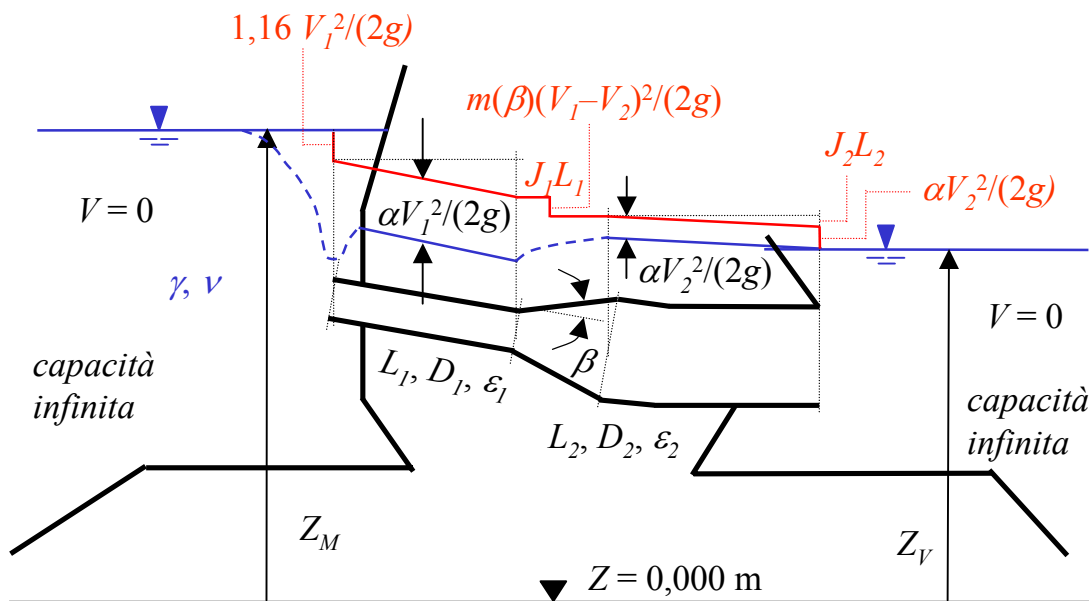
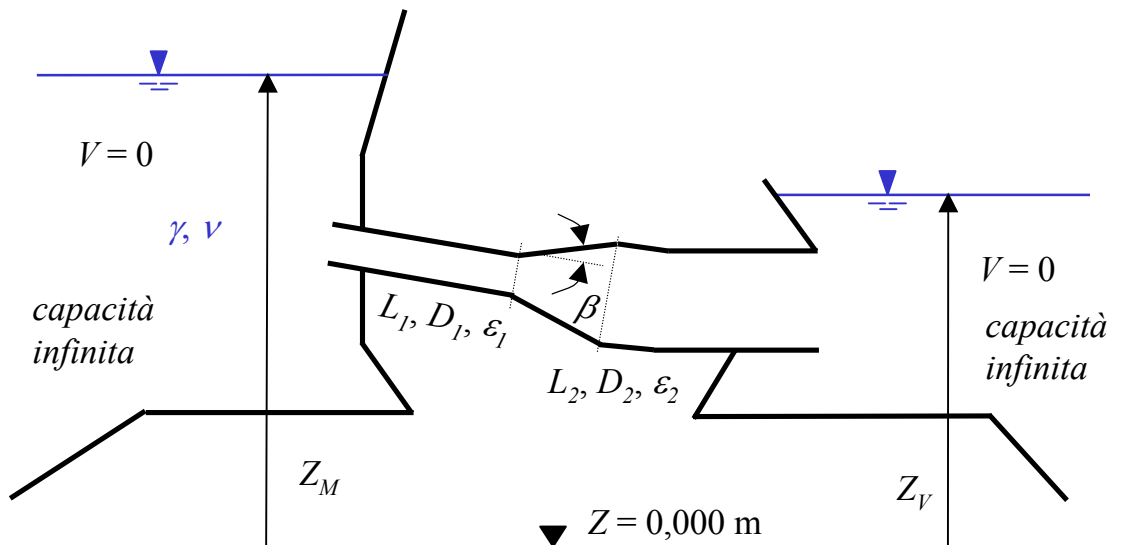


$$\left[ \begin{aligned} Z_M &= 1,16 V_1^2/(2g) + J_{1,1} L_1 + (V_1 - V_2)^2/(2g) + J_2 L_2 + \alpha V_2^2/(2g) + Z_V = 32,837 \text{ m} \\ Z_M &= 1,16 V_1^2/(2g) + J_{1,2} L_1 + (V_1 - V_2)^2/(2g) + J_2 L_2 + \alpha V_2^2/(2g) + Z_V = 33,498 \text{ m} \end{aligned} \right]$$

### Esercizio 42

**Noti:**  $Z_V = 30,000$  m,  $L_1 = 10,000$  m,  $L_2 = 16,000$  m,  $D_1 = 0,300$  m,  $D_2 = 0,400$  m,  $\gamma = 12366$  N/m<sup>3</sup>,  $\alpha = 1$ ,  $\nu = 6,35 \cdot 10^{-5}$  m<sup>2</sup>/s,  $Q = 0,300$  m<sup>3</sup>/s,  $m(\beta) = 0,3$ ,  $\varepsilon_{1,1} = 0,000$  m (primo caso),  $\varepsilon_{1,2} = 0,005$  m (secondo caso),  $\varepsilon_2 = 0,005$  m,  $g = 9,806$  m/s<sup>2</sup>.

**Determinare** il livello  $Z_M$  del serbatoio di monte. **Tracciare** la L.C.T. e la L.P..

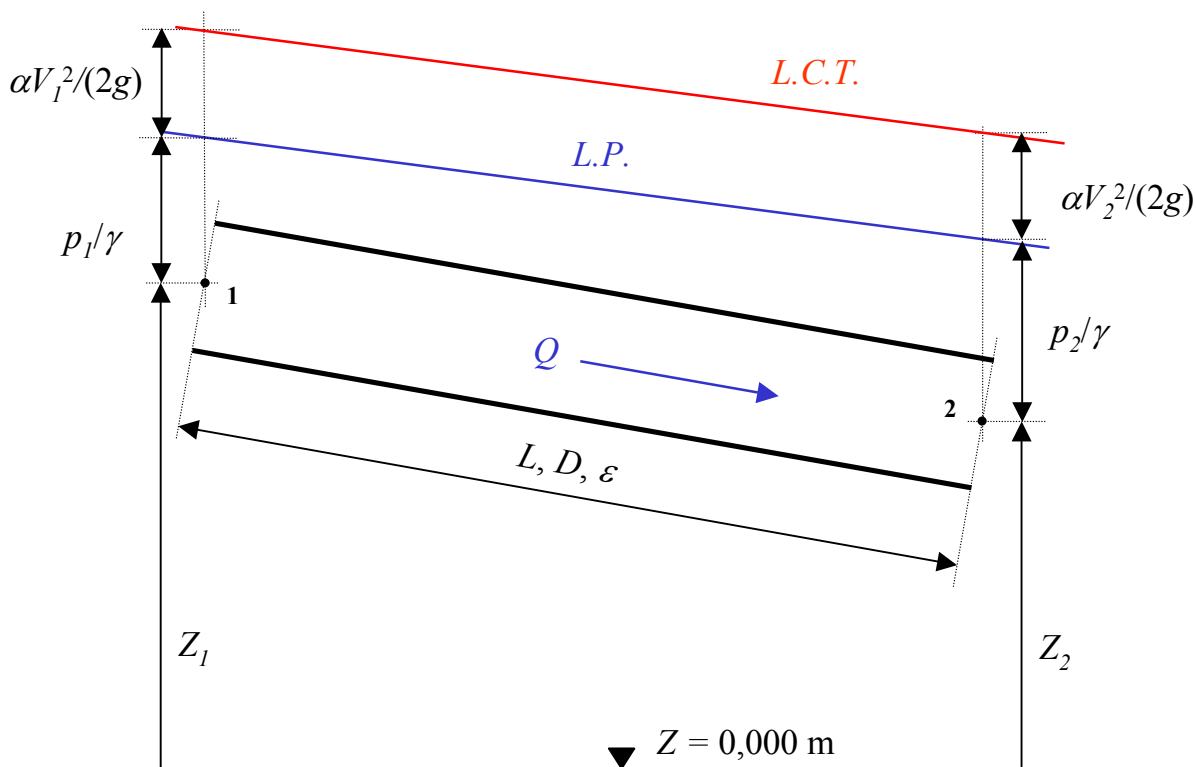


$$\left[ \begin{aligned} Z_M &= 1,16 V_1^2/(2g) + J_{1,1} L_1 + m(\beta) (V_1 - V_2)^2 + J_2 L_2 + \alpha V_2^2/(2g) + Z_V = 32,713 \text{ m} \\ Z_M &= 1,16 V_1^2/(2g) + J_{1,2} L_1 + m(\beta) (V_1 - V_2)^2 + J_2 L_2 + \alpha V_2^2/(2g) + Z_V = 33,375 \text{ m} \end{aligned} \right]$$

### Esercizio 43

Noti:  $Z_1 = 45,000$  m,  $Z_2 = 15,000$  m,  $\gamma = 7845$  N/m<sup>3</sup>,  $\nu = 2,3 \cdot 10^{-6}$  m<sup>2</sup>/s,  $p_1 = 300000$  Pa,  $p_2 = 500000$  Pa,  $D = 0,250$  m,  $L = 150,000$  m,  $\varepsilon = 0,00025$  m,  $\alpha = 1$ ,  $g = 9,806$  m/s<sup>2</sup>.

Determinare la portata  $Q$  transitante. Tracciare la L.C.T. e la L.P..

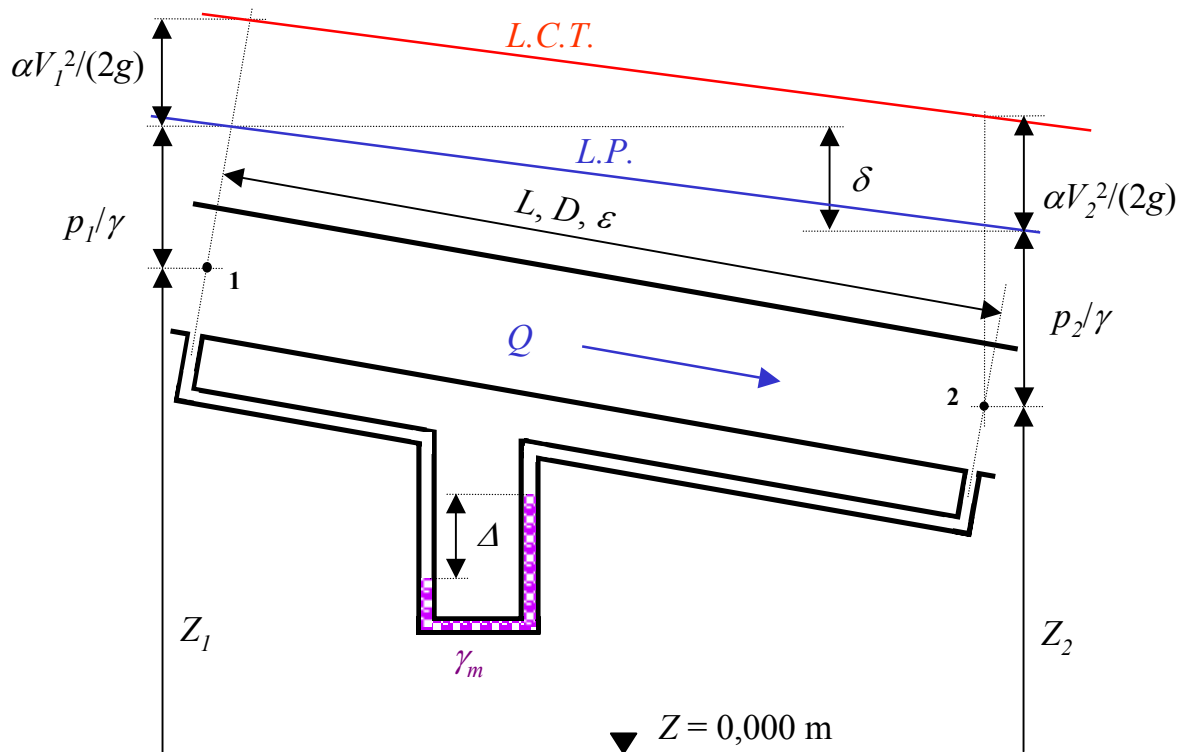


$$(Q = \pi D^2/4 [2 g D J/\lambda]^{1/2} = 0,131 \text{ m}^3/\text{s})$$

### Esercizio 44

Noti:  $\Delta = 0,282$  m,  $\gamma = 7845$  N/m<sup>3</sup>,  $\nu = 2,3 \cdot 10^{-6}$  m<sup>2</sup>/s,  $\gamma_m = 133362$  N/m<sup>3</sup>,  $D = 0,250$  m,  $L = 150,000$  m,  $\varepsilon = 0,00025$  m,  $\alpha = 1$ ,  $g = 9,806$  m/s<sup>2</sup>.

Determinare la portata  $Q$  transitante. Tracciare la *L.C.T.* e la *L.P.*.

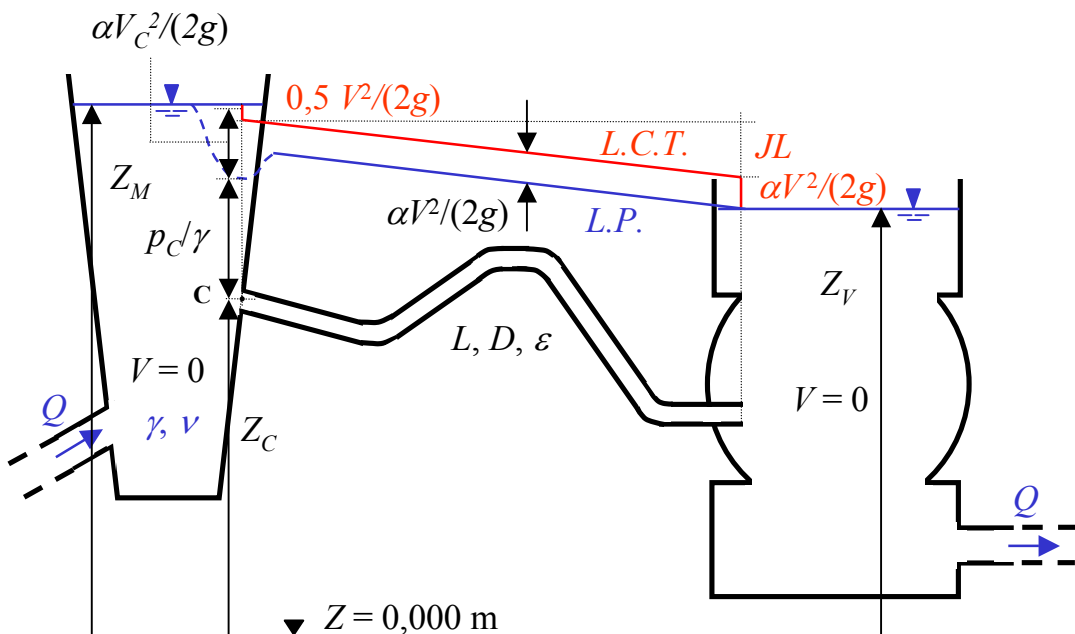
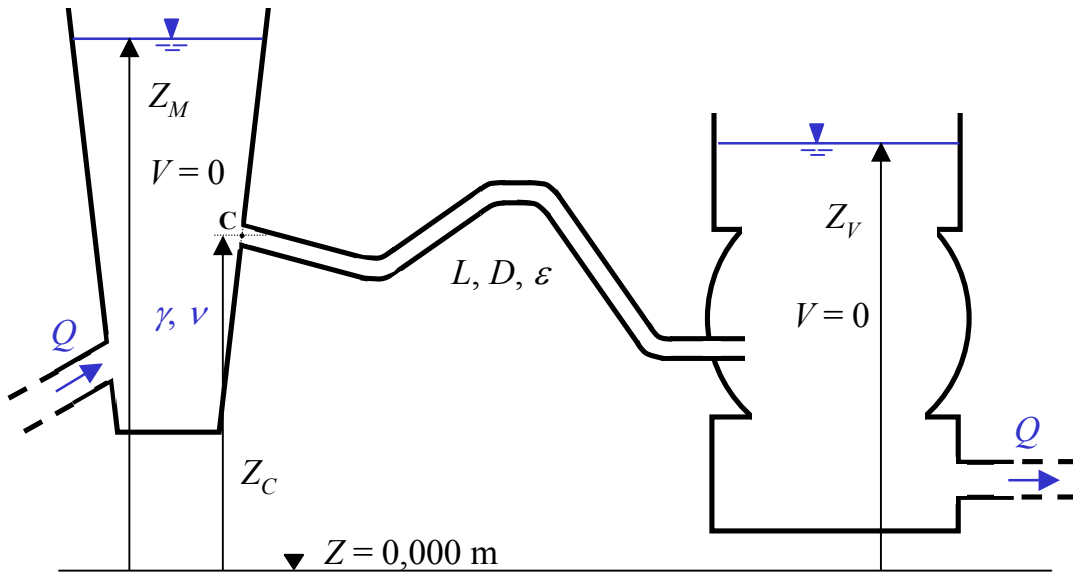


$$(Q = \pi D^2/4 [2 g D J/\lambda]^{1/2} = 0,131 \text{ m}^3/\text{s})$$

### Esercizio 45

Noti:  $Z_M = 50,000$  m,  $Z_V = 20,000$  m,  $Z_C = 35,000$  m,  $L = 100,000$  m,  $D = 0,100$  m,  $\varepsilon = 1,0 \cdot 10^{-4}$  m,  $\gamma = 9806$  N/m<sup>3</sup>,  $\nu = 1,0 \cdot 10^{-6}$  m<sup>2</sup>/s,  $\alpha = 1$ ,  $g = 9,806$  m/s<sup>2</sup>.

Determinare la portata circolante  $Q$  e verificare la pressione all'imbocco **Tracciare** la *L.C.T.* e la *L.P.*.

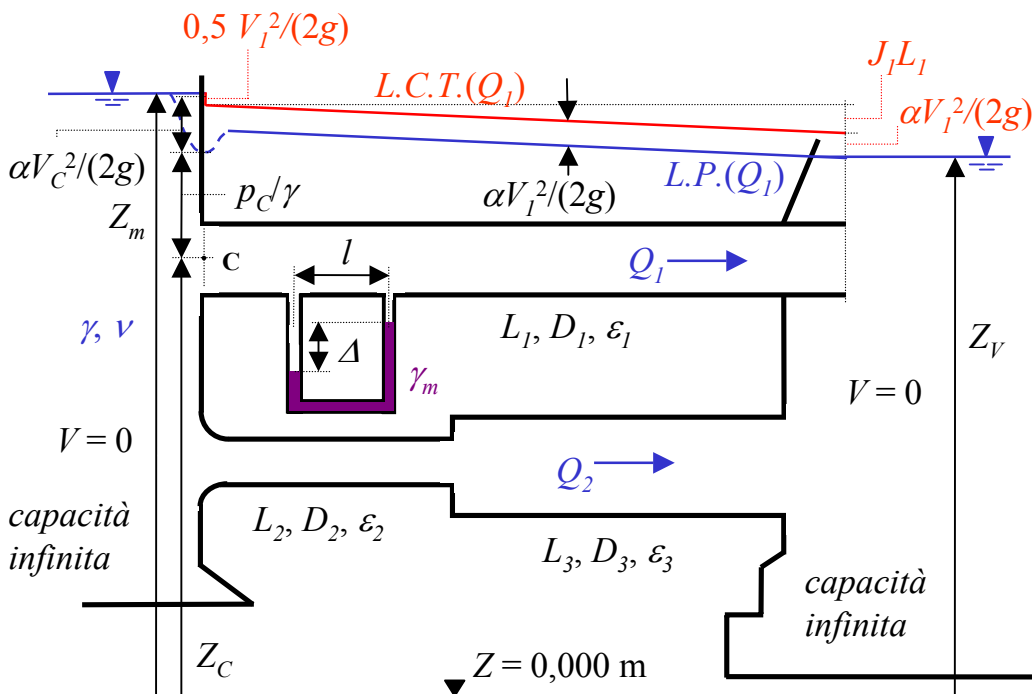
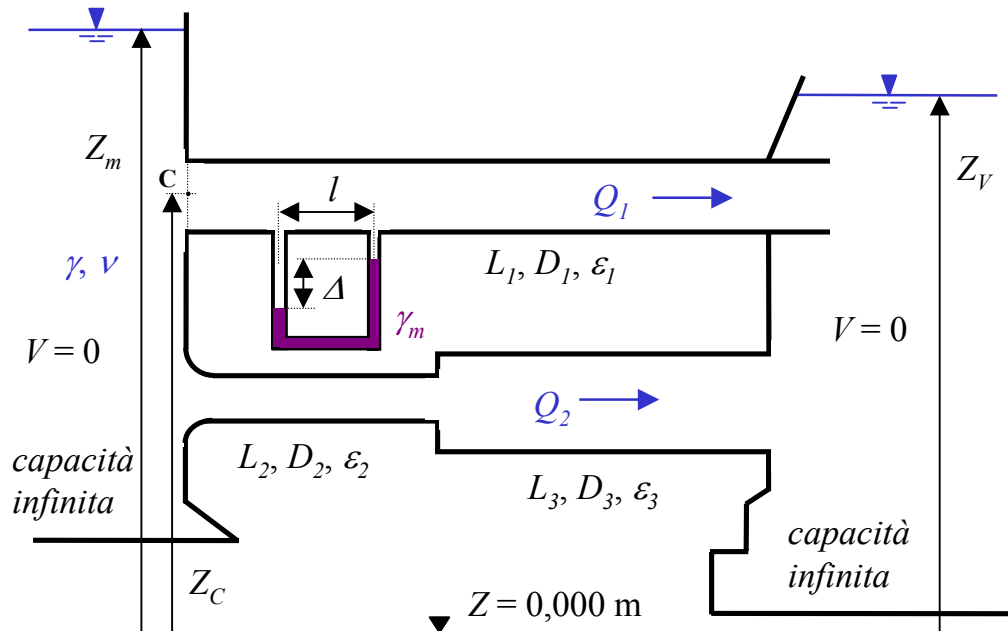


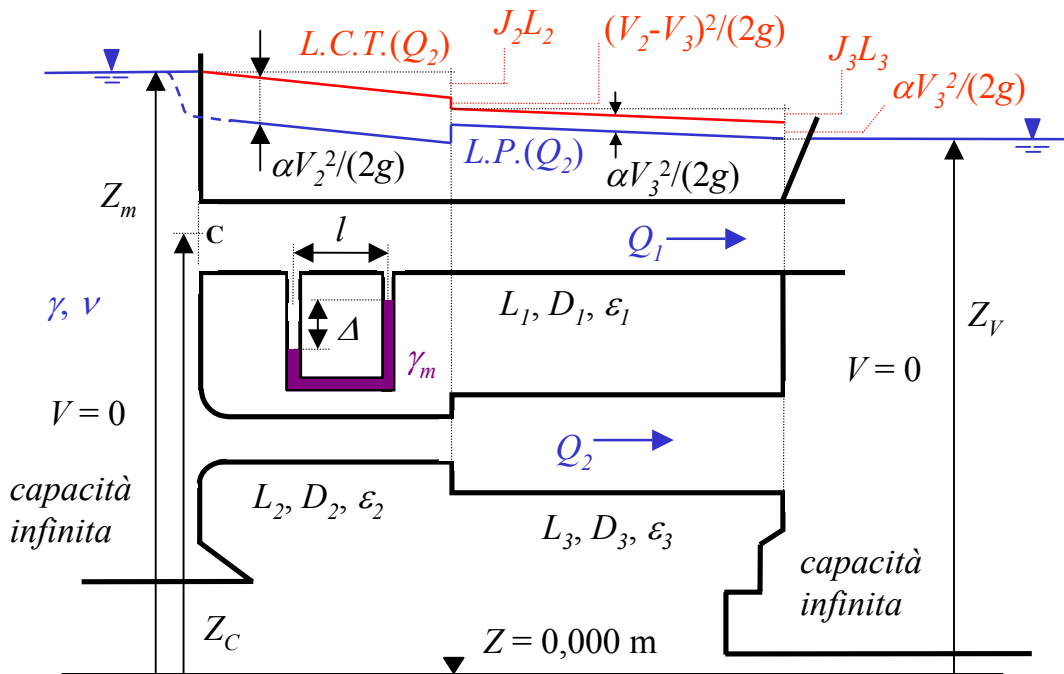
$$\left[ \begin{aligned} Q^{(IV)} &= A \{ [2g(Z_M - Z_V)] / [0,5 + \lambda^{(III)} L/D + 1] \}^{1/2} = 0,0409 \text{ m}^3/\text{s} \\ p_C &= \gamma \{ Z_M - [Z_C + \alpha V_C^2 / (2g) + 0,1 V^2 / (2g)] \} = 108811 \text{ Pa} \end{aligned} \right.$$

### Esercizio 46

Noti:  $Z_m = 50,000$  m,  $Z_C = 40,000$  m,  $L_1 = 300,000$  m,  $L_2 = 150,000$  m,  $L_3 = 150,000$  m,  $D_1 = 0,500$  m,  $D_2 = 0,300$  m,  $D_3 = 0,600$  m,  $\varepsilon_1 = 0,005$  m,  $\varepsilon_2 = 0,009$  m,  $\varepsilon_3 = 0,009$  m,  $\gamma = 9806$  N/m<sup>3</sup>,  $\nu = 1,0 \cdot 10^{-6}$  m<sup>2</sup>/s,  $\gamma_m = 133362$  N/m<sup>3</sup>,  $\Delta = 0,300$  m,  $l = 30,000$  m,  $C_C = 0,61$ ,  $g = 9,806$  m/s<sup>2</sup>,  $\alpha = 1$ .

**Determinare** le portate circolanti  $Q_1$  e  $Q_2$  ed il livello  $Z_V$  del serbatoio di valle. **Verificare** il valore della pressione all'imbocco. **Tracciare** le L.C.T. e le L.P..





$$Q_1 = A_1 [2 g D_1 J_1 / \lambda_1]^{1/2} = 1,121 \text{ m}^3/\text{s}$$

$$Z_V = Z_M - [0,5 Q_1^2 / (2 g A_1^2) + J_1 L_1 + Q_1^2 / (2 g A_1^2)] = 9,706 \text{ m}$$

$$p_c / \gamma = Z_M - [Z_C + \alpha V_C^2 / (2 g) + 0,1 V_1^2 / (2 g)] = 5,365 \text{ m}$$

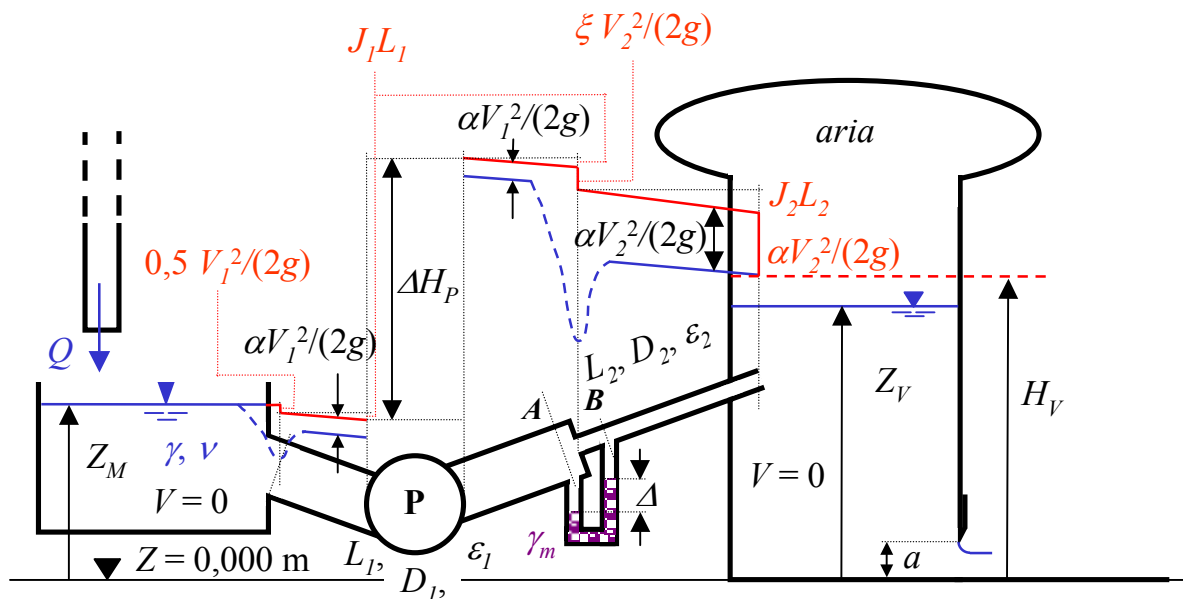
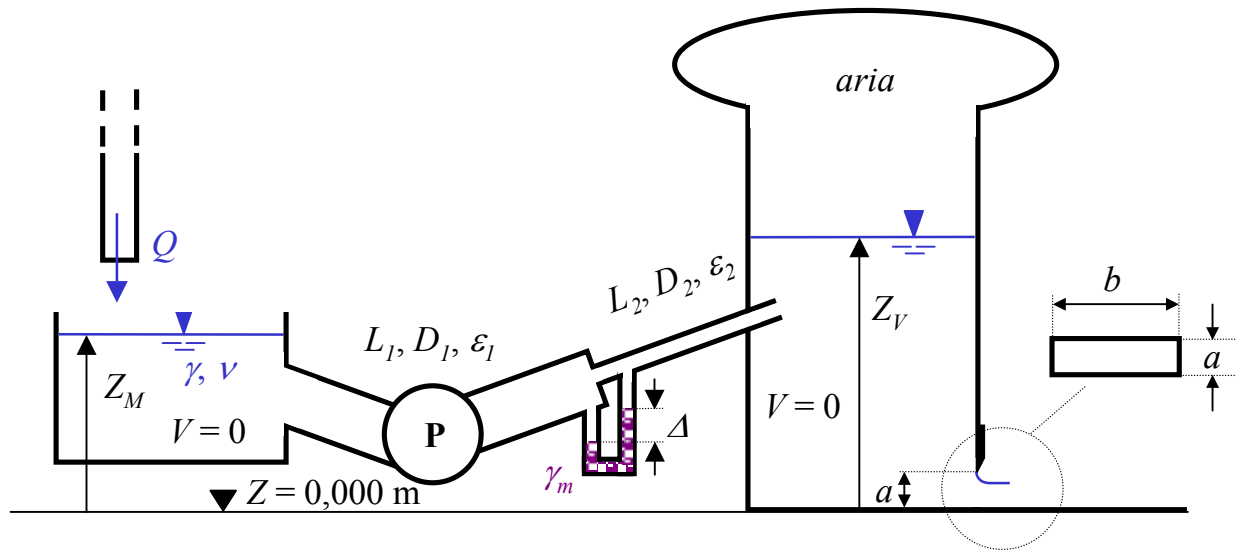
$$Q_2 = \{ (Z_M - Z_V) [ (\lambda_2 L_2) / (2 g D_2 A_2^2) + 1 / (2 g) (1/A_2 - 1/A_3)^2 + (\lambda_3 L_3) / (2 g D_3 A_3^2) + 1 / (2 g A_3^2) ] \}^{1/2} = 0,364 \text{ m}^3/\text{s}$$

### Esercizio 47

**Noti:**  $Z_M = 3,000 \text{ m}$ ,  $Z_V = 6,500 \text{ m}$ ,  $L_1 = 55,000 \text{ m}$ ,  $L_2 = 40,000 \text{ m}$ ,  $a = 0,040 \text{ m}$ ,  $b = 0,750 \text{ m}$ ,  $\alpha = 1$ ,  
 $D_1 = 0,300 \text{ m}$ ,  $D_2 = 0,200 \text{ m}$ ,  $\xi_{brusco\ restr.} = 0,32$ ,  $\eta_p = 0,75$ ,  $C_C = 0,61$ ,  $\mu = 0,6$ ,  $\varepsilon_1 = \varepsilon_2 = 6,0 \cdot 10^{-4} \text{ m}$ ,  
 $\Delta = 0,300 \text{ m}$ ,  $\gamma = 7845 \text{ N/m}^3$ ,  $\nu = 2,3 \cdot 10^{-6} \text{ m}^2/\text{s}$ ,  $\gamma_m = 133362 \text{ N/m}^3$ ,  $g = 9,806 \text{ m/s}^2$ .

**Determinare** la portata circolante  $Q$ , il carico  $H_V$  del serbatoio di valle, la pressione dell'aria e la potenza  $W_p$  assorbita dalla pompa.

**Tracciare** la *L.C.T.* e la *L.P.*.



$$Q = \left\{ \frac{2g\Delta(\gamma_m - \gamma)}{\gamma} \left[ \frac{1}{(1 + \xi)/A_2^2 - 1/A_1^2} \right] \right\}^{1/2} = 0,288 \text{ m}^3/\text{s} \quad H_V = C_C a + \frac{Q^2}{[(\mu a b)^2 2g]} = 13,050 \text{ m}$$

$$\Delta H_p = H_V + 0,5 \frac{Q^2}{2gA_1^2} + (\lambda_1/D_1) \frac{Q^2}{2gA_1^2} L_1 + (\lambda_2/D_2) \frac{Q^2}{2gA_2^2} L_2 + \xi \frac{Q^2}{2gA_2^2} +$$

$$W_p = \gamma Q \Delta H_p / \eta_p = 127293 \text{ W} \quad + \alpha \frac{Q^2}{2gA_2^2} - Z_M = 42,299 \text{ m}$$

$$p_{aria} = \gamma [H_V - Z_V] = 51388 \text{ Pa}$$

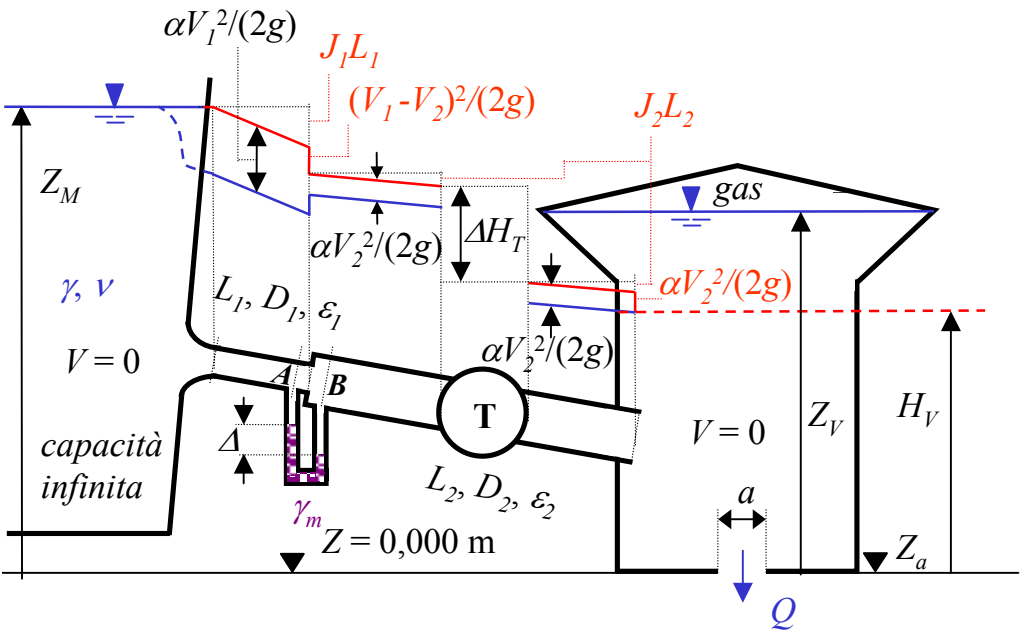
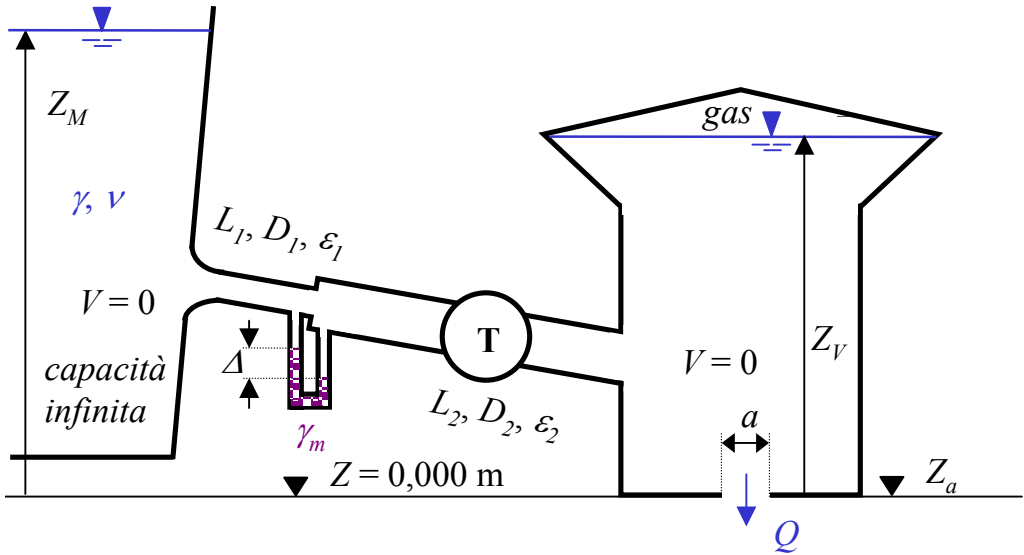


### Esercizio 48

**Noti:**  $Z_M = 25,000$  m,  $Z_V = 9,000$  m,  $Z_a = 0,000$  m,  $L_1 = 30,000$  m,  $L_2 = 60,000$  m,  $a = 0,150$  m (luce circolare),  $D_1 = 0,200$  m,  $D_2 = 0,400$  m,  $\eta_T = 0,8$ ,  $\mu = 0,6$ ,  $\varepsilon_1 = \varepsilon_2 = 2,0 \cdot 10^{-4}$  m,  $\alpha = 1$ ,  $\Delta = 0,030$  m,  $\gamma = 6668$  N/m<sup>3</sup>,  $\nu = 4,4 \cdot 10^{-7}$  m<sup>2</sup>/s,  $\gamma_m = 133362$  N/m<sup>3</sup>,  $g = 9,806$  m/s<sup>2</sup>.

**Determinare** la portata circolante  $Q$ , il carico  $H_V$  del serbatoio di valle, la pressione del gas e la potenza  $W_T$  ritraibile dalla turbina.

**Tracciare** la *L.C.T.* e la *L.P.*.



$$Q = \left\{ \frac{2 g \Delta (\gamma_m - \gamma) \gamma}{[1/A_1^2 - 1/A_2^2 - (1/A_1 - 1/A_2)^2]} \right\}^{1/2} = 0,120 \text{ m}^3/\text{s}$$

$$H_V = \frac{Q^2}{[\mu^2 (\pi a^2/4)^2 2g]} = 6,551 \text{ m}$$

$$\Delta H_T = Z_M - (\lambda_1/D_1) \frac{Q^2}{(2g A_1^2)} L_1 - \frac{Q^2}{(2g)} (1/A_1 - 1/A_2)^2 - (\lambda_2/D_2) \frac{Q^2}{(2g A_2^2)} L_2 - \alpha \frac{Q^2}{(2g A_2^2)} - H_V = 6,551 \text{ m}$$

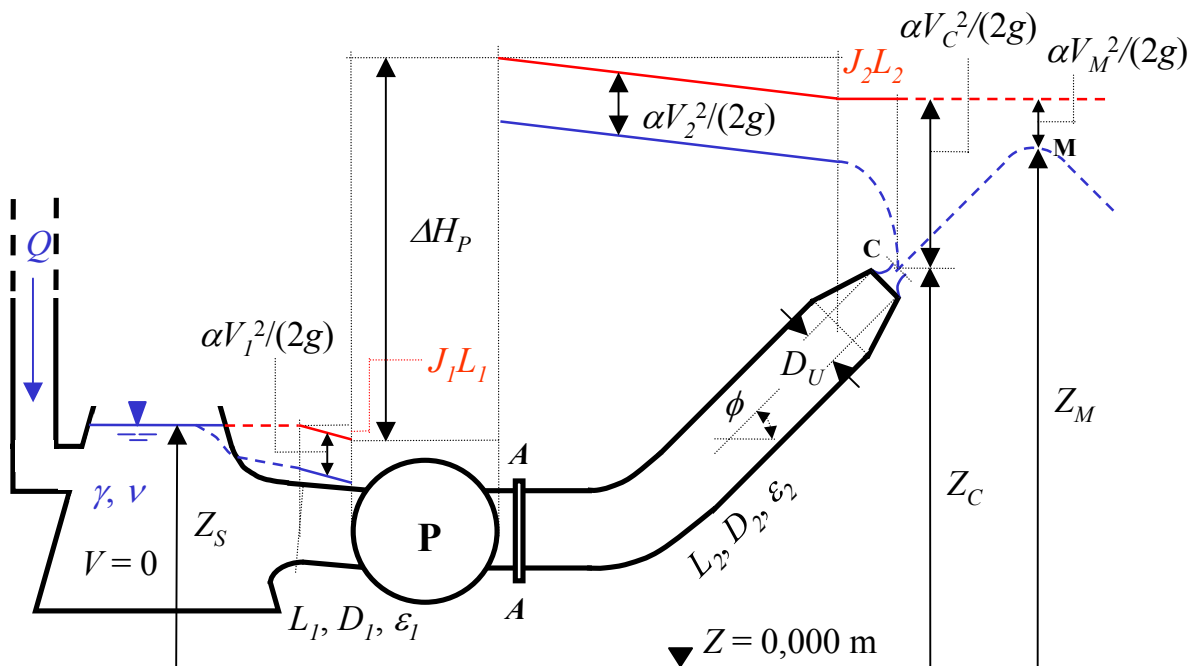
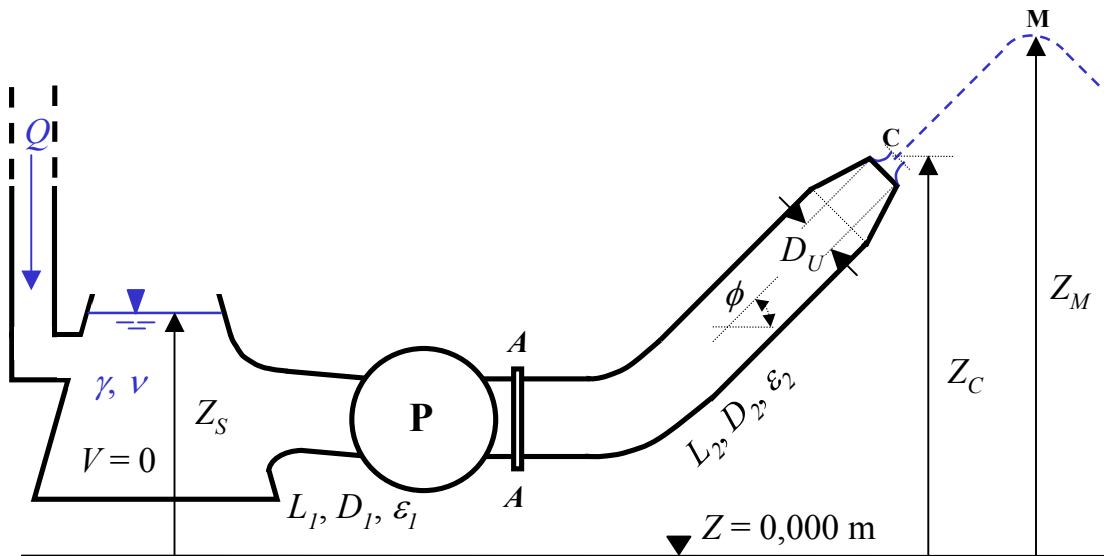
$$W_T = \eta_T \gamma Q \Delta H_T = 4200 \text{ W}$$

$$p_{\text{gas}} = \gamma [H_V - Z_V] = -16330 \text{ Pa}$$

### Esercizio 49

**Noti:**  $Z_S = 9,000$  m,  $Z_C = 11,500$  m,  $Z_M = 13,000$  m,  $\alpha = 1$ ,  $L_1 = 11,000$  m,  $D_1 = 0,250$  m,  $\varepsilon_1 = 1,0 \cdot 10^{-3}$  m,  $L_2 = 20,000$  m,  $D_2 = 0,200$  m,  $\varepsilon_2 = 5,0 \cdot 10^{-4}$  m,  $D_U = 0,150$  m,  $C_C = 0,8$ ,  $\gamma = 7845$  N/m<sup>3</sup>,  $\nu = 2,3 \cdot 10^{-6}$  m<sup>2</sup>/s,  $\eta_P = 0,78$ ,  $\phi = 0,78$ ,  $g = 9,806$  m/s<sup>2</sup> – si consideri trascurabile la distanza tra la pompa e la flangia di traccia AA ed ideale il comportamento del liquido nell'atmosfera.

**Determinare** la portata  $Q$  transitante, la potenza  $W_P$  assorbita dalla pompa. **Tracciare** la *L.C.T.* e la *L.P.*

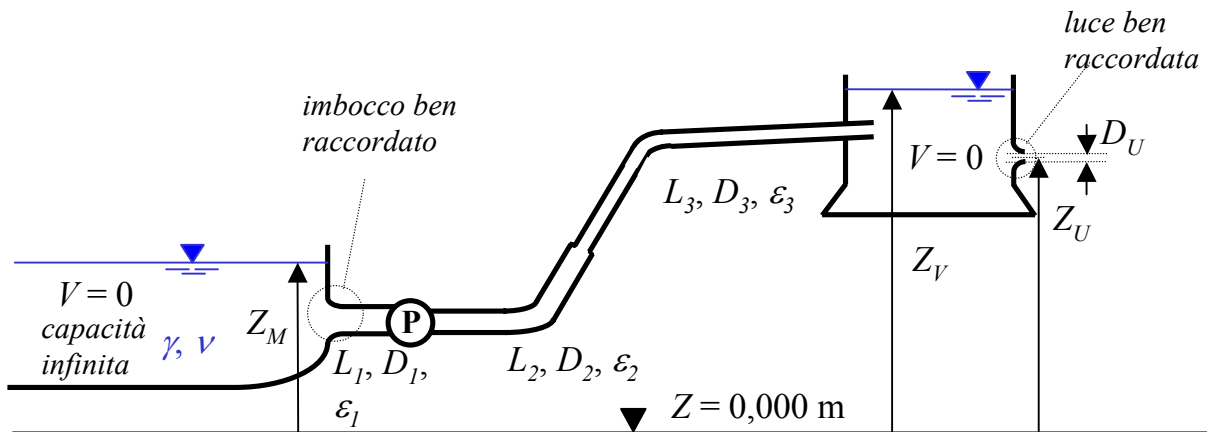


$$\begin{aligned}
 Q &= C_C A_U [2g(Z_M - Z_C) / (\sin \phi)^2]^{1/2} = 0,108 \text{ m}^3/\text{s} \\
 \Delta H_P &= Z_C + \alpha V_C^2 / (2g) + J_2 L_2 - Z_S + J_1 L_1 = 7,358 \text{ m} \\
 W_P &= \gamma Q \Delta H_P / \eta_P = 8024 \text{ W}
 \end{aligned}$$

**Esercizio 50 (Tema d'esame del 15 Luglio 2002)**

**Noti:**  $Z_V = 35,000$  m,  $Z_U = 31,000$  m,  $W_P = (75000 + C \cdot 100)$  W,  $D_1 = 0,400$  m,  $D_2 = 0,350$  m,  $D_3 = 0,300$  m,  $L_1 = 8,000$  m,  $L_2 = (6,000 + N/20)$  m,  $L_3 = 9,000$  m,  $\varepsilon_1 = \varepsilon_2 = \varepsilon_3 = 9 \cdot 10^{-4}$  m,  $D_U = 0,200$  m,  $C_v = 0,98$ ,  $\alpha = 1$ ,  $\eta_p = 0,75$ ,  $\gamma = 9806$  N/m<sup>3</sup>,  $\nu = 1 \cdot 10^{-6}$  m<sup>2</sup>/s,  $\xi_{brusco restr.} = 0,3$ ,  $g = 9,806$  m/s<sup>2</sup>.

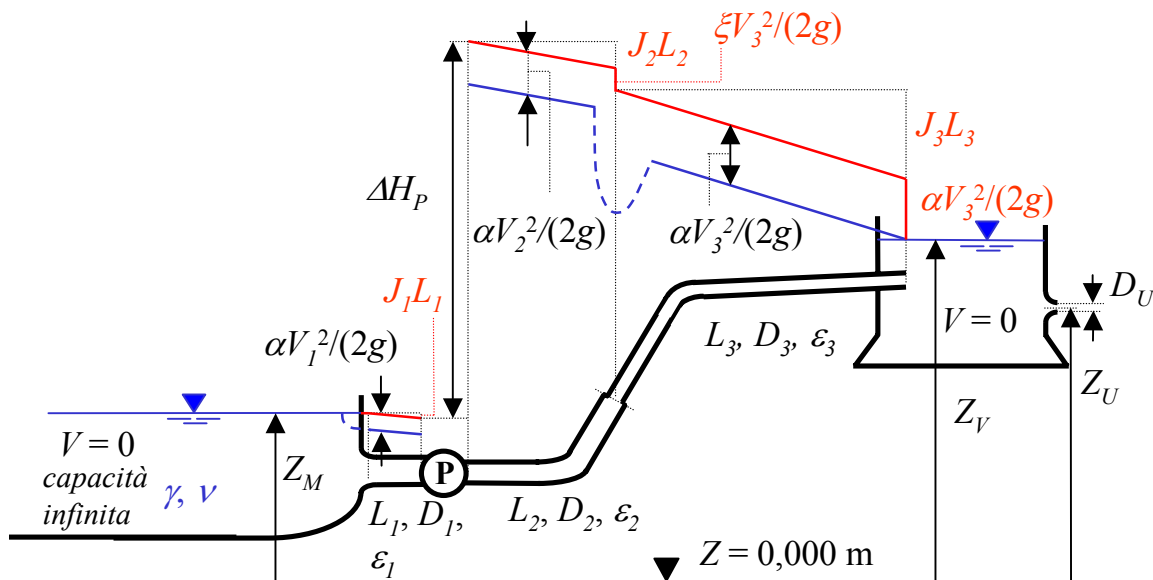
**Determinare** la portata  $Q$  circolante nell'impianto, la prevalenza  $\Delta H_p$  superata dalla pompa, la quota  $Z_M$  del serbatoio di monte. **Tracciare** la LCT e la LP.



A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26

$N =$  prima lettera del nome = 26

$C =$  prima lettera del cognome = 26



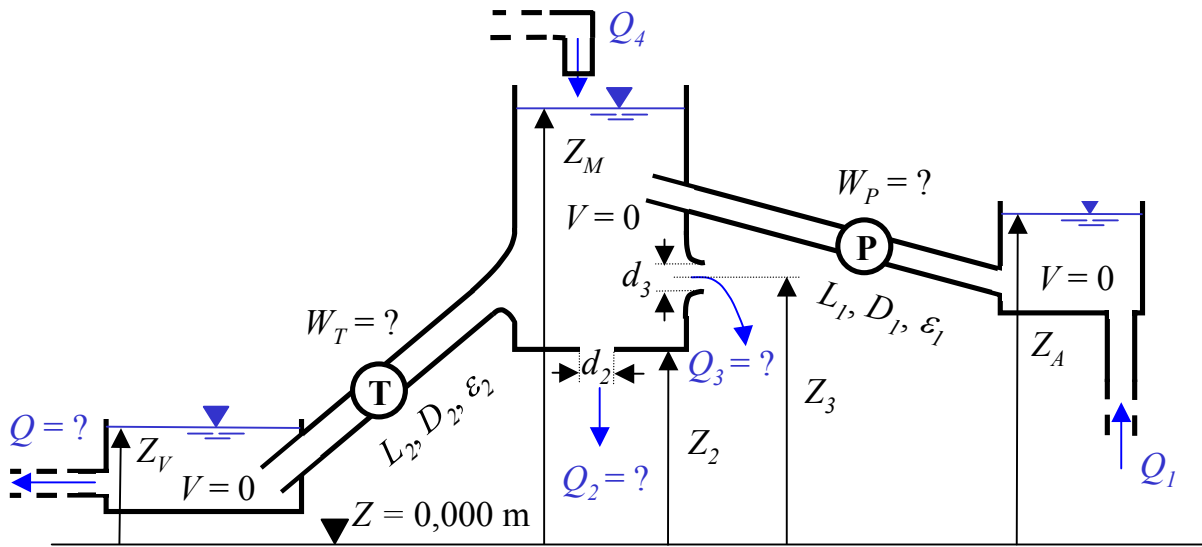
$$\left[ \begin{aligned}
 Q &= C_v A_U [2g(Z_V - Z_U)]^{1/2} = 0,273 \text{ m}^3/\text{s} & \Delta H_p &= \eta_p W_P / (\gamma Q) = 21,765 \text{ m} \\
 Z_M &= (\lambda_1/D_1) Q^2 / (2g A_1^2) L_1 - \Delta H_p + (\lambda_2/D_2) Q^2 / (2g A_2^2) L_2 + \xi Q^2 / (2g A_3^2) + \\
 &\quad + (\lambda_3/D_3) Q^2 / (2g A_3^2) L_2 + \alpha Q^2 / (2g A_3^2) + Z_V = 15,151 \text{ m}
 \end{aligned} \right.$$

**Esercizio 51 (Tema d'esame del 13 Luglio 2004)**

**Noti:**  $Z_A = 450,000$  m,  $Z_M = 500,000$  m,  $Z_V = 200,000$  m,  $Z_2 = 490,000$  m,  $Z_3 = 494,000$  m, moto permanente,  $Q_1 = 0,500$  m<sup>3</sup>/s,  $Q_4 = 0,200$  m<sup>3</sup>/s,  $L_1 = (200,000 + N/10)$  m,  $L_2 = (500,000 + C/10)$  m,  $D_1 = 0,400$  m,  $D_2 = 0,500$  m,  $d_2 = d_3 = 0,100$  m,  $\varepsilon_1 = 0,00$  m,  $\varepsilon_2 = 2,0 \cdot 10^{-3}$  m,  $\alpha = 1$ ,  $\gamma = 9806$  N/m<sup>3</sup>,  $\nu = 1,0 \cdot 10^{-6}$  m<sup>2</sup>/s (viscosità cinematica),  $g = 9,806$  m/s<sup>2</sup>,  $C_v = 0,98$ ,  $\mu = 0,6$ ,  $\eta_T = 0,8$ ,  $\eta_P = 0,7$ .

**Determinare** la potenza  $W_p$  assorbita dalla pompa, le portate effluenti  $Q_2$  e  $Q_3$ , quella circolante  $Q$  e la potenza  $W_T$  ottenibile dalla turbina. **Tracciare** L.P. e L.C.T..

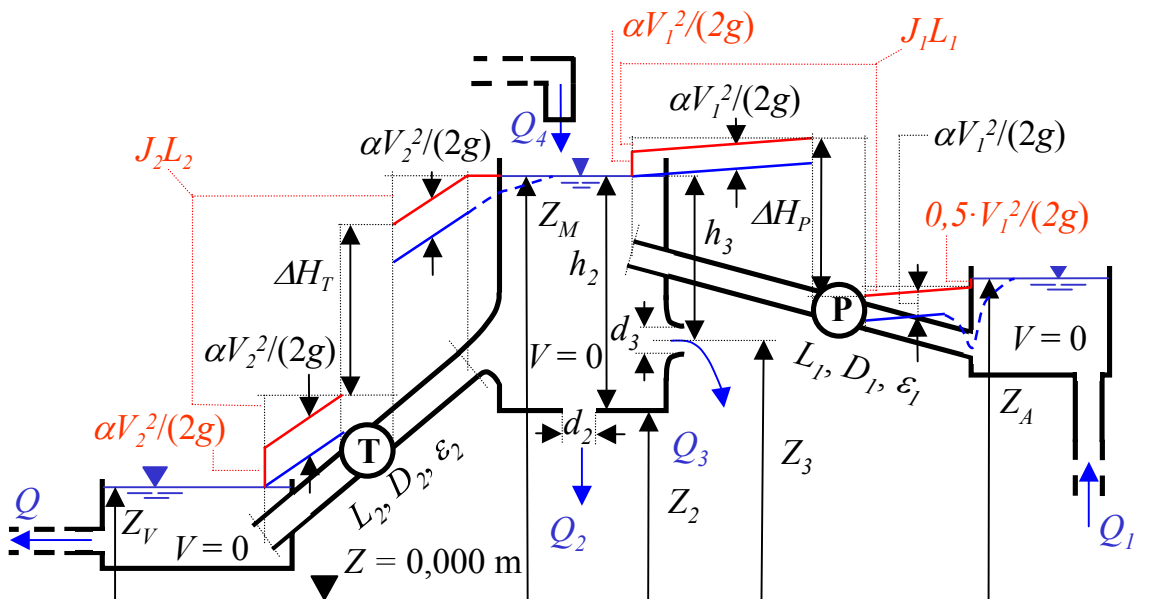
Si descrivano in modo esaustivo le grandezze in gioco ed i passaggi occorrenti alla soluzione.



A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26

$N =$  prima lettera del nome = 1

$C =$  prima lettera del cognome = 1

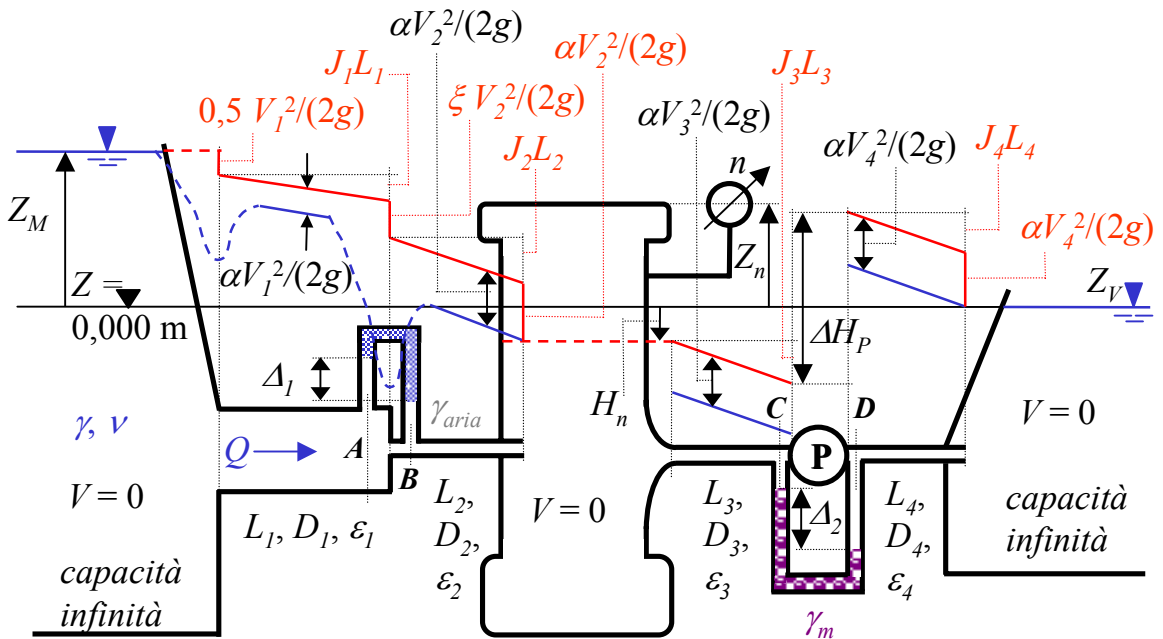
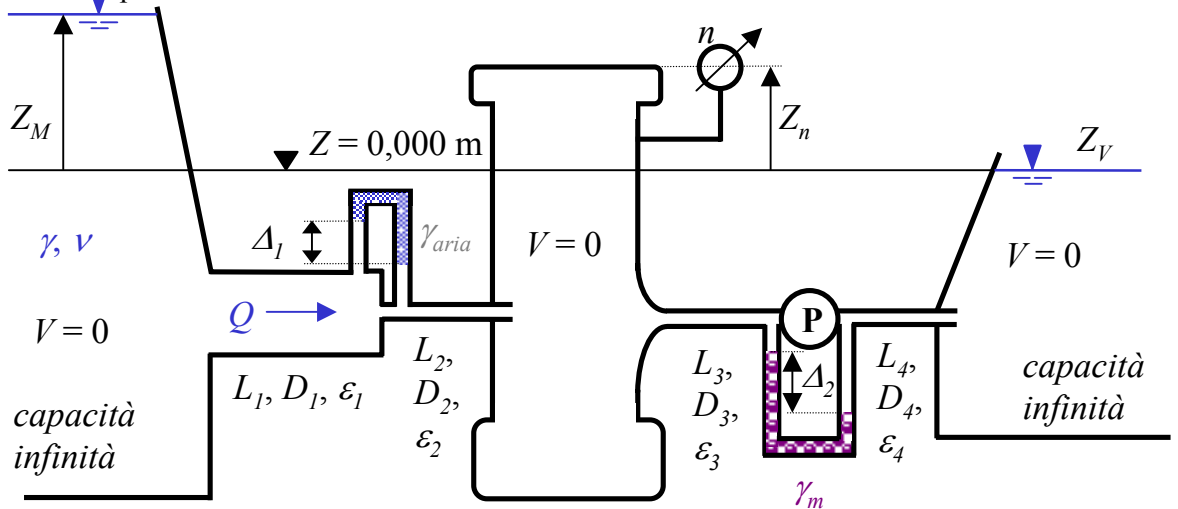


$(W_p = 389153$  W  $Q_2 = 0,066$  m<sup>3</sup>/s  $Q_2 = 0,083$  m<sup>3</sup>/s  $Q_2 = 0,551$  m<sup>3</sup>/s  $W_T = 1244567$  W) 52

### Esercizio 52

**Noti:**  $Z_n = 6,000$  m,  $Z_V = 0,000$  m,  $\alpha = 1$ ,  $L_1 = 15,000$  m,  $L_2 = L_3 = 12,000$  m,  $L_4 = 13,000$  m,  $D_1 = 0,500$  m,  $D_2 = D_3 = D_4 = 0,300$  m,  $\varepsilon_1 = \varepsilon_2 = \varepsilon_3 = \varepsilon_4 = 1,0 \cdot 10^{-3}$  m,  $\xi_{(brusco restr.)} = 0,3$ ,  $\eta_P = 0,75$ ,  $\gamma_m = 133362$  N/m<sup>3</sup>,  $\gamma = 7845$  N/m<sup>3</sup>,  $\nu = 2,3 \cdot 10^{-6}$  m<sup>2</sup>/s,  $\Delta_1 = 0,900$  m,  $\Delta_2 = 0,200$  m,  $g = 9,806$  m/s<sup>2</sup>.

**Determinare** la portata circolante  $Q$ , la potenza  $W_P$  assorbita dalla pompa, il livello  $Z_M$  del serbatoio di monte e la pressione  $n$  rilevata dal manometro metallico. Fare attenzione, l'esercizio può essere risolto anche senza adoperare il manometro differenziale di valle. **Tracciare** la L.C.T. e la L.P..



$$Q = \{ [2 g \Delta_1 / ((1 + \xi) A_2^2 - 1/A_1^2)] \}^{1/2} = 0,275 \text{ m}^3/\text{s} \quad \Delta H_P = \Delta_2 (\gamma_m - \gamma) / \gamma = 3,200 \text{ m}$$

$$W_P = \gamma Q \Delta H_P / \eta_P = 9188 \text{ W}$$

$$H_n = (\lambda_3 / D_3) Q^2 / (2 g A_3^2) L_3 - \Delta H_P + (\lambda_4 / D_4) Q^2 / (2 g A_4^2) L_4 + \alpha Q^2 / (2 g A_4^2) + Z_V = -0,689 \text{ m}$$

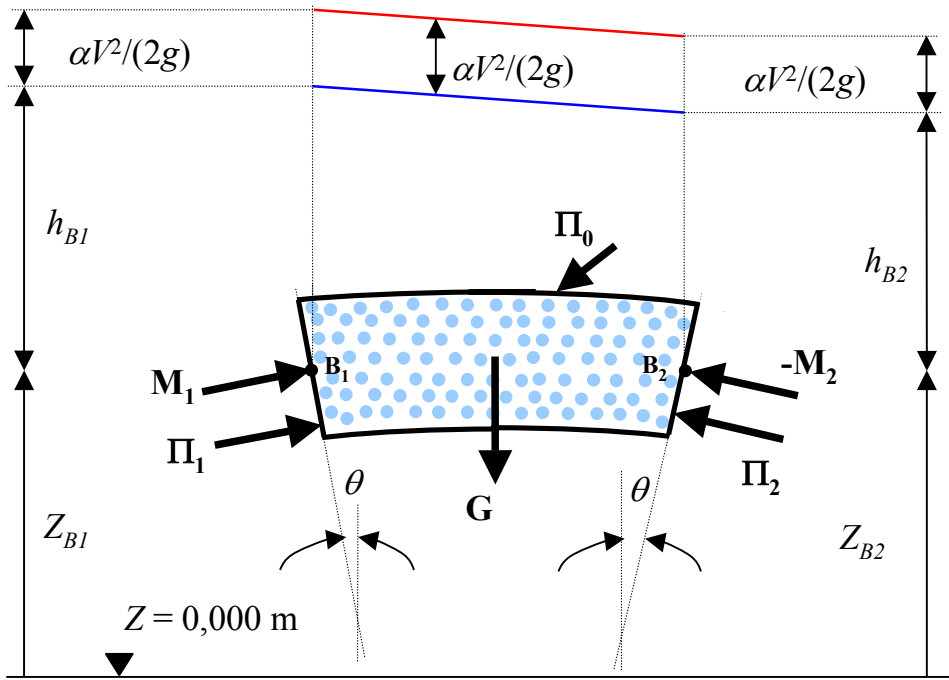
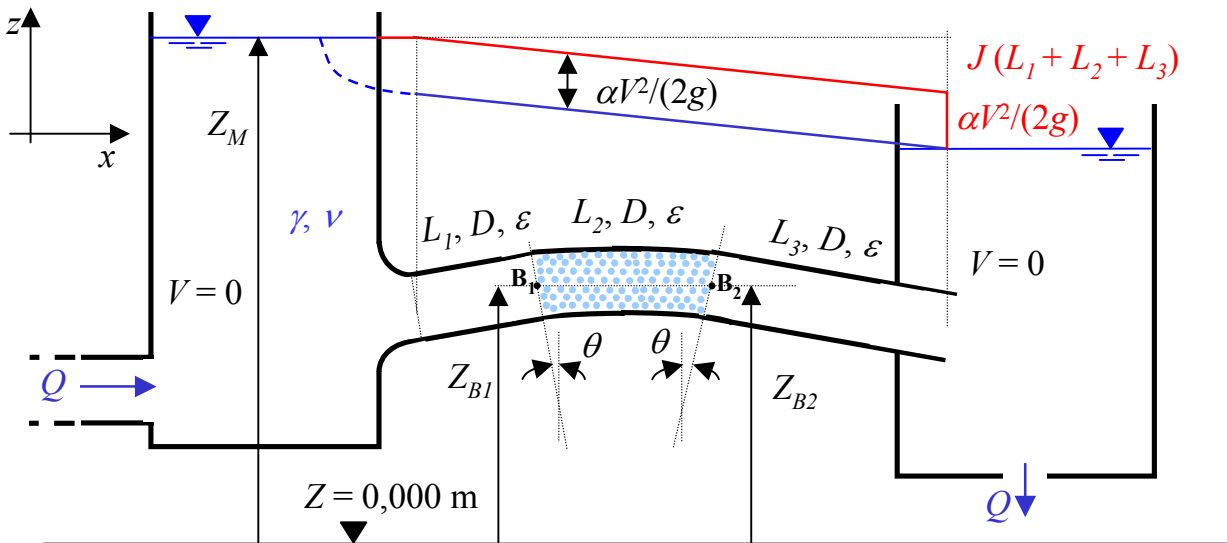
$$n = \gamma [H_n - Z_n] = -52474 \text{ Pa}$$

$$Z_M = 0,5 Q^2 / (2 g A_1^2) + (\lambda_1 / D_1) Q^2 / (2 g A_1^2) L_1 + \xi Q^2 / (2 g A_2^2) + (\lambda_2 / D_2) Q^2 / (2 g A_2^2) L_2 + \alpha Q^2 / (2 g A_2^2) + H_n = 1,269 \text{ m}$$

### Esercizio 53

Noti:  $Z_M = 65,000$  m,  $Z_{B1} = Z_{B2} = 20,000$  m,  $Q = 0,250$  m<sup>3</sup>/s,  $L_1 = 10,000$  m,  $L_2 = 12,000$  m,  $L_3 = 15,000$  m,  $D = 0,200$  m,  $\varepsilon = 7,0 \cdot 10^{-4}$  m,  $\gamma = 6668$  N/m<sup>3</sup>,  $g = 9,806$  m/s<sup>2</sup>,  $\nu = 4,4 \cdot 10^{-7}$  m<sup>2</sup>/s,  $\theta = 10^\circ$ ,  $\alpha = 1$ ,  $\beta = 1$ .

Determinare le componenti della spinta sulla superficie curva di lunghezza  $L_2$  secondo l'assegnato sistema di riferimento.



$$G + \Pi_1 + \Pi_2 + \Pi_0 + M_1 - M_2 = 0$$

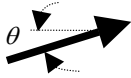
$$S = -\Pi_0 = G + \Pi_1 + \Pi_2 + M_1 - M_2$$

$$G \cong \gamma A L_2$$



applicato nel baricentro del volume di controllo

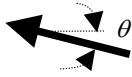
$$\Pi_1 = \gamma h_{B1} A$$



applicata nel centro di spinta della superficie di baricentro  $B_1$ , posto più in basso di quest'ultimo.

$$h_{B1} = Z_M - J L_1 - \alpha V^2 / (2g) - Z_{B1}$$

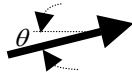
$$\Pi_2 = \gamma h_{B2} A$$



applicata nel centro di spinta della superficie di baricentro  $B_2$ , posto più in basso di quest'ultimo.

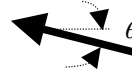
$$h_{B2} = Z_M - J(L_1 + L_2) - \alpha V^2 / (2g) - Z_{B2}$$

$$M_1 = \beta \rho Q V$$



applicato nel baricentro  $B_1$

$$M_2 = \beta \rho Q V$$



applicato nel baricentro  $B_2$

$$S_x = (\Pi_1 + M_1 - \Pi_2 - M_2) \cos \theta = (\Pi_1 - \Pi_2) \cos \theta = \gamma A J L_2 \cos \theta = 290 \text{ N} \longrightarrow$$

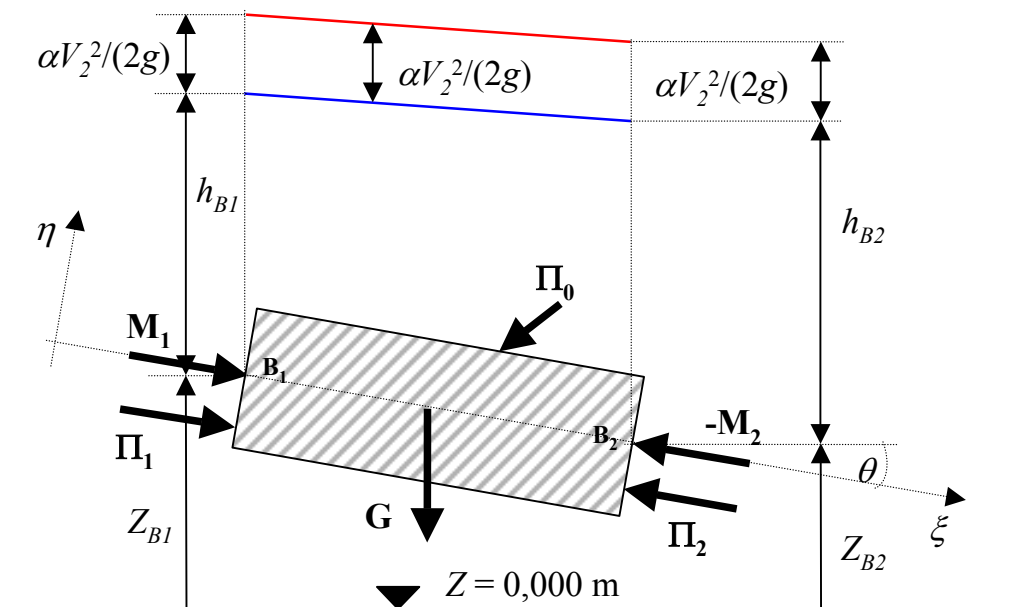
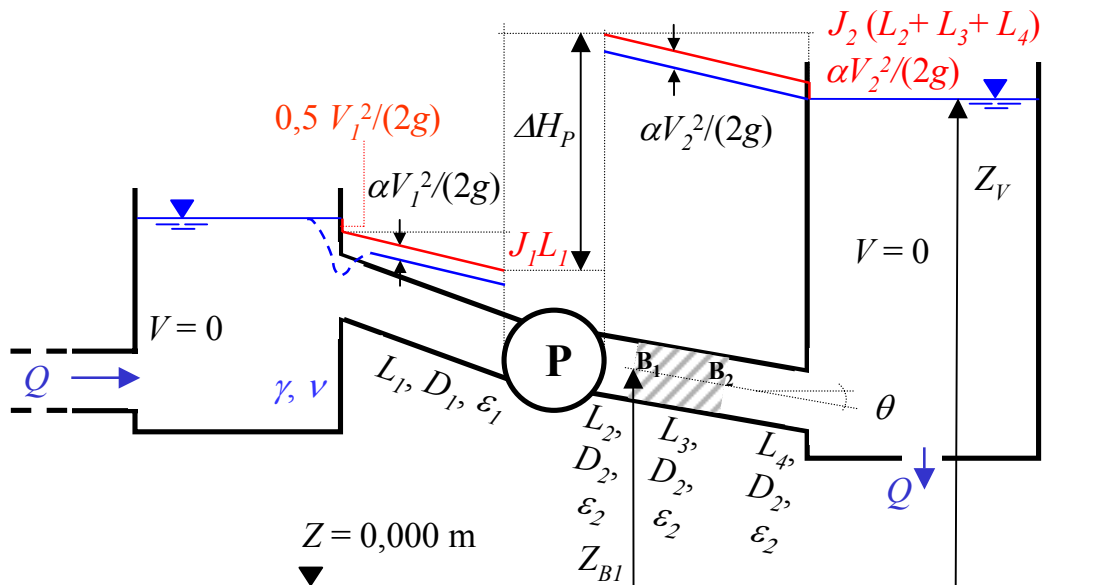
$$S_z = (\Pi_1 + M_1 + \Pi_2 + M_2) \sin \theta - G = 1678 \text{ N} \uparrow$$

$$S = [S_x^2 + S_z^2]^{1/2} = 1703 \text{ N}$$

### Esercizio 54

Noti:  $Z_V = 45,000$  m,  $Z_{B1} = 20,000$  m,  $Q = 0,300$  m<sup>3</sup>/s,  $L_1 = 10,000$  m,  $L_2 = 12,000$  m,  $L_3 = 15,000$  m,  $L_4 = 15,000$  m,  $D_1 = 0,350$  m,  $D_2 = 0,300$  m,  $\varepsilon_1 = 1,0 \cdot 10^{-3}$  m,  $\varepsilon_2 = 5,0 \cdot 10^{-4}$  m,  $\gamma = 7845$  N/m<sup>3</sup>,  $\nu = 2,3 \cdot 10^{-6}$  m<sup>2</sup>/s,  $g = 9,806$  m/s<sup>2</sup>,  $\theta = 20^\circ$ ,  $\alpha = 1$ ,  $\beta = 1$ .

**Determinare** le componenti della spinta sulla superficie curva di lunghezza  $L_3$  secondo un "conveniente" sistema di riferimento.



$$\mathbf{G} + \Pi_1 + \Pi_2 + \Pi_0 + \mathbf{M}_1 - \mathbf{M}_2 = 0 \quad \mathbf{S} = -\Pi_0 = \mathbf{G} + \Pi_1 + \Pi_2 + \mathbf{M}_1 - \mathbf{M}_2$$

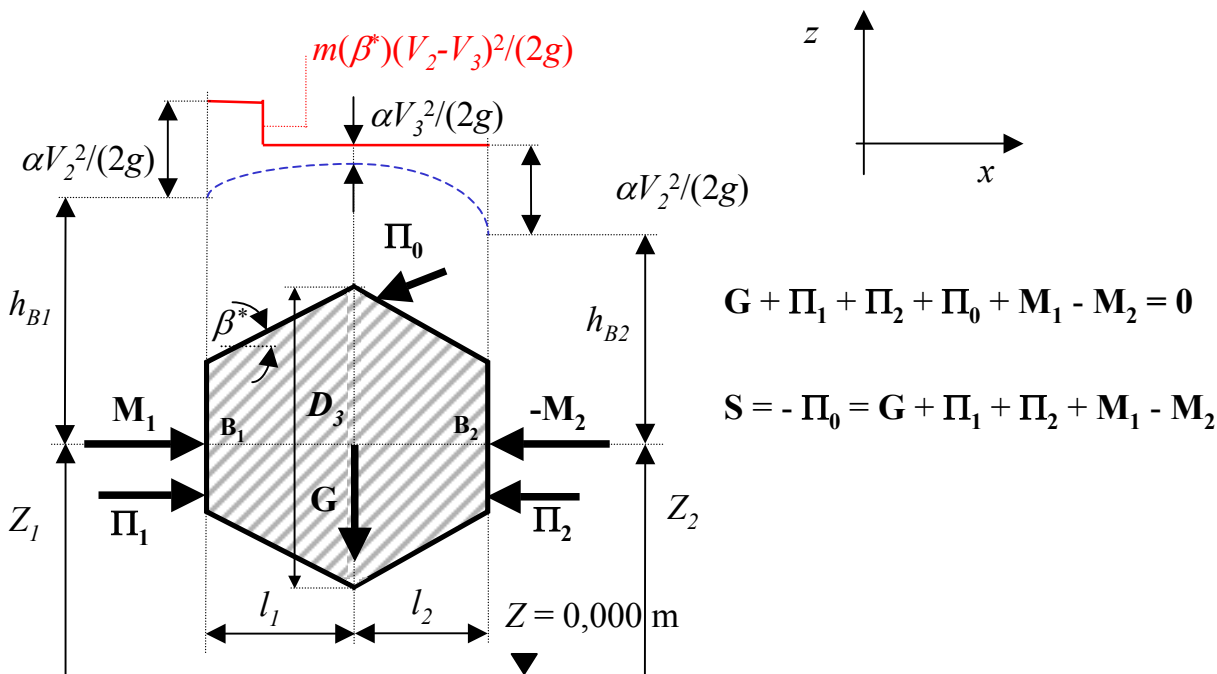
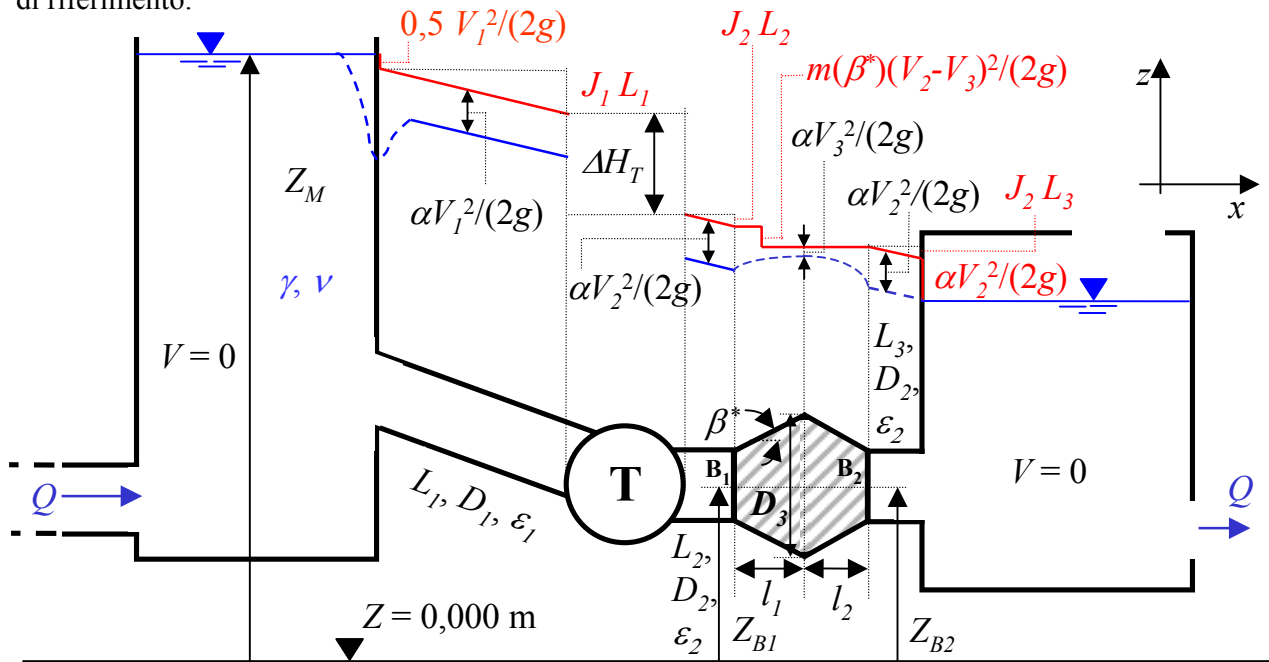
$$\left[ \begin{aligned} S_\xi &= (\Pi_1 + M_1 - \Pi_2 - M_2) + G \sin \theta = (\Pi_1 - \Pi_2) + G \sin \theta = 270 \text{ N} \\ S_\eta &= -G \cos \theta = -3648 \text{ N} \\ S &= [S_\xi^2 + S_\eta^2]^{1/2} = 3658 \text{ N} \end{aligned} \right. \quad \left. \begin{array}{c} \nearrow \\ \searrow \end{array} \right.$$



### Esercizio 55

**Noti:**  $Z_M = 100,000$  m,  $Z_{B1} = Z_{B2} = 15,000$  m,  $W_T = 100000$  W,  $Q = 0,300$  m<sup>3</sup>/s,  $m(\beta^*) = 0,7$ ,  $\alpha = 1$ ,  $\beta = 1$ ,  $L_1 = 100,000$  m,  $D_1 = 0,300$  m,  $\varepsilon_1 = 5,0 \cdot 10^{-4}$  m,  $L_2 = 10,000$  m,  $D_2 = 0,500$  m,  $\varepsilon_2 = 9,0 \cdot 10^{-4}$  m,  $D_3 = 0,700$  m,  $l_1 = l_2 = 0,951$  m,  $\gamma = 9806$  N/m<sup>3</sup>,  $\nu = 1,0 \cdot 10^{-6}$  m<sup>2</sup>/s,  $g = 9,806$  m/s<sup>2</sup>,  $\eta_T = 0,8$ .

**Determinare** le componenti della spinta sul tronco divergente+convergente secondo l'assegnato sistema di riferimento.



$$G + \Pi_1 + \Pi_2 + \Pi_0 + M_1 - M_2 = 0$$

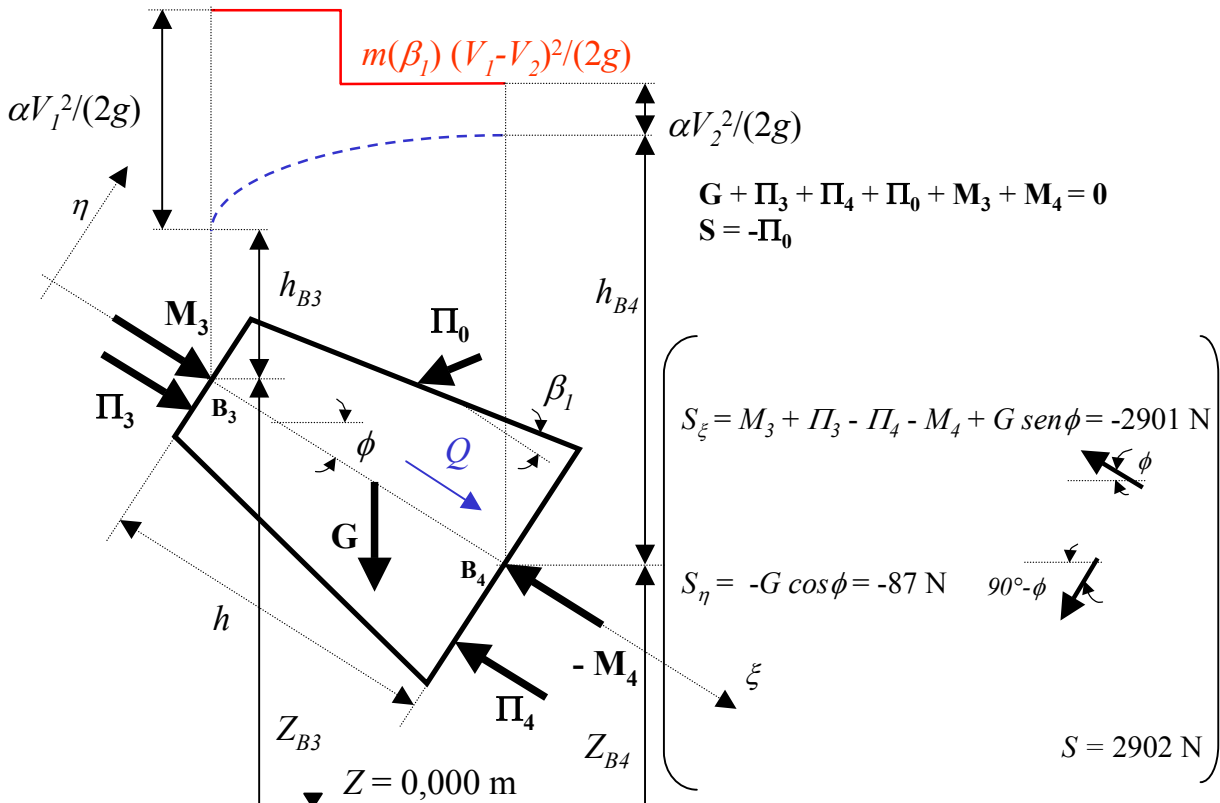
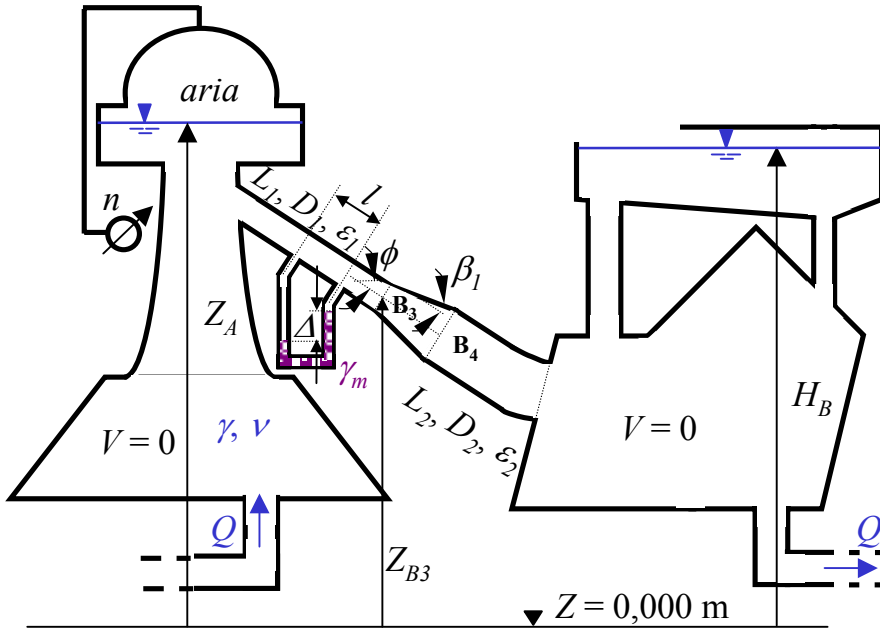
$$S = -\Pi_0 = G + \Pi_1 + \Pi_2 + M_1 - M_2$$

$$\left[ \begin{aligned} S_x &= (\Pi_1 + M_1 - \Pi_2 - M_2) = (\Pi_1 - \Pi_2) = \gamma A_2 m(\beta^*) (V_2 - V_3)^2 / (2g) = 38 \text{ N} \rightarrow \\ S_z &= -G = \gamma 1/3 \pi (l_1 + l_2) [(D_2/2)^2 + (D_3/2)^2 + (D_2/2 D_3/2)] = -5325 \text{ N} \downarrow \\ S &= [S_x^2 + S_z^2]^{1/2} = 5325 \text{ N} \end{aligned} \right]$$

### Esercizio 56

Noti:  $Z_A = 25,000$  m,  $Z_{B3} = 16,000$  m,  $n = 0,6$  bar,  $\alpha = 1$ ,  $L_1 = 12,000$  m,  $L_2 = 9,000$  m,  $l = 7,000$  m,  $D_1 = 0,200$  m,  $D_2 = 0,400$  m,  $\varepsilon_1 = 6,0 \cdot 10^{-4}$  m,  $\varepsilon_2 = 7,0 \cdot 10^{-4}$  m,  $\Delta = 0,150$  m  $\beta_1 = 30^\circ$ ,  $\phi = 33^\circ$ ,  $\beta = 1$ ,  $m(\beta_1) = 0,38$ ,  $\gamma = 8139$  N/m<sup>3</sup>,  $\nu = 1,2 \cdot 10^{-5}$  m<sup>2</sup>/s,  $\rho = 830$  kg/m<sup>3</sup>,  $\gamma_m = 133362$  N/m<sup>3</sup>,  $g = 9,806$  m/s<sup>2</sup>.

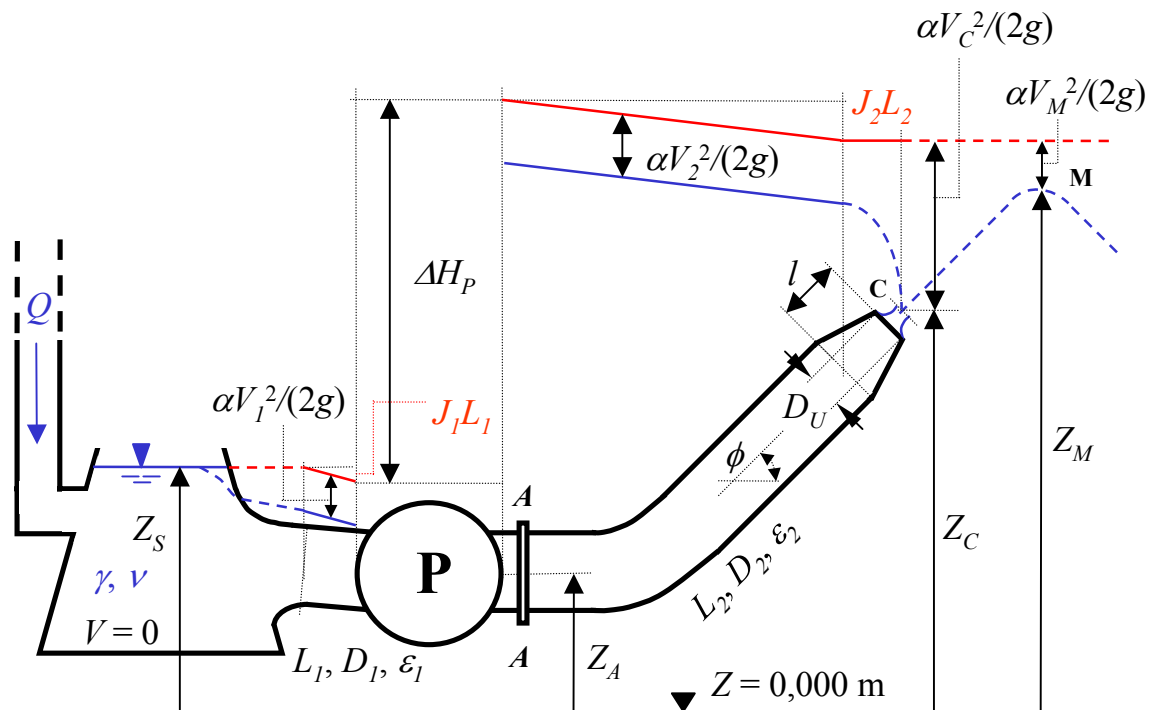
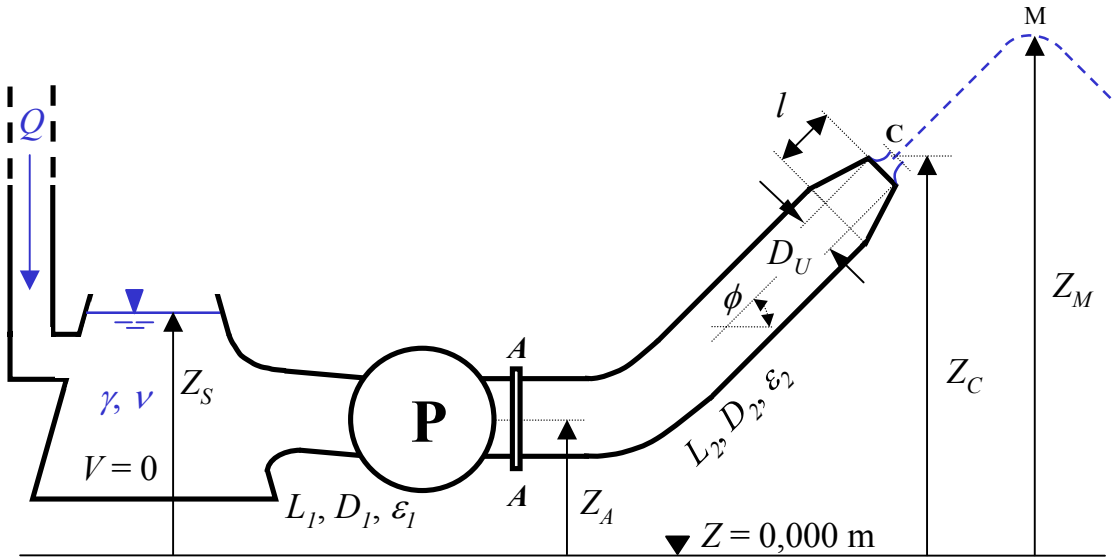
**Determinare** la portata circolante  $Q$ , il livello  $H_B$  del serbatoio di valle e la spinta  $S$  sul divergente troncoconico. **Tracciare** la *L.C.T.* e la *L.P.*.

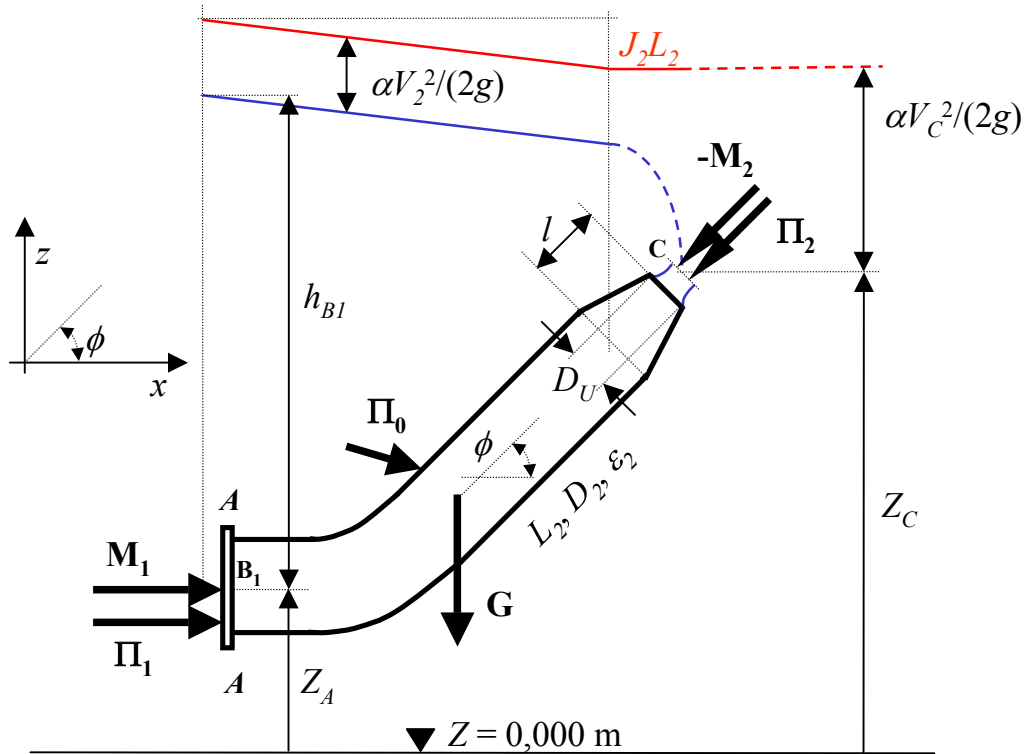


### Esercizio 57

**Noti:**  $Z_S = 9,000$  m,  $Z_A = 4,000$  m,  $Z_C = 11,500$  m,  $Z_M = 13,000$  m,  $\alpha = 1$ ,  $L_1 = 11,000$  m,  $D_1 = 0,250$  m,  $\varepsilon_1 = 1,0 \cdot 10^{-3}$  m,  $L_2 = 20,000$  m,  $D_2 = 0,200$  m,  $\varepsilon_2 = 5,0 \cdot 10^{-4}$  m,  $l = 0,286$  m,  $D_U = 0,150$  m,  $C_C = 0,80$ ,  $\gamma = 7845$  N/m<sup>3</sup>,  $\nu = 2,3 \cdot 10^{-6}$  m<sup>2</sup>/s,  $g = 9,806$  m/s<sup>2</sup>,  $\eta_p = 0,78$ ,  $\phi = 0,78$ ,  $\beta = 1$  – si consideri trascurabile la distanza tra la pompa e la flangia di traccia AA ed ideale il comportamento del liquido nell'atmosfera.

**Determinare** la portata  $Q$  transitante, la potenza  $W_p$  assorbita dalla pompa e le componenti della spinta sul tronco di tubazione compreso tra la flangia di traccia AA e l'ugello. **Tracciare** la L.C.T. e la L.P..





$$G + \Pi_1 + \Pi_2 + \Pi_0 + M_1 - M_2 = 0$$

$$S = -\Pi_0$$

$$Q = C_C A_U [2 g (Z_M - Z_C) / (\text{sen } \phi)^2]^{1/2} = 0,108 \text{ m}^3/\text{s}$$

$$W_p = \gamma Q \Delta H_p / \eta_p = 8024 \text{ W}$$

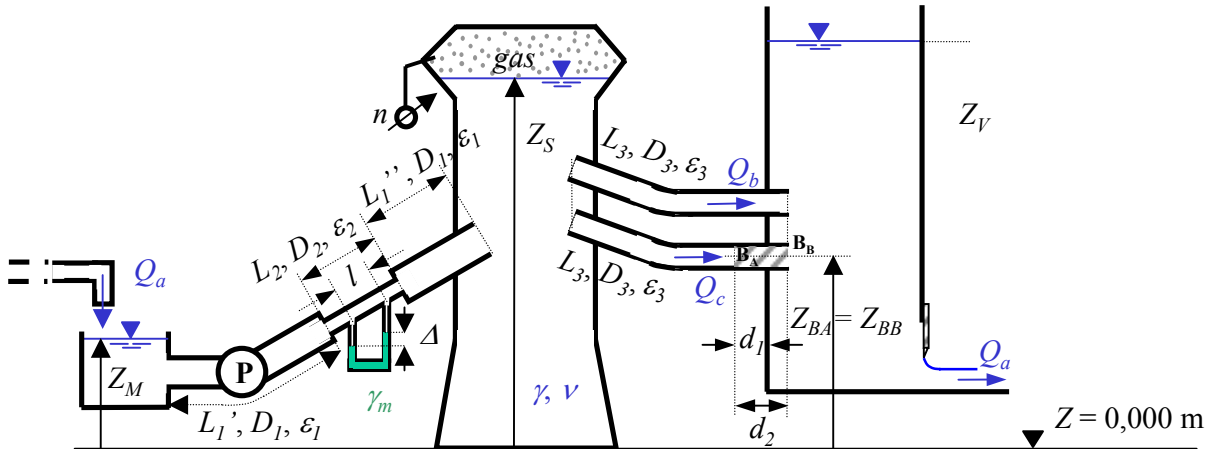
$$S_x = 2647 \text{ N} \longrightarrow \quad S_z = -5590 \text{ N} \downarrow$$

$$S = [S_x^2 + S_z^2]^{1/2} = 6185 \text{ N}$$

### Esercizio 58 (Tema d'esame del 15 Luglio 2002)

**Noti:**  $Z_M = 15,000$  m,  $Z_S = 55,000$  m,  $Z_A = Z_B = 35,000$  m,  $n = 0,500$  bar,  $\Delta = 0,050$  m,  $L_1' = 21,000$  m,  $L_1'' = 13,000$  m,  $L_2 = (10,000 + C/10)$  m,  $L_3 = 34,000$  m,  $D_1 = 0,350$  m,  $D_2 = 0,200$  m,  $D_3 = 0,150$  m,  $\varepsilon_1 = \varepsilon_2 = 7 \cdot 10^{-4}$  m,  $\varepsilon_3 = 9 \cdot 10^{-4}$  m,  $d_1 = 2,000$  m,  $d_2 = 8,000$  m,  $l = (7,000 + 0,05 N)$  m,  $\gamma = 9806$  N/m<sup>3</sup>,  $\gamma_m = 133362$  N/m<sup>3</sup>,  $\nu = 1 \cdot 10^{-6}$  m<sup>2</sup>/s,  $\eta_p = 0,78$ ,  $g = 9,806$  m/s<sup>2</sup>,  $\xi_{brusco\ restringimento} = 0,4$ ,  $\alpha = 1$ , moto permanente.

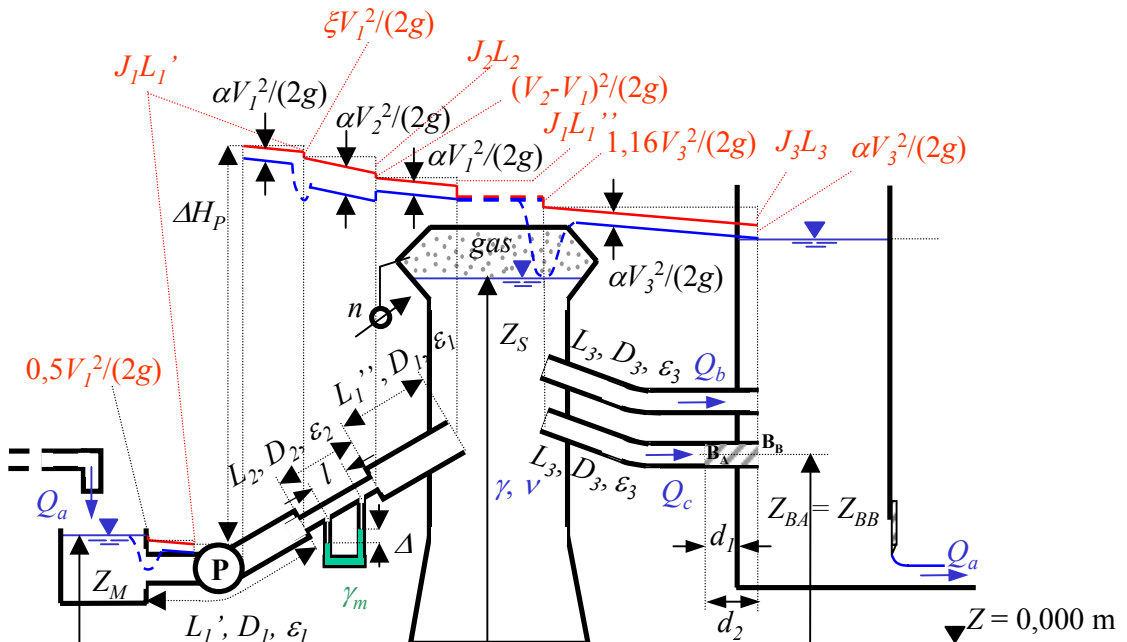
**Determinare** le portate  $Q_a$ ,  $Q_b$  e  $Q_c$  circolanti nell'impianto, la potenza  $W_P$  assorbita dalla pompa, il livello  $Z_V$  nel serbatoio di valle e le componenti della spinta sul tratto di tubazione orizzontale evidenziato in figura. **Tracciare** LCT e LP.

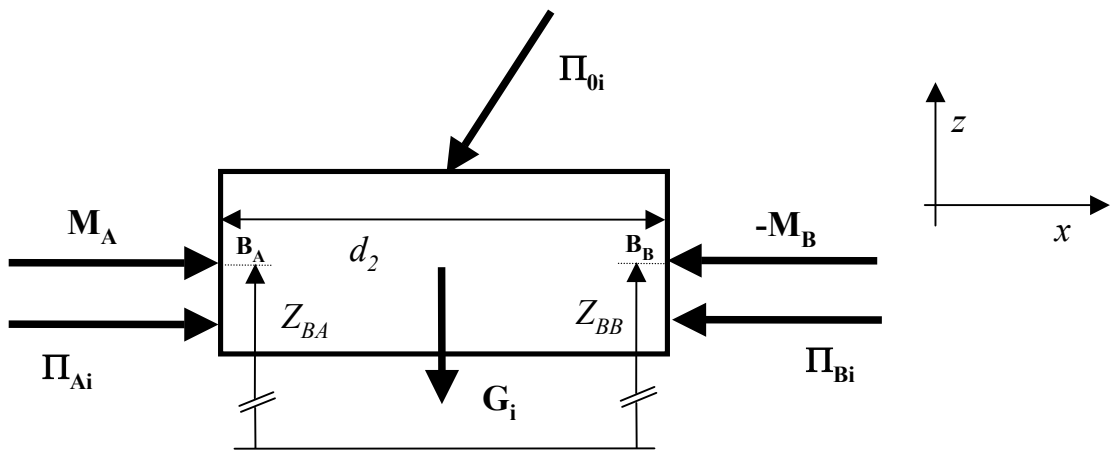


A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26

$N =$  prima lettera del nome = 1

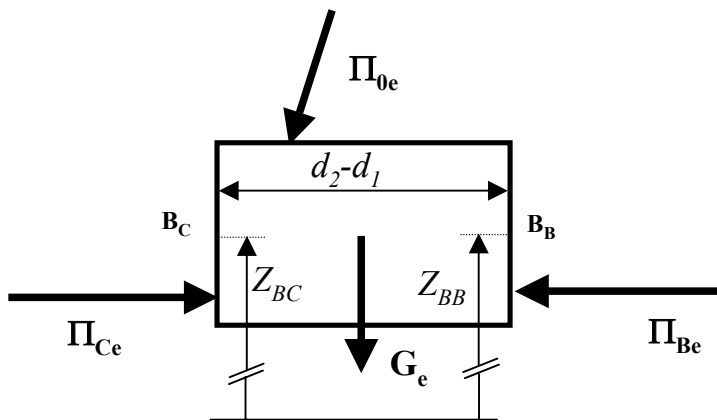
$C =$  prima lettera del cognome = 1





Spinta dovuta al fluido interno al tubo (pedice "i")

$$G_i + \Pi_{Ai} + \Pi_{Bi} + \Pi_{0i} + M_A - M_B = 0 \quad S_i = -\Pi_{0i} = G_i + \Pi_{Ai} + \Pi_{Bi}$$



Spinta dovuta al fluido esterno al tubo (pedice "e")

$$G_e + \Pi_{Ce} + \Pi_{Be} + \Pi_{0e} = 0 \quad S_e = \Pi_{0e} = -G_e$$

$$Q_a = A_2 [2gJ_2 D_2 / \lambda_2]^{1/2} = 0,112 \text{ m}^3/\text{s}$$

$$Q_b = Q_c = Q_a / 2 = 0,056 \text{ m}^3/\text{s}$$

$$S_x = \gamma J_3 d_2 A_3 = 153 \text{ N} \quad \longrightarrow$$

$$S = 379 \text{ N}$$

$$W_p = \gamma Q_a \Delta H_p / \eta_p = 66523 \text{ W}$$

$$Z_V = H_S - 1,16 V_3^2 / (2g) - J_3 L_3 - \alpha V_3^2 / (2g) = 55,232 \text{ m}$$

$$S_z = G_e - G_i = -347 \text{ N} \quad \downarrow$$